

١. ٥

$$\text{الف) } y = x^3 - 3x^2 + 3x \rightarrow (x-1)^3 + 1 \rightarrow y-1 = (x-1)^3 \rightarrow x = \sqrt[3]{y-1} + 1 \rightarrow R_f = \mathbb{R}$$

$$\text{ب) } y = \frac{1}{x^2 - 1} \rightarrow yx^2 - 2xy - 1 = 0 \rightarrow \frac{2y \pm \sqrt{4y^2 + 4y}}{2y} \rightarrow 2\sqrt{y(y+1)} \rightarrow \frac{-1 \pm \sqrt{1+4y}}{2y} + \frac{1}{2y} + \frac{1}{2y}$$

$$R_f = (-\infty, -1] \cup (0, +\infty)$$

$$\text{الف) } y = x^2 - 4x + 1 \rightarrow y = \frac{-\Delta}{4a} = \frac{-(16 - 4 \cdot 1 \cdot 1)}{4 \cdot 1} = 4 \rightarrow R = [4, +\infty)$$

$$\text{ب) } y = -x^2 + 4x + 2 \rightarrow y = \frac{-(16 - 4(-1)(2))}{-4} = 12 \rightarrow R = (-\infty, 12]$$

$$\text{ج) } y = \sqrt{x^2 - 4x - 2} \rightarrow y = \frac{-(16 - 4 \cdot 1 \cdot (-2))}{4} = -5 \rightarrow R = \sqrt{[-5, +\infty)} \cup [0, +\infty)$$

$$\text{د) } y = \sqrt{-x^2 + 4x} \rightarrow y = \frac{-(16 - 4 \cdot (-1) \cdot 0)}{-4} = 4 \rightarrow R = \sqrt{(-4, 4)} \cup [0, 4]$$

$$\text{الف) } y = x^3 - 6x^2 + 9x + 1 \rightarrow R = \mathbb{R}$$

$$\text{ب) } y = x^3 - 4x^2 + 3x + 2 \rightarrow R = \mathbb{R}$$

$$\text{ج) } y = \sqrt{x^3 - 4x^2 + 6x + 1} \rightarrow R = [0, +\infty)$$

$$\text{د) } y = (x^3 - 4x^2 + 3x + 1)^2 \rightarrow R = [0, +\infty)$$

٢. ٥

$$\text{الف) } y = \frac{3x+1}{x-2} \rightarrow R = \mathbb{R} - \{3\}$$

$$\text{ب) } y = \frac{2x+1}{x+1} \rightarrow R = \mathbb{R} - \{1\}$$

$$\text{الف) } y = \sqrt{\frac{2x+1}{x+1}} \rightarrow R = \sqrt{\mathbb{R} - \{1\}} \rightarrow R = [0, +\infty) - \{\sqrt{1}\}$$

$$\text{ب) } y = \sqrt{\frac{2x+1}{x}} \rightarrow y = \sqrt{\frac{3x+1}{-x+1}} \rightarrow R = \sqrt{\mathbb{R} - \{1\}} \rightarrow R = [0, +\infty)$$

٣. ٥

6. 5

الف) $y = \frac{2x - 3}{x + 1}$

→ -1 جانب عمودي

→ 2 جانب افقي

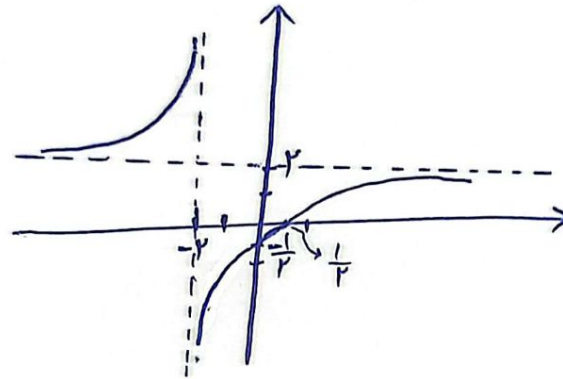
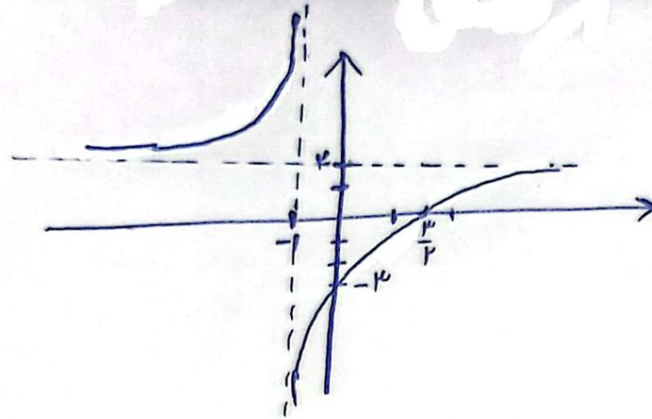
$$\frac{2}{1} - (-3) = 5 > 0$$

ب) $y = \frac{2x - 1}{x + 2}$

→ -2 جانب عمودي

→ 2 جانب افقي

$$\frac{2}{-2} - (-1) = -1 + 1 = 0$$



$$a) y = \sin x + \frac{1}{\sin x} \rightarrow D: (-\frac{\pi}{2}, 0) \cup (\pi, \frac{3\pi}{2})$$

5.7

$$b) y = \frac{x^4 + 1}{x^4} = 1 + \frac{1}{x^4} \rightarrow D: (-\infty, -1] \cup [1, +\infty)$$

$$c) y = \frac{\sqrt[3]{x^3 + 1}}{\sqrt[3]{x^3}} = \sqrt[3]{x} + \frac{1}{\sqrt[3]{x}} \rightarrow D: (-\infty, -1] \cup [1, +\infty)$$

$$d) y = \sqrt{x} + \frac{1}{\sqrt{x}} \rightarrow D: [1, +\infty)$$

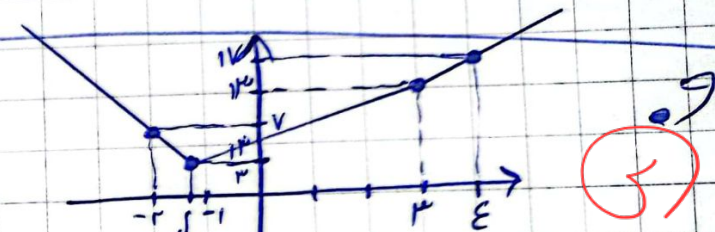
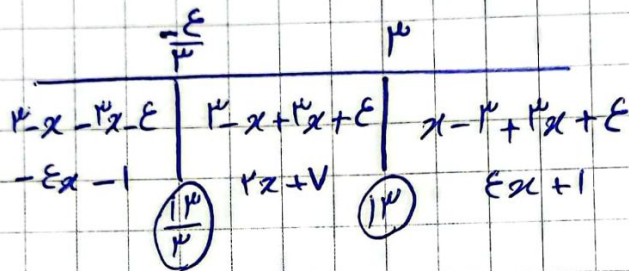
$$e) y = x^k + \frac{1}{x^k + k} \rightarrow \left((x^k + k) + \frac{1}{x^k + k} \right) - k \rightarrow D: [\frac{1}{k}, +\infty) \quad \text{5.8}$$

$$f) y = \frac{x^k + 0}{\sqrt{x^k + \varepsilon}} = \sqrt{x^k + \varepsilon} + \frac{1}{\sqrt{x^k + \varepsilon}} \rightarrow D: [\frac{0}{k}, +\infty)$$

sometimes
never

$$y = |x - \mu| + |\mu x + \varepsilon|$$

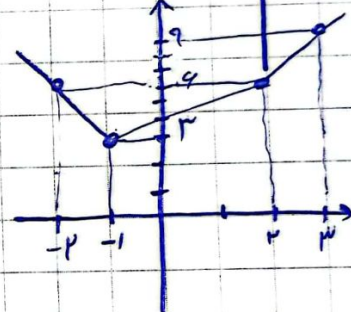
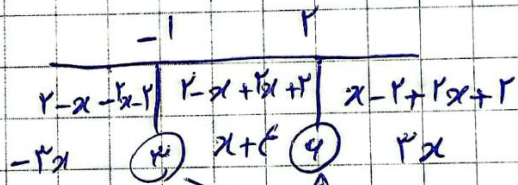
$\downarrow$ $\downarrow$
 $x = \mu$ $x = -\frac{\varepsilon}{\mu}$



b) $y = |x - r| + |\mu x + r|$

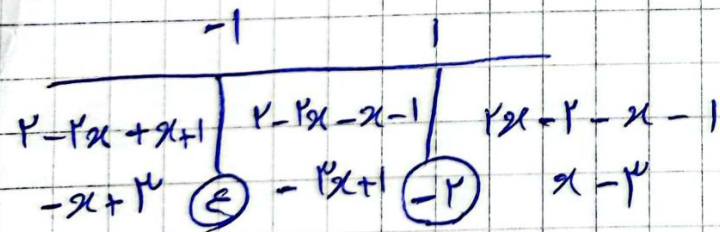
$\downarrow$ $\downarrow$
 $x = r$ $x = -1$

$R = [\mu, +\infty)$



c) $y = |r x - r| - |x + 1|$

$\downarrow$ $\downarrow$
 $x = 1$ $x = -1$



$R = [-r, +\infty)$

