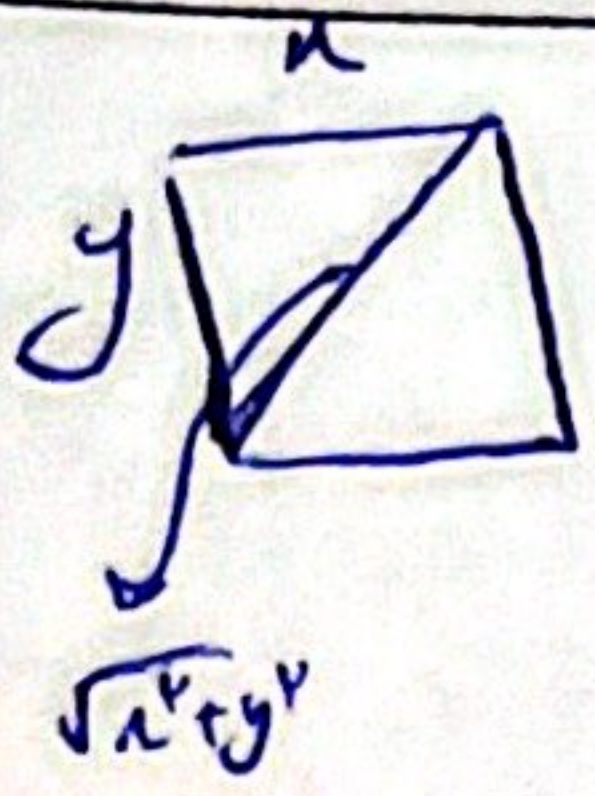


$$\frac{S_2}{S_1} = \frac{y(a+1)x \times F_n}{a \cdot y \cdot x^2} = \frac{1}{4}(a+1) \checkmark$$

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$$\frac{\sqrt{n^2 + y^2}}{n} = \frac{\sqrt{a+1}}{y}$$

$$\frac{n^2 + y^2}{n^2} = \frac{y + y\sqrt{a}}{y} = \frac{y + y\sqrt{a}}{y}$$

$$1 + \frac{y^2}{n^2} = \frac{y + y\sqrt{a}}{y} \rightarrow \frac{y^2}{n^2} = \frac{1 + \sqrt{a}}{y}$$

$$\frac{n^2}{y^2} = \frac{y}{1 + \sqrt{a}} = \frac{y(\sqrt{a} - 1)}{y^2} = \frac{\sqrt{a} - 1}{y} \checkmark$$

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$$\sqrt{y^2 + 6a + 4a} = y$$

$$\sqrt{y^2 + 6a} = y - 2a \rightarrow y - 2a > 0 \rightarrow \frac{y}{2} > a$$

$$y^2 + 6a = y^2 - 4ay + 4a^2$$

$$\sqrt{y^2 - 4ay + 4a^2} = y - 2a$$

$$y^2 - 4ay + 4a^2 = (y - 2a)^2$$

$$(y - 2a)^2 = (y - 2a)^2$$

$$\frac{y}{2} > a$$

$$a > y \propto \infty \rightarrow a = \frac{y}{2} \checkmark$$

$$\frac{a+1}{a} = 1 + \frac{1}{a}$$

$$1 + \frac{y}{2} = \frac{y}{2} \checkmark$$

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$$\frac{\sqrt{x+1}}{\sqrt{x-1} + 3} - \frac{\sqrt{x+1}}{x - \sqrt{x-1}} = \frac{x-1}{\sqrt{x-1}} \rightarrow D = (1, +\infty) - \{1\}$$

$$\sqrt{x+1} \left(\frac{x - \sqrt{x-1} - \sqrt{x-1}}{9 - (x-1)} \right) = \sqrt{x-1}$$

$$\sqrt{x+1} \left(\frac{x - 2\sqrt{x-1}}{8 - x} \right) = \sqrt{x-1}$$

$$x \neq 1 \rightarrow x\sqrt{x+1} = x - 1 \Rightarrow x \geq 10$$

$$x^2 + x = x^2 - 2x + 1 \rightarrow x^2 - 3x + 1 = 0 \rightarrow x = \frac{3 \pm \sqrt{9 - 4}}{2} = \frac{3 \pm \sqrt{5}}{2}$$

$$x = \frac{3 + \sqrt{5}}{2} \approx 2.618$$

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$$\frac{1}{x^2} + \frac{1}{(1-x)^2} = \frac{19}{9}$$

$$\frac{x^2 - 2x + 1}{(x^2 - 2x + 1)^2} + \frac{1}{(1-x)^2} = \frac{19}{9}$$

$$\frac{(x^2 - 2x + 1)^2}{t^2} = \frac{19}{9} \rightarrow \frac{t^2 + 2t + 1}{t^2} = \frac{19}{9} \rightarrow \frac{t+1}{t} = \pm \frac{13}{3}$$

$$\frac{x^2 + 2x + 1}{x^2 - 2x + 1} = \frac{13}{3} \rightarrow x = \frac{13 + \sqrt{13^2 - 4}}{2} = \frac{13 + \sqrt{169 - 4}}{2} = \frac{13 + \sqrt{165}}{2}$$

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$$\frac{t+1}{t} = \pm \frac{13}{3} \rightarrow \frac{1}{t} = \frac{13}{3} \rightarrow t = \frac{3}{13}$$

$$\frac{1}{t} = -\frac{13}{3} \rightarrow t = -\frac{3}{13}$$

$$x^2 - 2x - \frac{1}{9} = 0 \rightarrow x = \frac{2 \pm \sqrt{4 + \frac{4}{9}}}{2} = \frac{2 \pm \sqrt{\frac{40}{9}}}{2} = \frac{2 \pm \frac{2\sqrt{10}}{3}}{2} = 1 \pm \frac{\sqrt{10}}{3}$$

$$\sqrt{x + \sqrt{-x^2 + cx + pa - l}} + \sqrt{x^2 + \sqrt{-x^2 + pa - l}} = x + y$$

$$\begin{aligned} & \downarrow \\ & -x^2(x-c) + pa(x-c) \\ & \downarrow \\ & -(x-c)(x^2 - pa) \end{aligned}$$

$$\begin{aligned} & \downarrow \\ & -(x-c)(x^2 - pa) \\ & \downarrow \\ & \frac{-a \quad c \quad a}{+ \quad - \quad + \quad -} \end{aligned}$$

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$$-(x-c)(x-y)$$

$$\frac{y \quad c}{- \quad + \quad -}$$

(2)

$$1 \text{ (2)} \rightarrow x = y \rightarrow \sqrt{x} + \sqrt{x} = 9$$

$$\downarrow$$

$$x = \frac{81}{4} \checkmark \rightarrow \text{مطلوب}$$

$$y = |x+y| + |x-1|$$

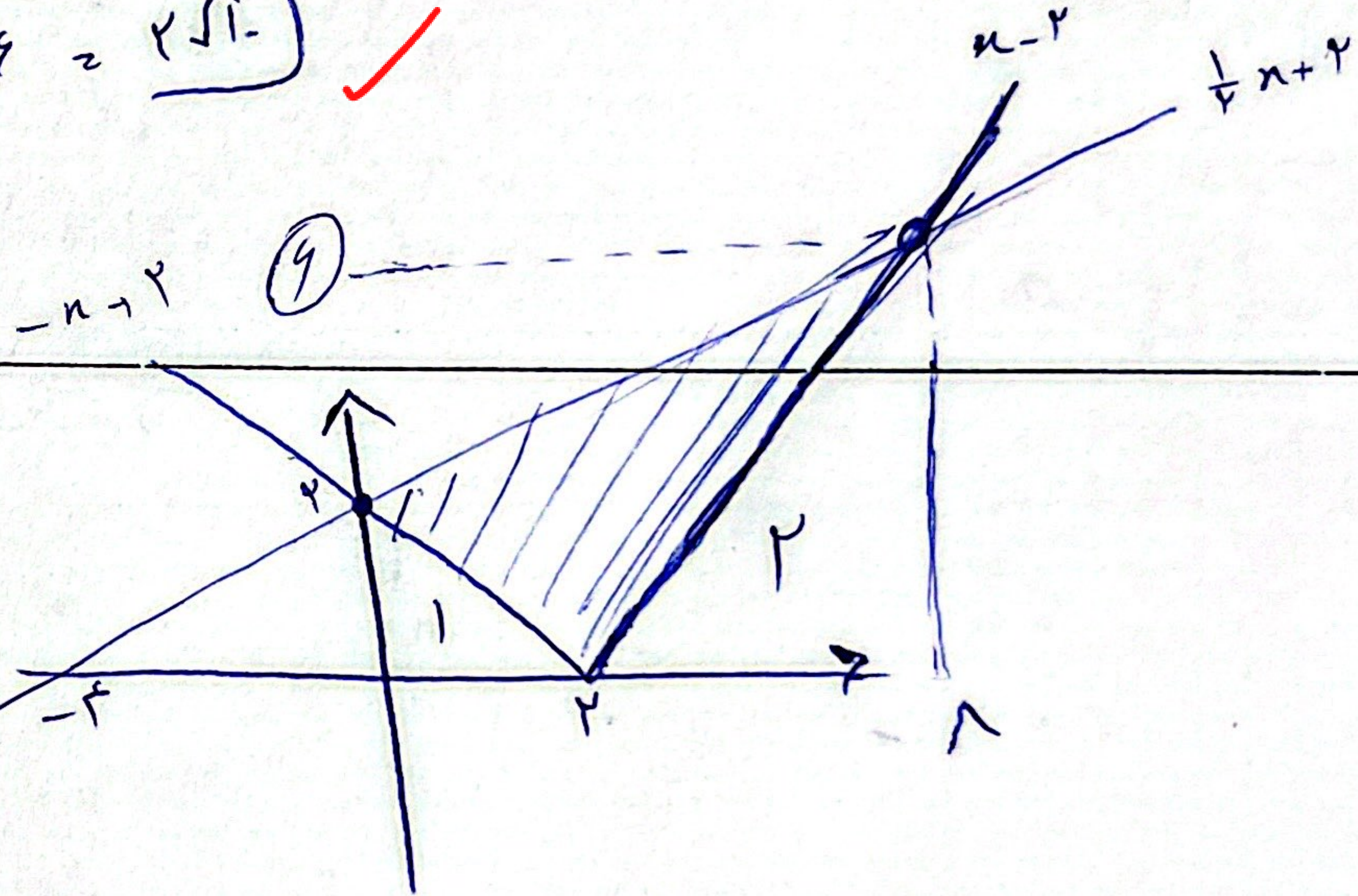
$$xy + x = 14$$

$$\begin{cases} x > 1 \\ -x < x < 1 \\ x \leq -1 \end{cases}$$

$$\begin{aligned} & \downarrow \\ & 4x + y + x = 14 \\ & \downarrow \\ & \sqrt{x} = 5 \rightarrow x = 25 \checkmark \\ & \downarrow \\ & 9 + x = 14 \rightarrow x = 5 \times \text{مطلوب} \\ & \downarrow \\ & -9x - y + x = 14 \\ & \downarrow \\ & -9x = 14 \rightarrow x = -\frac{14}{9} \checkmark \end{aligned}$$

$$A(x, y)$$

$$B(-c, v) \rightarrow |AB| = \sqrt{c^2 + v^2} = r \sqrt{1}$$



$$y = \sqrt{\frac{x^2 - cx + c}{(x-y)^2}} = |x-y|$$

$$y = \frac{1}{y}x + y$$

$$S_{\text{شکله}} = S_{\Delta} - S_1 - S_2$$

$$\downarrow$$

$$\frac{1 \times 1}{2} - \frac{y \times y}{2} - \frac{y \times y}{2} = 1 - y^2$$

$$\text{جزء اولی} = 2x - 9$$

$$\text{جزء دوم} = x + 9$$

$$\rightarrow \frac{1}{x} + \frac{1}{x+9} = \frac{1}{y} \rightarrow y(x+9) + y \cdot x = x^2 + 9x$$

$$c \cdot x + 2x$$

$$x^2 = 14/x - 14 \cdot 2$$

$$(x-14)(x+14) = 2$$

$$\text{حاصل می شود} = \frac{x = 14}{x = -14} \checkmark$$

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$$\frac{1}{\sqrt{r-n} + r} - \frac{1}{r - \sqrt{r-n}} = \frac{r-n}{\omega \sqrt{r-n}}$$

$r \neq r$

$$\frac{r - \sqrt{r-n} - \sqrt{r-n} - r}{\omega \sqrt{r-n}} = \frac{\sqrt{r-n}}{\omega}$$

$$\frac{r - (r-n)}{r + r}$$

$$\frac{r + r - 1}{r - 1}$$

✓ نافع جواب ہے