

$$y = (a-1)x^2 + x + 3$$

$$\frac{-b}{2a} = 2 \quad \frac{-1}{2(a-1)} = 2 \quad 1(a-1) = -1 \quad a = 0$$

$$y = -\frac{1}{2}x^2 + x + 3 \quad -\frac{1}{2}x^2 + x + 3 = 0 \quad -x^2 + 2x + 6 = 0 \quad -(x-4)(x+2) = 0 \quad \boxed{x = 4}$$

$$f(x) = mx^2 - 2x + m$$

$$m \in (I) \cap (II) = \left(-\frac{5}{4}, 0\right)$$

$$\begin{aligned} & \frac{x_1}{y} = \frac{x_2}{y} = \frac{x_3}{y} \quad \Delta > 0 \\ & m < 0 \quad (I) \quad \begin{aligned} & 2\omega - 4m^2 > 0 \\ & (\omega = 2m)(\omega = 2m) > 0 \\ & m = \pm \frac{\omega}{2} \end{aligned} \\ & \frac{-\frac{\omega}{2}}{-1} + \frac{\frac{\omega}{2}}{1} = \frac{\omega}{2} \quad (-\frac{\omega}{2}, \frac{\omega}{2}) \quad (II) \end{aligned}$$

$$S = \frac{3-\sqrt{5}}{3} + \frac{3+\sqrt{5}}{3} = \frac{6}{3} = 2$$

$$P = \frac{3-\sqrt{5}}{3} \times \frac{3+\sqrt{5}}{3} = \frac{4}{9}$$

$$x^2 - 5x + p = 0$$

$$x^2 - 5x + \frac{4}{9} = 0 \quad \xrightarrow{\times 9} \quad 9x^2 - 45x + 4 = 0 \quad \text{ضرب در ۹}$$

$$x^2 - 12x + m + 12 = 0 \quad 12a^2 = 12a - m - 12$$

$$12a^2 + 12 = 12$$

$$S = a + b = \frac{1}{2} = 1 \quad P = \frac{m+12}{12}$$

$$12a^2 + 12a + 12 = 12$$

$$12a - m - 12 + 12 - m - 12 = 12$$

$$12a = 12m \quad a = \frac{m}{12}$$

$$b = \frac{m+12}{12} = \frac{m+12}{12}$$

$$S = \frac{m}{12} + \frac{m+12}{12} = \frac{m+12+m}{12} = 1 \quad m^2 - 12m + 12 = 0 \quad (m-6)^2 = 0 \quad m = 6$$

$$y = a(x-1)^2 + 4 \quad \xrightarrow{\Delta} \quad \omega = 4a + 4 \quad a = -1$$

$$y = -x^2 + 4x + 4 \quad \rightarrow \quad -x^2 + 4x + 4 > 0$$

$$-(x-4)(x+1) > 0$$

$$\frac{x-4}{x+1} > 0 \quad \Rightarrow \quad (-1, 4)$$

$$\alpha x^r - vx + q\beta = 0 \quad S: \alpha + \beta = \frac{v}{\alpha} \rightarrow \beta = -\frac{\alpha^r + v}{\alpha}$$

$$\begin{cases} \alpha\beta^r - v\beta + q\beta = \alpha\beta^r + \beta = \beta(\alpha\beta + 1) = 0 \\ \alpha\beta = -1 \end{cases}$$

$$\frac{-\alpha^r + v}{\alpha} \times \alpha = -\alpha^r + v = -1 \quad \alpha^r = q \quad \alpha = \pm \frac{q}{\sqrt{q}}$$

$$\beta = \frac{-1}{\alpha} = \frac{1}{\alpha} \quad \frac{1}{\alpha} + \frac{1}{\beta} = \frac{1}{\alpha} + \frac{1}{\alpha} = \frac{-1+q}{\alpha} = \frac{v}{\alpha}$$

$$x^r + mx - vm = 0 \quad -m\beta = \beta^r - vm$$

$$\alpha^r - m\beta = 1 \quad S = -m$$

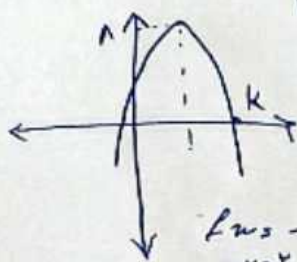
$$\alpha^r + \beta^r - vm = 1 \quad \beta = -vm$$

$$m^r + vm - vm = 1$$

$$m^r + vm = m(m+v) = 1 \quad \begin{cases} m = 0 \quad x \\ m = -1 \end{cases}$$

$$S = -m = 1$$

$$f(x) = mx^r + f_1x + \frac{m}{r} + v$$



$$\frac{-b}{2a} = \frac{-f_1}{2m} = \frac{-1}{2m}$$

$$m\left(\frac{1}{m+r}\right) + f_1\left(\frac{-1}{m}\right) + \frac{m}{r} + v = \frac{-1+m+r}{rm} = 1$$

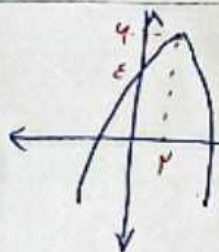
$$m^r - rm - 1 = 0$$

$$(m-1)(m+r) = 0$$

$$m = 1 \quad m = -r$$

$$f(x) = -rx^r + f_1x + 4 \quad x = -1$$

$$-rx^r + f_1x + 4 = 0 \rightarrow x = 4$$



$$y = a(x-4)^r + 4 \quad y = -\frac{1}{r}x^r + rx + k$$

$$k = fa + 4$$

$$a = -\frac{1}{r}$$

$$(-r)x - \frac{1}{r}x^r + rx + k = 0$$

$$x^r - rx - 1 = 0 \quad (r + \sqrt{r}, r - \sqrt{r})$$

$$\Delta: 1^2 + 4r = r^2$$

$$\frac{1}{r + \sqrt{r}} + \frac{1}{r - \sqrt{r}} = \frac{r - \sqrt{r} + r + \sqrt{r}}{r^2 - r} = \frac{2r}{r(r-1)} = \frac{2}{r-1}$$

$$x^r - (fa+r)x + (ra^r + 4a + v) = 0$$

$$r - 1a - 1 + ra^r + 4a + v = 0$$

$$ra^r - 1a - 1 = 0 \quad a = \frac{1}{r} \rightarrow x = \frac{1}{r}$$

$$x^r - 1x + 1 = (x-1)(x-4) = 0 \quad x = 4$$