

$$1) \text{ ا) } y = ax + b \rightarrow a = \frac{dy}{dx} = \frac{2 - (-2)}{4 - 0} = \frac{4}{-1} = -4$$

$$\rightarrow y = -4x + b \rightarrow 2 = -4(4) + b \rightarrow b = 18 \rightarrow y = -4x + 18$$

$$ب) 2y + 4x + C = 0 \rightarrow 2(2) + 4(4) + C = 0 \rightarrow C = -20$$

$$\rightarrow 2y + 4x - 20 = 0$$

$$2) x + 3y = 1 \rightarrow a = -\frac{1}{3} \rightarrow a' = 3 \rightarrow y = 3x + b \rightarrow 2 = 3(1) + b \rightarrow b = -1 \rightarrow y = 3x - 1$$

$$2) \tan \frac{\theta}{2} = \left| \frac{m - m_1}{1 + m m_1} \right| \rightarrow \sqrt{3} = m \rightarrow y = \sqrt{3}x + b$$

$$\rightarrow 2 = \sqrt{3} + b \rightarrow b = 2 - \sqrt{3} \rightarrow y = \sqrt{3}x + 2 - \sqrt{3}$$

$$\text{ان) } \sqrt{\frac{(2 - (-1))^2}{9} + \frac{(3 - 1)^2}{16}} = 1$$

$$ب) \frac{|(12 \times 2) + (4 \times 3) - 3|}{\sqrt{9 + 16}} = \frac{4 + 12 - 3}{5} = 3$$

$$1) \quad rx + y = 1 \xrightarrow{\text{wh}} rx + ry = r \quad - \text{K}$$

$$rx + ry = 4$$

$$\text{do: } rx + ry - \frac{r^2 y}{r} = rx + ry - \Delta \phi$$

$$\therefore \frac{|-1 - (-r)|}{\sqrt{r+9}} = \frac{r}{\sqrt{1r}} =$$

$$\frac{|rx - ry - 1|}{\sqrt{1r}} = \frac{|rx + ry - r|}{\sqrt{1r}} \quad - \text{K}$$

$$rx - ry - 1 = rx + ry - r \rightarrow x - 4y + r = 0$$

$$rx - ry - 1 = -rx - ry + r \rightarrow 4x + y - r = 0$$

$$a = r, a' = r \rightarrow \tan \theta = \left| \frac{\frac{-r}{1} - \frac{-r}{-4}}{\frac{1}{1} + \frac{r}{-4}} \right| = 1 \quad - \Delta$$

$$\rightarrow \tan \theta = 1 \rightarrow \theta = 45^\circ$$



$$4 - \sqrt{\frac{(-4+3)^2}{4} + \frac{(4-(-2))^2}{4}} = 10$$

$$ب) \frac{-4+3}{2} = x = -1, \frac{4-2}{2} = y = 1 \rightarrow \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$5 - \frac{-10-2+3}{3} = x = -3, y = \frac{-13+3+1}{3} = -3$$

$$\begin{pmatrix} -3 \\ -3 \end{pmatrix}$$

$$ج) S = \frac{1}{2} \begin{vmatrix} -10 & -13 & 1 \\ -2 & 3 & 1 \\ 3 & 1 & 1 \end{vmatrix} = \frac{1}{2} (9 + 24 - 10 - (-30 - 39 - 2))$$

$$= \frac{1}{2} (9 + 24 + 41) = 37$$

$$الف) -y = \frac{2x+1}{4x-3} \rightarrow y = \frac{-2x-1}{4x-3}$$

$$ب) y = \frac{-2x+1}{-4x-3}$$

$$ج) x = \frac{2y+1}{4y-3} \rightarrow y = \frac{2x+1}{4x-3}$$

$$د) -x = \frac{-2y+1}{-4y-3} \rightarrow y = \frac{2x-1}{-4x-2}$$

$$\text{c)} \quad x' \leq x-2 \rightarrow x \leq x'+2$$

$$y' \leq y+3 \rightarrow y \leq y'-3$$

$$y'-3 \leq \frac{2(x'+2)+1}{x'+2-3} \leq \frac{2x'+5}{x'-1} \leq \frac{2x'+4}{x'-1}$$

$$\rightarrow y' \leq \frac{2x'+4}{x'-1} + 3 \leq \frac{2x'+4 + 3x' - 3}{x'-1} \leq \frac{5x'+1}{x'-1}$$

$$\begin{aligned} \text{d)} \quad x' \leq x-3 &\rightarrow x \leq x'+3 \\ y' \leq y-2 &\rightarrow y \leq y'+2 \end{aligned} \rightarrow y'+2 \leq \frac{2(x'+3)+1}{(x'+3)-2}$$

$$\rightarrow y'+2 \leq \frac{2x'+7+1}{x'} \leq \frac{2x'+8}{x'} \rightarrow y' \leq \frac{2x'+6}{x'} - 2$$

$$y' \leq \frac{2x'+6-2x'}{x'} \leq \frac{6}{x'}$$

$$\text{e)} \quad 3x+4y \leq 2 \rightarrow 3x+4y \leq 2$$

$$(x-4y \leq 1) \times 3 \rightarrow 3x-12y \leq 3$$

$$19y \leq -1 \rightarrow y \leq \frac{-1}{19} \rightarrow x \leq \frac{15}{19}$$

$$\Rightarrow x \leq \frac{2-(-10)}{-14-(4)} \leq \frac{12}{18} \Rightarrow y \leq \frac{3-2}{-14-3} \leq \frac{-1}{17}$$