

$$1) \lim_{x \rightarrow 1} \frac{x^2 - \sqrt{2x+3}}{\omega x^2 - \lambda x + \nu} = \frac{(x-1)(x+3)}{(x-1)(\omega x - \nu)} = \frac{x+3}{\omega x - \nu} = \frac{1}{\nu} \checkmark$$

(2)

$$2) \lim_{x \rightarrow 0} \frac{|x^2-1| - |x^2+1|}{x} = \frac{-(x^2-1) - (x^2+1)}{x} = -\frac{2x^2}{x} = -2 \checkmark$$

(2)

$$3) \lim_{x \rightarrow 4} \frac{3-x}{\sqrt{x}-2} = \frac{(\sqrt{x}-2)(\sqrt{x}+2)}{(\sqrt{x}-2)} = \sqrt{x}+2 = 2+2 = 4 \checkmark$$

(2)

$$4) \lim_{x \rightarrow 2} \frac{x - \sqrt{2x}}{\nu x^2 - \alpha - \gamma} \times \frac{x + \sqrt{2x}}{x + \sqrt{2x}} = \frac{x^2 - 2x}{(\nu x^2 - \alpha - \gamma)(x + \sqrt{2x})} = \frac{x(x-2)}{(x + \sqrt{2x})(\nu x^2 - \alpha - \gamma)} = \frac{1}{\nu} \checkmark$$

(2)

$$5) \lim_{x \rightarrow 1} \frac{1 - \sqrt{x}}{\nu - \sqrt{\omega - x}} \times \frac{1 + \sqrt{x}}{1 + \sqrt{x}} \times \frac{\nu + \sqrt{\omega - x}}{\nu + \sqrt{\omega - x}} = \frac{(1-x)(\nu + \sqrt{\omega - x})}{-(x - (\omega - x)) \times (1 + \sqrt{x})} = \frac{(1-x)(\nu + \sqrt{\omega - x})}{-(1-x)(1 + \sqrt{x})} = -\frac{\nu + \sqrt{\omega - x}}{1 + \sqrt{x}} = -\nu \checkmark$$

(2)

$$6) \lim_{x \rightarrow 8} \frac{\sqrt{x+8} - 8}{\sqrt{\omega x + \nu} - \nu} \times \frac{\sqrt{x+8} + 8}{\sqrt{x+8} + 8} \times \frac{\sqrt{(\omega x + \nu)^2 + \nu \sqrt{\omega x + \nu} + 9}}{\sqrt{(\omega x + \nu)^2 + \nu \sqrt{\omega x + \nu} + 9}} = \frac{(\nu x + 8 - 64)(\sqrt{(\omega x + \nu)^2 + \nu \sqrt{\omega x + \nu} + 9})}{(\omega x + \nu - 2\nu)(\sqrt{x+8} + 8)} = \frac{\nu \times (9 + 9 + 9)}{\omega x (\nu + \nu)} = \frac{11}{\nu} \checkmark$$

(2)

$$7) \lim_{x \rightarrow 1} \frac{\sqrt{x+2} - 2}{\sqrt{x} - 1} \times \frac{\sqrt{x+2} + 2}{\sqrt{x+2} + 2} \times \frac{\sqrt{x^2} + \sqrt{x} + 1}{\sqrt{x^2} + \sqrt{x} + 1} = \frac{(\nu x + 2 - 4)(\sqrt{x^2} + \sqrt{x} + 1)}{(x-1)(\sqrt{x+2} + 2)} = \frac{(\nu \sqrt{x} + 2)(\sqrt{x^2} + \sqrt{x} + 1)}{(\sqrt{x} + 1)(\sqrt{x+2} + 2)} = \frac{(\nu + 2)(1 + 1 + 1)}{(1 + 1)(\nu + 2)} = \frac{\nu + 2}{\nu} \checkmark$$

(2)

$$1) \lim_{x \rightarrow 0} \frac{1 + \cos^2 x}{\sin^2 x} = \frac{(1 + \cos^2) (\cos^2 x - \cos^2 x + 1)}{(1 - \cos^2 x)(1 + \cos^2 x)} = \frac{\cos^2 x - \cos^2 x + 1}{1 - \cos^2 x} = \frac{1+1}{1+1} = \frac{2}{2}$$

$$9) \lim_{x \rightarrow \frac{\pi}{4}} \frac{1 - \tan x}{\sin x - \cos x} = \frac{1 - \frac{\sin x}{\cos x}}{\sin x - \cos x} = \frac{\frac{\cos x - \sin x}{\cos x}}{\sin x - \cos x} = \frac{-1}{\cos x} = -\frac{1}{\frac{\sqrt{2}}{2}} = -\frac{2}{\sqrt{2}} = -\sqrt{2}$$

$$10) \lim_{x \rightarrow \frac{\pi}{4}} \frac{\tan^2 x - 1}{\cos^2 x} = \frac{\frac{\sin^2 x}{\cos^2 x} - 1}{\cos^2 x} = \frac{\frac{\sin^2 x - \cos^2 x}{\cos^2 x}}{\cos^2 x} = -\frac{1}{\cos^2 x} = -2$$