

$$f(x) = \sqrt{1-x^2} \quad g = \{(-1,1)(0,1)(1,1)\}$$

$$Df = \sqrt{(1-x)(1+x)} \quad \frac{-1}{-b+b} \quad Df = [-1,1]$$

$$^1 f(x) = \{(-1,0)(0,1)(1,0)\}$$

$$^2 g(x) = \{(-1,1)(0,1)(1,1)\}$$

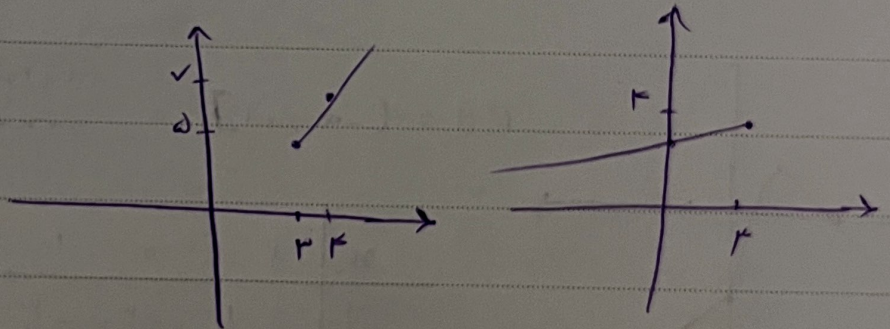
$$^2 g - ^1 f = \{(-1,1)(0,1)(1,1)\} \rightarrow 1+0+1=2$$

$$f(x) = 2x-1 \quad Df = [1,+\infty)$$

$$g(x) = \frac{1}{2}x + 1 \quad Dg = (-\infty, 1]$$

$$Rf + Rg = ?$$

$$(-\infty, 1] \cup [1, +\infty)$$



$$y = -\frac{x^2}{r} + x + r \quad R_y \xrightarrow{\text{min}} (a,b) \rightarrow (\frac{r}{2}, +\infty)$$

$$\max \sqrt{b-a} \quad \sqrt{r-(-1)} = r \quad -\frac{x^2}{r} + x + r \geq r$$

$$-x^2 + x + r \geq r$$

$$-(x^2 - x - r) \geq 0$$

$$-(x-r)(x+1) \geq 0$$

$$\frac{-1}{-d+b}$$

$$(-1, r) \rightarrow \frac{r}{2}$$

$$a = -1$$

$$b = r$$

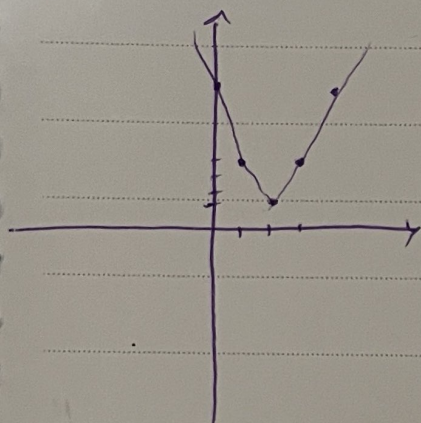
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$$\min y = ?$$

$$y = |x-1| + |x-2| + |2x-3|$$

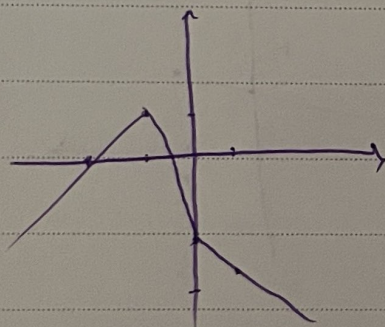
|                   |                  |                  |                  |
|-------------------|------------------|------------------|------------------|
| $x < 1$           | $1 < x < 2$      | $2 < x < 3$      | $x > 3$          |
| $-x+1 -x+2 -2x+3$ | $x-1 -x+2 -2x+3$ | $x-1 -x+2 +2x-3$ | $x-1 +x-2 +2x-3$ |
| $-3x+6$           | $-2x+2$          | $x-1$            | $3x-6$           |



$$\min y = 1$$

| x | 0 | 1 | 2 | 3 | 4 |
|---|---|---|---|---|---|
| y | 6 | 2 | 1 | 2 | 6 |

$$R_y = \mathbb{R}$$



$$R_y = (-\infty, 1]$$

|                  |                  |                  |                  |
|------------------|------------------|------------------|------------------|
| $x < -1$         | $-1 < x < 1$     | $1 < x < 2$      | $x > 2$          |
| $-x-1 -x+1 -x+2$ | $-x-1 -x+1 -x+2$ | $-x-1 +x-1 -x+2$ | $-x-1 +x-1 +x-2$ |
| $-2x$            | $-2x$            | $-x$             | $x-4$            |

| x | -1 | 0 | 1 | 2 |
|---|----|---|---|---|
| y | 1  | 1 | 1 | 1 |

$$m \text{ is a real number} \rightarrow R_y = \mathbb{R}$$

$$y = \frac{x^2 + 2x + m}{x+1}$$

$$x^2 + (2-y)x + m-y = 0 \quad x = \frac{y-2 \pm \sqrt{(2-y)^2 - 4(m-y)}}{2} \Rightarrow y^2 - 4y + 4 - 4m + 4y = 0$$

$$y^2 - 4y + 4 - 4m \leq 0 \Rightarrow (y-2)^2 - 4m \leq 0 \Rightarrow (y-2)^2 \leq 4m$$

$$y^2 - 4y + 4 - 4m \geq 0$$

$$\Rightarrow (y-2)^2 \leq 4m \Rightarrow 14m \leq 4 \Rightarrow m \leq \frac{1}{4}$$

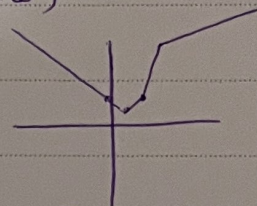
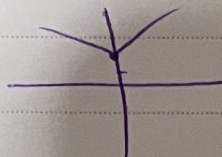
$$m \leq \frac{1}{4} \Rightarrow \{1, 2, 3\} \text{ are not solutions} \leftarrow \frac{x^2 + 2x + \frac{1}{4}}{x+1} = \frac{(x+1)^2 - \frac{3}{4}}{(x+1)} = x - \frac{3}{4(x+1)}$$

$$R_f = ?$$

$$f(x) = \begin{cases} x+r, & x \geq r \\ x^r - rx + r, & 0 \leq x < r \\ |x| + r, & x < 0 \end{cases} \quad R_f = [0, +\infty)$$

$$\begin{array}{c|cc} x & r & 0 \\ \hline y & r & r \end{array}$$

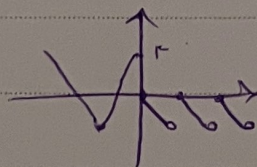
$$\begin{array}{c|ccc} x & 0 & -1 & \\ \hline y & r & r & r \end{array}$$



$$R_f = [1, +\infty)$$

$$R_f = ?$$

$$f(x) = \begin{cases} x^r + rx + r & x \geq 0 \rightarrow S| = r \\ [rx] - rx & x < 0 \rightarrow R_f = (-1, 0] \end{cases} \quad R_f = [-1, +\infty)$$



$$y = a + 1 - \sqrt{rx + r}$$

$$D_f = [b, +\infty)$$

$$R_f = (-\infty, 0]$$

$$D_f = rx + r \geq 0 \rightarrow x \geq -\frac{r}{r} = -1$$

$$R_f \rightarrow y_{\max} \rightarrow \sqrt{rx + r} \rightarrow \min \rightarrow \sqrt{rx + r} = 0 \rightarrow x = -\frac{r}{r} = -1, y = 0$$

$$ab$$

$$y = a + 1 - 0 \rightarrow 1$$

$$a = 1$$

$$\left(-\frac{r}{r}\right) \times 1 = -1$$

$$f(x) = r\sqrt{x+1} + \varepsilon\sqrt{1-x} \quad x+1 \geq 0 \rightarrow x \geq -1$$

$$f(x) + g(x) = r\sqrt{r+x} + \varepsilon\sqrt{1-x} \quad 1-x \geq 0 \rightarrow x \leq 1 \quad x \in [-1, 1]$$

$$D_f = D_g$$

$$f(1) = r\sqrt{r} + \varepsilon\sqrt{0} = r\sqrt{r} \quad f(-1) = \varepsilon\sqrt{2} \quad f(0) = r$$

$$R_f = ?$$

$$f(1) + g(1) = r\sqrt{r+x} + \varepsilon\sqrt{1-x} = g(1) = r\sqrt{r} - \varepsilon\sqrt{r} = \sqrt{r}$$

$$y = \frac{f(x)}{r} - \frac{g(x)}{r}$$

$$f(-1) + g(-1) = r\sqrt{r+x} + \varepsilon\sqrt{1-x} = g(-1) = r\sqrt{r} - \varepsilon\sqrt{r} = \sqrt{r}$$

$$y(1) = \frac{r\sqrt{r}}{r} - \frac{\sqrt{r}}{r} = 0$$

$$y(-1) = \frac{\varepsilon\sqrt{r}}{r} - \frac{\sqrt{r}}{r} = \frac{\varepsilon\sqrt{r}}{r} = \sqrt{r}$$