

$$f(x) = \sqrt{1-x^2} \rightarrow D_f = [-1, 1]$$

$$rg - wf = \{(-1, 2), (0, 5), (1, 4)\}$$

$$- (2 + 5 + 4 = 11) \checkmark$$

2

1

$$f(x) = 2x - 1, D_f = [3, +\infty) \rightarrow R_f = [5, +\infty)$$

$$g(x) = \frac{x}{x+3}, D_g = (-\infty, 3] \rightarrow R_g = (-\infty, 4]$$

$$\left. \begin{array}{l} f(x) = 2x - 1, D_f = [3, +\infty) \rightarrow R_f = [5, +\infty) \\ g(x) = \frac{x}{x+3}, D_g = (-\infty, 3] \rightarrow R_g = (-\infty, 4] \end{array} \right\} R_f \cup R_g = (-\infty, 4] \cup [5, +\infty) \checkmark$$

2

2

$$f(3) = 5 \quad f(4) = 7 \Rightarrow \text{صعودی است}$$

$$g(3) = 4 \quad g(4) = \frac{11}{7} \Rightarrow \text{نزولی است}$$

$$-\frac{x^2}{4} + x + 3 > \frac{3}{4} \rightarrow -\frac{x^2}{4} + x + \frac{9}{4} > 0$$

$$-\frac{x^2}{4} + x + \frac{9}{4} = 0 \rightarrow -(x^2 - 4x - 9) = 0 \rightarrow -(x-3)(x+1) = 0 \rightarrow x = 3 \text{ و } -1$$

$$\frac{x}{-1} + \frac{1}{-1} + \frac{9}{-1} \rightarrow x \in (-1, 3)$$

$$\Rightarrow \sqrt{b-a} = \sqrt{3-(-1)} = 2 \checkmark$$

2

3

$$y = |x-1| + |x-3| + |2x-5|$$

$$\begin{array}{c|c|c|c} 1 & 3 & 5 & \\ \hline x-1 & x-3 & 2x-5 & x-5 \end{array}$$

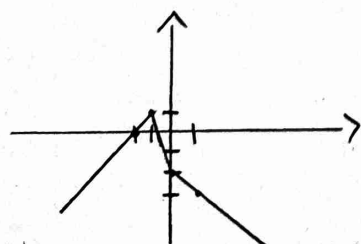
$$\left. \begin{array}{l} x \leq 1 \rightarrow R = [4, +\infty) \\ 1 < x \leq 3 \rightarrow R = [2, 4) \\ 3 < x \leq 5 \rightarrow R = (2, 4] \\ x > 5 \rightarrow R = [4, +\infty) \end{array} \right\} \min y = 2 \checkmark$$

2

4

$$y = |x| - 2|x+1|$$

$$\begin{array}{c|c|c} -1 & 0 & \\ \hline x & x+1 & x+1 \end{array}$$



$$y = (-\infty, 1] \checkmark$$

2

5

$$y = \frac{x^2 + \alpha x + m}{x+1} \rightarrow x^2 + \alpha x + m = yx + y \rightarrow x^2 + (\alpha - y)x + m - y = 0$$

$$x = \frac{y - \alpha \pm \sqrt{y^2 - 10y + 25 - 4m + 4y}}{2} \Rightarrow y^2 - 4y + 25 - 4m > 0 \rightarrow \alpha > 0, \alpha \leq 0$$

$$\rightarrow 36 - 100 + 14m \leq 0 \rightarrow 14m \leq 64 \rightarrow m \leq 4$$

$$m \in \mathbb{N} \Rightarrow m = \{1, 2, 3, 4\}$$

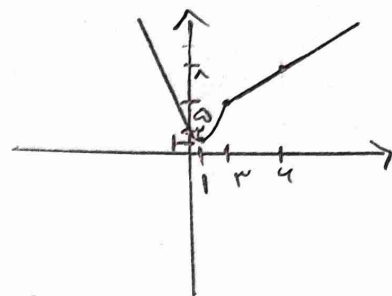
اینه $m = 4$ باشه ۳ از بد حذف میشه و
دقیقه ۱۸ نیست پس $m = \{1, 2, 3\}$

$$x > 3 \rightarrow R = [5, +\infty)$$

$$0 < x < 3 \rightarrow R = [1, 5)$$

$$x \leq 0 \rightarrow R = (2, +\infty)$$

$$R = [1, +\infty) \checkmark$$

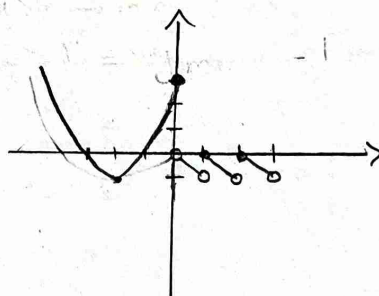


$$-1 > [0] - 0 > 0$$

$$x > 0 \rightarrow R = (-1, 0]$$

$$x \leq 0 \rightarrow R = [-1, +\infty)$$

$$\Rightarrow R_f = [-1, +\infty) \checkmark$$



$$y = \alpha + 1 - \sqrt{2x+3}$$

$$2x+3 > 0 \rightarrow x > -\frac{3}{2} \rightarrow D_f = [-\frac{3}{2}, +\infty) \rightarrow b = -\frac{3}{2} \checkmark$$

$$y = (-\infty, \underbrace{\alpha+1}_{\max}] \rightarrow \alpha+1 = \omega = \alpha = 4 \checkmark$$

$$ab = -\frac{3}{2} \times 4 = -6 \checkmark$$

$$f(x) + g(x) = 3\sqrt{2+2\sqrt{1-x^2}} = \sqrt{18+18\sqrt{1-x^2}} = \sqrt{(3\sqrt{1+x} + 3\sqrt{1-x})^2}$$

$$f(x) = 2\sqrt{x+1} + 4\sqrt{1-x} \rightarrow g(x) = \sqrt{x+1} - \sqrt{1-x} \quad D_f = D_g = [-1, 1]$$

$$y = \frac{f(x)}{4} - \frac{g(x)}{3} = \frac{f(x) - 4g(x)}{4} = \frac{4\sqrt{1-x}}{4} = \sqrt{1-x}$$

$$R_y = [0, 1] \rightarrow \text{باید توانی [0, 1] محاسب کنی}$$