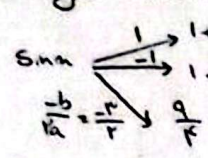
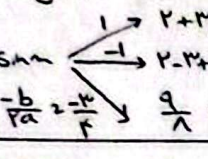


 CamScanner

ا) $y = r \sin n + r \cos n \rightarrow \sqrt{a^2 + b^2} = \sqrt{1+1} = \sqrt{2} \rightarrow R_f = [-\sqrt{2}, \sqrt{2}]$ ب) $y = r \sin n - r \cos n \rightarrow \sqrt{a^2 + b^2} = \sqrt{1+1} = \sqrt{2} \rightarrow R_f = [-\sqrt{2}, \sqrt{2}]$ ج) $y = [r \sin n + r \cos n] \rightarrow \sqrt{a^2 + b^2} = \sqrt{1+1} = \sqrt{2} \rightarrow [-\sqrt{2}, \sqrt{2}] \rightarrow R_f = \left\{ \begin{matrix} -\sqrt{2}, \pm \sqrt{2}, \pm \sqrt{2} \\ \pm \sqrt{2}, \pm \sqrt{2}, 0 \end{matrix} \right\}$ د) $y = \sqrt{\cos n - r \sin n} \rightarrow \sqrt{a^2 + b^2} = \sqrt{1+1} = \sqrt{2} \rightarrow \sqrt{[-\sqrt{2}, \sqrt{2}]} \Rightarrow R_f = [0, \sqrt{2}]$	
ا) $y = r \sin^2 n + r \cos^2 n$  $\Rightarrow R_f = [0, 1]$ ب) $y = r \sin^2 n + r \cos^2 n$  $\Rightarrow R_f = \left[\frac{1}{\sqrt{2}}, \sqrt{2} \right]$	٧
ا) $y = \sin^2 n + \frac{r \cos^2 n}{\cos^2 n + \cos^2 n} = \frac{(\sin^2 n + \cos^2 n) + r \cos^2 n}{2} \rightarrow R_f = [1, \frac{1+r}{2}]$ ب) $y = \frac{r \cot n}{1 + \cot^2 n} = \frac{r \cos n}{\sin n} \times \sin^2 n = r \sin n \cos n = \frac{r}{2} \sin 2n$ $\Rightarrow R_f = [-\frac{r}{2}, \frac{r}{2}]$	٨
ا) $y = \sin^4 n + \cos^4 n \rightarrow \left(\frac{1-r}{2} \right) \left(\sin^2 n + \cos^2 n \right) \Rightarrow R_f = \left[\frac{1-r}{2}, 1 \right]$ ب) $y = [\sin^4 n + \cos^4 n] \Rightarrow \left[\left[\frac{1-r}{2}, 1 \right] \right] \Rightarrow R_f = \left\{ \frac{1-r}{2}, 1 \right\}$ $\left(\frac{1-r}{2} \right) \left(\sin^2 n + \cos^2 n \right)$	٩
ا) $y = \frac{r n^2 + 1/n - r}{n+r} = \frac{(n+r)(n-1)}{(n+r)} = n-1 \rightarrow R = \mathbb{R} \rightarrow R_f = \mathbb{R} - \{-1\}$ $n \neq -r \rightarrow R = -1$ ب) $y = \frac{n^2-1}{n-1} = \frac{(n-1)(n+1)}{(n-1)} = n+1$ $\min \left \frac{-1}{r} \right \Rightarrow R_f = \left[\frac{r}{r}, +\infty \right)$	١٠