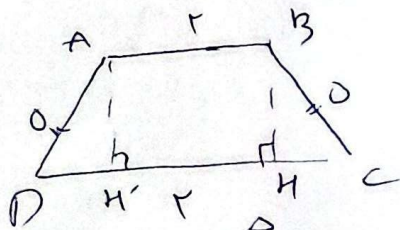


$$\left. \begin{aligned} \frac{1}{\sqrt{\cos^2 \alpha}} \\ \frac{1}{\cot \alpha} = \frac{\sin \alpha}{\cos \alpha} \end{aligned} \right\} \begin{aligned} \frac{1}{|\cos \alpha|} - \frac{\sin \alpha}{\cos \alpha} \begin{cases} \cos \alpha > 0 \\ \frac{1 - \sin \alpha}{\cos \alpha} = \frac{1 - \sin \alpha}{\cos \alpha} \\ \cos \alpha < 0 \\ \frac{-1 - \sin \alpha}{\cos \alpha} = \frac{\sin \alpha - 1}{\cos \alpha} \end{cases} \\ \cot \alpha = \frac{\cos \alpha}{\sin \alpha} = \frac{\cos \alpha}{\sqrt{\sin^2 \alpha}} = \frac{\cos \alpha}{|\sin \alpha|} \Rightarrow \sin \alpha = |\sin \alpha| \Rightarrow \sin \alpha > 0 \end{aligned}$$

$$\begin{aligned} -\frac{\pi}{2} < \alpha < \frac{\pi}{2} &\Rightarrow -\frac{1}{2} < \sin \alpha \leq 1 \Rightarrow -\frac{1}{2} < \frac{m-1}{2} \leq 1 \\ &\Rightarrow -2 < m-1 \leq 2 \Rightarrow -1 < m \leq 3 \Rightarrow m \in (-1, 3] \end{aligned}$$

$$\frac{\sin u}{\cos u} + \frac{\cos u}{\sin u} = -5 \Rightarrow \sin u \cdot \cos u = -\frac{1}{5}$$

$$\begin{aligned} \Rightarrow 5 \sin u \cos u = -1 \Rightarrow (\sin u + \cos u)^2 &= 1 + 2 \sin u \cos u = \frac{1}{5} \\ \frac{\pi}{2} < u < \pi \Rightarrow \sin u + \cos u &= \frac{-1}{\sqrt{5}} \\ \frac{1}{\sin u + \cos u} &= \frac{1}{(\sin u + \cos u)(1 - \sin u \cos u)} = \frac{\sqrt{5}}{\frac{4}{5}} = \frac{5\sqrt{5}}{4} \end{aligned}$$



$$\begin{aligned} \Delta BCH: \cos \theta &= \frac{CH}{BC} = \frac{CH}{l} = \frac{r}{l} \Rightarrow CH = r \\ \Delta BCH \cong \Delta ADH &\Rightarrow DH = CH = r \end{aligned}$$

$$\begin{aligned} ABMH' \rightarrow \text{مستطیل} \rightarrow HH' = 2 \rightarrow CD = r + r = 2r \\ \Delta BCH: BH^2 = BC^2 - CH^2 = l^2 - r^2 = 2l^2 \Rightarrow BH = l\sqrt{2} \\ s = (r + r) \times l = 2rl \end{aligned}$$

$$\tan 170^\circ = \tan(170^\circ + 10^\circ) = -\cot 10^\circ$$

$$\tan(-170^\circ) = \tan(-170^\circ + 10^\circ) = \tan 10^\circ$$

$$\sin 190^\circ = \sin(180^\circ + 10^\circ) = -\sin 10^\circ$$

$$\cos 170^\circ = \cos(180^\circ - 10^\circ) = -\cos 10^\circ$$

$$\tan 170^\circ \tan(-170^\circ) - \sin 190^\circ \cos 170^\circ$$

$$= (-\cot 10^\circ)(\tan 10^\circ) - (-\sin 10^\circ)(-\cos 10^\circ)$$

$$= -1 + \sin^2 10^\circ = -\cos^2 10^\circ \Rightarrow K = -1$$

$\Delta = 100 \Rightarrow r \tan \frac{u}{r} + \Lambda \tan \frac{v}{r} - r = 0$ (A) \rightarrow $\tan \frac{u}{r} = \frac{-\Lambda + 100}{r} = \frac{1}{r}$
 $\tan \frac{u}{r} = \frac{-\Lambda - 100}{r} = -\frac{1}{r}$ (عازي فضل الـ)

$A = \sqrt{r} \cos(15^\circ) \sin(15^\circ) - \sqrt{r} \sin(15^\circ) \cos(15^\circ)$

$A = \sqrt{r} \cos(110^\circ + 15^\circ) \sin(15^\circ) - \sqrt{r} \sin(110^\circ + 15^\circ) \cos(15^\circ)$

$A = \sqrt{r} \left(-\frac{\sqrt{r}}{r} \right) (-\cos 15^\circ) - \sqrt{r} \left(\frac{\sqrt{r}}{r} \right) (-\cos 15^\circ)$

$A = \frac{r}{r} (\cos 15^\circ + \cos 15^\circ) = \frac{2}{r} \cos 15^\circ = \frac{2}{r} \cos 15^\circ$

$f\left(\frac{\pi}{12}\right) = 16 \cos^2\left(\frac{\pi}{12}\right) \cos^2\left(\frac{\pi}{12}\right) \cos^2\left(\frac{\pi}{12}\right) \cos^2\left(\frac{\pi}{12}\right)$
 $= 16 \cos^4\left(\frac{\pi}{12}\right) \cos^4\left(\frac{\pi}{12}\right) \cos^4\left(\frac{\pi}{12}\right) \cos^4\left(\frac{\pi}{12}\right)$

$\cos^2 \alpha = \frac{1 + \cos 2\alpha}{2} \quad \cos^2\left(\frac{\pi}{12}\right) = \frac{1 + \cos\left(\frac{\pi}{6}\right)}{2} = \frac{1 + \frac{\sqrt{3}}{2}}{2} = \frac{2 + \sqrt{3}}{4}$

$16 \left(\frac{2 + \sqrt{3}}{4}\right)^4 \left(\frac{2 + \sqrt{3}}{4}\right)^4 \left(\frac{2 + \sqrt{3}}{4}\right)^4 \left(\frac{2 + \sqrt{3}}{4}\right)^4$
 $= 16 \left(\frac{2 + \sqrt{3}}{4}\right)^{16} = \frac{16(2 + \sqrt{3})^{16}}{4^{16}} = \frac{16(2 + \sqrt{3})^{16}}{2^{64}} = \frac{(2 + \sqrt{3})^{16}}{2^{63}}$

$\frac{1 - \sin u}{1 + \sin u} = r \Rightarrow 1 - \sin u = r + r \sin u \Rightarrow \delta \sin u = -r$
 $\Rightarrow \sin u = \frac{-r}{\delta}$

$\sin^2 u + \cos^2 u = 1 \Rightarrow \cos^2 u = 1 - \sin^2 u = 1 - \frac{r^2}{\delta^2} = \frac{\delta^2 - r^2}{\delta^2}$

$\cos u = \frac{-r}{\delta} \quad \tan u = \frac{-\frac{r}{\delta}}{\frac{\sqrt{\delta^2 - r^2}}{\delta}} = \frac{-r}{\sqrt{\delta^2 - r^2}} \quad \tan u = \frac{r \tan \frac{u}{r}}{1 - \tan^2 \frac{u}{r}}$

$\frac{r \tan \frac{u}{r}}{1 - \tan^2 \frac{u}{r}} = \frac{-r}{\sqrt{\delta^2 - r^2}} \Rightarrow r - r \tan^2 \frac{u}{r} = \Lambda \tan \frac{u}{r}$ (Ullur)

$\frac{\sin \theta}{1 - \cos \theta} + \frac{1 + \cos \theta}{\sin \theta} = k \cot \frac{\theta}{r}$

① $\frac{\sin \theta}{1 + \cos \theta} = \tan \frac{\theta}{r} \xrightarrow{\text{عكس}}$ $\frac{1 + \cos \theta}{\sin \theta} = \cot \frac{\theta}{r}$
 ② $\frac{1 - \cos \theta}{\sin \theta} = \tan \frac{\theta}{r} \xrightarrow{\text{عكس}}$ $\frac{\sin \theta}{1 - \cos \theta} = \cot \frac{\theta}{r}$
 $\left. \begin{matrix} \text{①} \cdot \text{②} \\ \hline \end{matrix} \right\} = r \cot \frac{\theta}{r}$
 $\boxed{k = r}$

$\cos\left(\frac{11\pi}{8} + \alpha\right) \quad \cos^2 \alpha + \sin^2 \alpha = 1 \quad \cos \alpha = \sqrt{1 - \sin^2 \alpha} = \sqrt{\frac{9}{16} - \frac{1}{16}} = \frac{\sqrt{8}}{4} = \frac{\sqrt{2}}{2}$

$\cos\left(2\pi + \frac{\pi}{8} + \alpha\right) = \cos\left(\frac{\pi}{8} + \alpha\right) = \cos \alpha \cos \frac{\pi}{8} - \sin \alpha \sin \frac{\pi}{8}$
 $\Rightarrow \left(\frac{\sqrt{2}}{2} \times \frac{\sqrt{2}}{2}\right) - \left(\frac{1}{2} \times \frac{\sqrt{2}}{2}\right) = \frac{2}{4} - \frac{\sqrt{2}}{4} = \frac{2 - \sqrt{2}}{4} = \frac{2 - \sqrt{2}}{4}$