

تایم: ۱۵ دقیقه؟

$$2x^2 + y^2 - \varepsilon x + 4y + k = 0$$

تبدیل به دایره

$$2x^2 - \varepsilon x + y^2 + 4y + k = 0 \xrightarrow{\text{تبدیل به دایره}} (\sqrt{2}x - \frac{\varepsilon}{\sqrt{2}})^2 + (y + 2)^2 = 0 \xrightarrow{\substack{z = \sqrt{2}x \\ t = y+2}} z^2 + t^2 = 0$$

پس $z = 0$ و $t = 0$

$$(\sqrt{2}x - \frac{\varepsilon}{\sqrt{2}})^2 + (y + 2)^2 = 0 \Rightarrow 2x^2 - \varepsilon x + y^2 + 4y + k = 0$$

پس $k = 4$

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$f(n) = \begin{cases} n^2 + \varepsilon n; n \geq a \\ 2n + a + 1; n \leq a \end{cases}$

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$f(n) \xrightarrow{a=1} \begin{cases} n^2 + \varepsilon n; n \geq 1 \\ 2n + 3; n \leq 1 \end{cases} \xrightarrow{n=1} 1 + \varepsilon = 0$

پس $\varepsilon = -1$

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$f(n) = \begin{cases} n^2 - b; |n+1| \geq 2 \\ a + 2n; -3 \leq n \leq -1 \end{cases}$

پس $a + b = 12$

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پس $\frac{b}{a} = \frac{1}{12}$

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پس $D_f = [-1, 3) \cup (3, 4]$

$$a) y = \sqrt{\frac{x^2 - x - 4}{x^2 - 12x^2 + 44}} \Rightarrow \sqrt{\frac{(x-3)(x+1)}{(x^2-9)(x^2-4)}} = \sqrt{\frac{(x-3)(x+1)}{(x-3)(x+3)(x-2)(x+2)}} \rightarrow \frac{-3 \quad -1 \quad 1 \quad 3}{+ \quad - \quad - \quad +}$$

$$D_f: (-\infty, -3) \cup (-1, 3) \cup (3, +\infty)$$

$$b) y = \sqrt{\frac{x^2 - 2x^2 - 4x + 4}{x^2 + 2x^2 - 4x - 4}} = \sqrt{\frac{(x-1)(x^2 - x - 4)}{(x+1)(x^2 + x - 4)}} = \sqrt{\frac{(x-1)(x-2)(x+2)}{(x+1)(x+2)(x-2)}} \rightarrow \frac{-3 \quad -1 \quad 1 \quad 3}{+ \quad - \quad - \quad +}$$

$$D_f: (-\infty, -3) \cup (-2, -1) \cup (1, 2) \cup (2, +\infty)$$

$$a) y = \sqrt{[-x] - 2} \quad [-x] - 2 \geq 0 \rightarrow [-x] \geq 2 \rightarrow [x] \geq -2 \rightarrow x \geq -2$$

$$D_f: (-\infty, -2]$$

$$b) y = \frac{x^2 + 4}{[x]^2 - 2[x] - 3} \rightarrow [x]^2 - 2[x] - 3 \neq 0 \quad [x] = t \quad t^2 - 2t - 3 = (t-3)(t+1) = 0$$

$$D_f: (-\infty, -1) \cup (0, 3) \cup (3, +\infty) \quad [x] \neq 3 \rightarrow x \notin [3, 4) \quad [x] \neq -1 \rightarrow x \notin [-1, 0)$$

$$a) y = \frac{\cos n + 1}{\tan n + 1} \rightarrow \frac{\cos n}{\sin n} + 1 \rightarrow \frac{\sin n}{\cos n} + 1 \rightarrow \text{Unit Circle} \rightarrow D_f: \mathbb{R} - \left\{ \frac{k\pi}{2}, k\pi + \frac{\pi}{2} \right\}$$

$$b) y = \sqrt{1 - \varepsilon \sin^2 n} \rightarrow 1 - \varepsilon \sin^2 n \geq 0 \quad \varepsilon \sin^2 n \leq 1 \rightarrow \sin^2 n \leq \frac{1}{\varepsilon}$$

$$D_f = \left[k\pi - \frac{\pi}{\sqrt{\varepsilon}}, k\pi + \frac{\pi}{\sqrt{\varepsilon}} \right] \leftarrow \text{Unit Circle} \leftarrow -\frac{1}{\sqrt{\varepsilon}} \leq \sin n \leq \frac{1}{\sqrt{\varepsilon}}$$

$$a) y = \sqrt{1 - \log \frac{n-1}{\frac{1}{4}}} \rightarrow 1 - \log \frac{n-1}{\frac{1}{4}} \geq 0 \quad \log \frac{n-1}{\frac{1}{4}} \leq 1 \rightarrow n-1 \geq \frac{1}{4}$$

$$D_f: \left[\frac{5}{4}, +\infty \right) \leftarrow n \geq \frac{5}{4}$$

$$b) y = \sqrt{\frac{n^2 - n}{1 - \log \frac{n^2 - n}{\varepsilon}}} \rightarrow n(n-1) \geq 0 \rightarrow \frac{1}{1 - \log \frac{n^2 - n}{\varepsilon}} \geq 0 \rightarrow 1 - \log \frac{n^2 - n}{\varepsilon} \neq 0 \rightarrow 1 \neq \log \frac{n^2 - n}{\varepsilon} \rightarrow n^2 - n \neq \varepsilon \rightarrow (n-\varepsilon)(n+1) = 0$$

$$a) y = \sqrt{\varepsilon n - n^2} \rightarrow \varepsilon n - n^2 \geq 0 \rightarrow \varepsilon n \geq n^2 \rightarrow \varepsilon n - n^2 \geq 0 \rightarrow -n^2 + \varepsilon n \geq 0 \rightarrow -(n^2 - \varepsilon n + 4) \geq 0 \rightarrow -(n-3)(n-1) \geq 0 \rightarrow \frac{1}{-1+1} = -$$

$$D_f: [1, 3]$$

$$b) y = \left(\frac{r n + \omega}{r n + \varepsilon} \right)! \rightarrow \frac{r n + \omega}{r n + \varepsilon} \in \mathbb{W} \rightarrow r n \mathbb{W} + \varepsilon \mathbb{W} = r n + \omega \rightarrow r = \frac{\omega - \varepsilon \mathbb{W}}{r \mathbb{W} - r}$$

$$D_f: \left\{ \frac{\omega - \varepsilon k}{r k - r} \mid k \in \mathbb{W} \right\}$$