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الف) $R_f = \mathbb{R}$ ——— محدوده‌ای مرتبه نبرد

ب) $y(n-1)^2 - 1 = 1 \Rightarrow y(n-1)^2 - y = 1 \Rightarrow (n-1)^2 - 1 = \frac{1}{y}$
 $(n-1)^2 = \frac{1}{y} + y \Rightarrow n-1 = \sqrt{\frac{1}{y} + y} \Rightarrow n = \sqrt{\frac{1}{y} + y} + 1$ $R_f = \mathbb{R} - (-1, 0]$

الف) $y = x^2 - 6x + 10 \quad a > 0 \Rightarrow \begin{cases} x_{min} = -\frac{b}{2a} = \frac{3}{1} = 3 \\ y_{min} = 4 \end{cases} \rightarrow R_f = [4, +\infty)$

ب) $y = -x^2 + 6x + 3 \quad a < 0 \Rightarrow \begin{cases} x_{min} = -\frac{b}{2a} = \frac{-6}{-2} = 3 \\ y_{min} = 12 \end{cases} \rightarrow R_f = (-\infty, 12]$

ج) $y = \sqrt{x^2 - 6x + 10} \quad a > 0 \Rightarrow \begin{cases} x_{min} = -\frac{b}{2a} = \frac{3}{1} = 3 \\ y_{min} = 4 \end{cases} \rightarrow R_f = [4, +\infty)$

د) $y = \sqrt{x - x^2} \quad a < 0 \Rightarrow \begin{cases} x_{min} = -\frac{b}{2a} = \frac{-1}{-2} = \frac{1}{2} \\ y_{min} = 0 \end{cases} \rightarrow R_f = [0, \frac{1}{2}]$

الف) $R_f = \mathbb{R}$ ——— محدوده‌ای مرتبه نبرد

ب) $R_f = \mathbb{R}$ ———

ج) $y = \sqrt{x^2 - 6x + 10} \rightarrow \mathbb{R} \rightarrow R_f = [0, +\infty)$

د) $R_f = [0, +\infty)$ ——— زیرا $|a| \leq 1$

الف) $R_f = \mathbb{R} - \left\{\frac{2}{1}\right\}$ ——— هر دو همواره اند و در آنجا
 $R_f = \mathbb{R} - \left\{\frac{9}{c}\right\}$

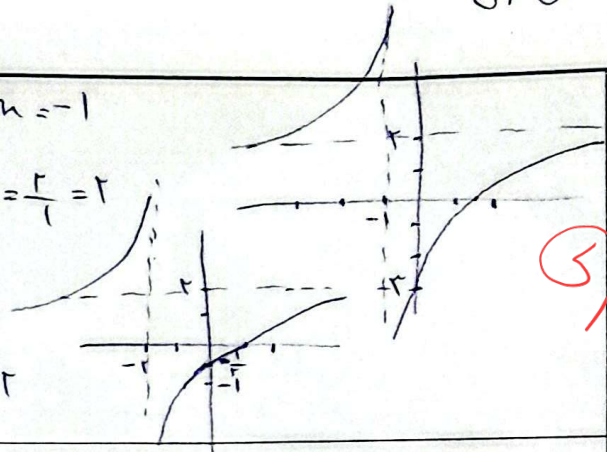
ب) $R_f = \mathbb{R} - \left\{\frac{2}{1}\right\}$

الف) $y = \sqrt{\frac{x+1}{x+1}} \rightarrow \mathbb{R} - \{1\} \rightarrow R_f = [0, +\infty) - \{1\}$

ب) $y = \sqrt{\frac{x+1}{x-1}} \rightarrow \sqrt{\frac{x+1}{x+1}} \rightarrow \mathbb{R} - \{-1\} \rightarrow R_f = [0, +\infty)$

الف) $n = -1$ → شذوذج → جانباً
 → افق → $y = \frac{a}{c} = \frac{r}{1} = r$

ب) $n = -2$ → جانباً
 → افق → $y = \frac{a}{c} = r$



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الف) $y = \sin x + \frac{1}{\sin x}$ $-1 \leq \sin x \leq 1$ $R_f = (-\infty, -r] \cup [r, +\infty)$

ب) $y = \frac{x^2+1}{x^2} \Rightarrow x^2 + \frac{1}{x^2}$ $R_f = (-\infty, -r] \cup [r, +\infty)$

ج) $\frac{\sqrt{x}+1}{\sqrt{x}} = \sqrt{\frac{x+r}{x}} + \frac{1}{\sqrt{x}}$ $R_f = (-\infty, -r] \cup [r, +\infty)$

د) $y = \sqrt{x} + \frac{1}{\sqrt{x}}$ $a > 0$ $R_f = [r, +\infty)$

الف) $x^2 + \frac{1}{x^2+r}$ $x^2+r + \frac{1}{x^2+r}$ $x^2+r = a \Rightarrow a + \frac{1}{a}$

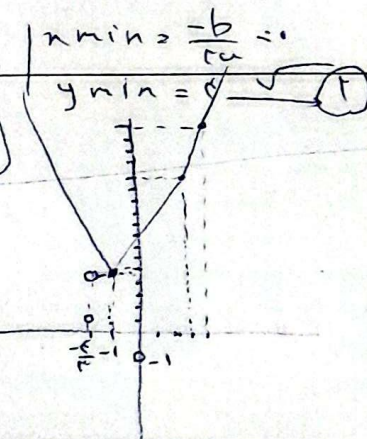
$a + \frac{1}{a} - r \geq -1$ $a + \frac{1}{a} \geq r$ $x^2+r + \frac{1}{x^2+r} - r$
 $x^2=0 \Rightarrow R_f = [\frac{1}{r}, +\infty)$

ب) $\frac{x^2+r+1}{\sqrt{x^2+r}} = \sqrt{x^2+r} + \frac{1}{\sqrt{x^2+r}}$

$\min_{x \in \mathbb{R}} = r + \frac{1}{r} = \frac{0}{r}$ $R_f = [\frac{0}{r}, +\infty)$

$y = |x-r| + |x+r|$
 $\begin{cases} x+1 & x > r \\ r+1 & -\frac{r}{r} \leq x \leq r \\ -x-1 & x < -\frac{r}{r} \end{cases}$
 $\begin{cases} n=r & y=r \\ n=r & y=r \\ n=r & y=r \\ n=-\frac{r}{r} & y=\frac{r}{r} \\ n=-\frac{r}{r} & y=\frac{r}{r} \\ n=0 & y=-1 \end{cases}$

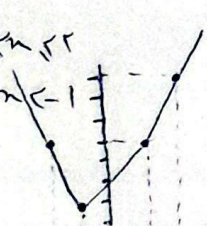
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الف) $y = |n-r| + |n+r|$

$\begin{cases} n-r+r+r=r & n > r \\ -n+r+r+r=r & -\frac{r}{r} \leq n \leq r \\ -n+r-r-r=-r & n < -1 \end{cases}$

$R_f = [r, +\infty)$



ب) $y = |r-n-r| - |n+1|$

$\begin{cases} r-n-r-n-1=n-r & n > 1 \\ -r-n-r-n-1=-r-n-1 & -1 \leq n \leq 1 \\ -r-n-r+n+1=-n-r & n < -1 \end{cases}$

$R = [-r, +\infty)$

