

$$M \begin{vmatrix} \frac{2+2}{2} \\ \frac{1-2}{2} \end{vmatrix} \rightarrow M \begin{vmatrix} 2 \\ 1 \end{vmatrix}$$

$$y = ax + b \rightarrow a = \frac{1 - (-4)}{2 - 2} = -\infty \rightarrow a \cdot a' = -1 \rightarrow a' = \frac{1}{\infty}$$

$$y = \frac{1}{\infty}x + b \xrightarrow{M \begin{vmatrix} 2 \\ 1 \end{vmatrix}} y = \frac{1}{\infty}x + \frac{1}{\infty} \checkmark$$

$$BC = \sqrt{(1-2)^2 + (-2-(-1))^2} = \sqrt{25} = 5$$

$$S_{ABC} = \frac{1}{2} \begin{vmatrix} 2 & 1 & 1 \\ -2 & 2 & 1 \\ -1 & 2 & 1 \end{vmatrix} = \frac{1}{2} (21 - 12 - 1 + 2 + 2 - 9) = 5 \checkmark$$

$$AH \cdot BC = 10 \rightarrow AH = 2 \checkmark \rightarrow BC - AH = 3 \checkmark$$

$$2y - x - 2 = 0 \quad \begin{cases} 4y - ax - 2 = 0 \rightarrow \frac{4}{2} = \frac{a}{1} \neq \frac{2}{\infty} \rightarrow a = 2 \end{cases}$$

$$\text{مقدار دایره} = \frac{|1-2-(-12)|}{\sqrt{4+2}} = \frac{12}{2\sqrt{5}} = \frac{6}{\sqrt{5}} \rightarrow \text{شعاع دایره} = \frac{3}{\sqrt{5}}$$

$$\text{مساحت دایره} = \pi r^2 = \frac{9}{5} \pi \checkmark$$

$$M \begin{vmatrix} \frac{2+2}{2} \\ \frac{2+1}{2} \end{vmatrix} \rightarrow M \begin{vmatrix} 2 \\ 2 \end{vmatrix}$$

$$x - 2 = -x + 0 \rightarrow x = \frac{2}{2}, y = \frac{2}{2} \rightarrow H \begin{vmatrix} \frac{2}{2} \\ \frac{2}{2} \end{vmatrix}$$

$$y = ax + b \rightarrow a = \frac{2-1}{2-2} = -1 \rightarrow a \cdot a' = -1 \rightarrow a' = 1$$

$$y = x + b \xrightarrow{C \begin{vmatrix} 2 \\ -2 \end{vmatrix}} y = x - 2 \quad \left\{ MH = \sqrt{\left(\frac{2}{2} - 2\right)^2 + \left(\frac{2}{2} - 2\right)^2} = \frac{\sqrt{2}}{2} \checkmark \right.$$

$$\frac{m+1}{2m-2} = \frac{5-m}{2m-2} \rightarrow 10m - 2m^2 - 20 + 4m = 2m^2 + m - 2$$

$$\rightarrow 4m^2 - 13m + 18 = 0 \rightarrow \Delta < 0 \rightarrow \text{هیچ مقدار} \checkmark$$

$$\begin{cases} x+2y=3 \\ y-2x=1 \end{cases} \rightarrow y=\frac{5}{5}, x=\frac{1}{5} \quad \begin{cases} x+2y=3 \\ x+y=4 \end{cases} \rightarrow y=-1, x=5$$

$\begin{cases} y-2x=1 \\ x+y=4 \end{cases} \rightarrow x=1, y=3$
 $y=mx+b \rightarrow m=\frac{0-3}{-1-1}=-1 \rightarrow d'=1$
 $y=x+\frac{4}{5} \rightarrow x+\frac{4}{5}=-x+3 \rightarrow x=\frac{11}{10}, y=\frac{19}{10}$
 $AM=\sqrt{(\frac{11}{10}-\frac{1}{5})^2+(\frac{19}{10}-\frac{5}{5})^2}=\frac{\sqrt{170}}{10}$

$B \begin{vmatrix} 1 & -1 \\ 0 & 1 \end{vmatrix} \rightarrow M \begin{vmatrix} \frac{1}{5} & -1 \\ 3 & 5 \end{vmatrix} \rightarrow AM=\sqrt{(\frac{1}{5}-1)^2+(10-\frac{1}{5})^2}$
 $\rightarrow AM=\frac{\sqrt{170}}{5}$

جواب صحیح به ...

$$y=-\frac{x}{2}+b \rightarrow y+\frac{x}{2}-b=0 \rightarrow \frac{|-b|}{\sqrt{\frac{5}{4}}}=\sqrt{2} \rightarrow b=5\sqrt{2}-5$$

$b=0 \rightarrow y=-\frac{x}{2}+0 \rightarrow A \begin{vmatrix} 0 & 1 \\ 0 & 1 \end{vmatrix} \rightarrow AB=\sqrt{125}=5\sqrt{5}$
 $b=-5 \rightarrow y=-\frac{x}{2}-5 \rightarrow A \begin{vmatrix} 0 & 1 \\ 0 & -1 \end{vmatrix} \rightarrow AB=\sqrt{125}=5\sqrt{5}$

$$my-2x=2m \rightarrow y=\frac{2}{m}x+2 \quad y+mx=x+2 \rightarrow y=(1-m)x+2$$

① و ② فرض از مبدأ فرد و متادله برابر است پس اختلاف مثلث برابر ۲ است
 تا به مثلث برابر است با اختلاف طول از مبدأ ۲ خط

$$\frac{2}{m}x+2=0 \rightarrow x=-\frac{m}{2} \quad (1-m)x+2=0 \rightarrow x=\frac{2}{m-1} \rightarrow |\frac{2}{m-1}+\frac{m}{2}| \times 2=0$$

$|\frac{2}{m-1}+\frac{m}{2}|=\frac{0}{2} \rightarrow \frac{m^2-m+2}{2m-2}=\frac{0}{2} \rightarrow 2m^2-12m+18=0$
 $\frac{m^2-m+2}{2m-2}=-\frac{0}{2} \rightarrow 2m^2+18m-2=0$
 $m=3$ به ضاعف (بنابراین دوبار ضرب کنیم)
 $\frac{c}{a} \times \frac{c'}{a'}=9 \times -1=-9$
 $\frac{c}{a}=-1$

$$A \begin{vmatrix} 2 & 1 \\ 1 & 1 \end{vmatrix}, M \begin{vmatrix} 2 & 1 \\ -2 & 1 \end{vmatrix} \rightarrow B \begin{vmatrix} 2 & 1 \\ 1 & 1 \end{vmatrix}$$

$y=2x+b \xrightarrow{B \begin{vmatrix} 2 & 1 \\ 1 & 1 \end{vmatrix}} y=2x-9$

$$y=-x+b \xrightarrow{A \begin{vmatrix} 1 & 1 \\ 1 & 1 \end{vmatrix}} y=-x+3 \rightarrow \begin{cases} y=-x+3 \\ y=x+0 \end{cases} \rightarrow y=3, x=-1$$

$\rightarrow M \begin{vmatrix} -1 & 1 \\ 1 & 1 \end{vmatrix}, A \begin{vmatrix} 1 & 1 \\ 1 & 1 \end{vmatrix} \rightarrow A' \begin{vmatrix} -3 & 1 \\ 4 & 1 \end{vmatrix} \rightarrow 2b-a=2(4)-(-3)=11$

AC و AB بخورد $\rightarrow A(1,1)$

AB و BC بخورد $\rightarrow B(5,-1)$

BC و AC بخورد $\rightarrow C(\frac{5}{3}, \frac{7}{3})$

$$\left\{ \begin{array}{l} \rightarrow m = (\frac{1}{3}, \frac{2}{3}) \\ B, C \end{array} \right.$$

$$AM = \frac{\sqrt{50}}{3}$$

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$$BC : A \text{ فاصله} = AH = \frac{|1+1-4|}{\sqrt{2}} = \sqrt{2}$$

$$\frac{AM}{AH} = \frac{5}{3}$$