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$$\text{الف) } y = \frac{x+r}{rx^r + r^2x^r - \Lambda x + r} \Rightarrow rx^r + r^2x^r - \Lambda x + r \rightarrow (x-1)(x+r)(rx-1)$$

$\hookrightarrow x=1 \quad \hookrightarrow x=-r \quad \hookrightarrow x=\frac{1}{r}$

$$D = \mathbb{R} - \left\{-r, 1, \frac{1}{r}\right\}$$

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$$\text{ب) } y = \frac{x+r}{rx^r + 9x^r + 10x + r} \Rightarrow rx^r + 9x^r + 10x + r \rightarrow (x+1)(x+r)(2x+1)$$

$\hookrightarrow x=-1 \quad \hookrightarrow x=-r \quad \hookrightarrow x=-\frac{1}{2}$

$$D = \mathbb{R} - \left\{-r, -1, -\frac{1}{2}\right\}$$

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$$\text{الف) } y = \frac{x+r}{x^r - rx^r + rx - 1} \rightarrow x^r - rx^r + rx - 1 = (x-1)(x^r - x + 1)$$

$\hookrightarrow \text{مميز صفر}$

$$D = \mathbb{R} - \{1\}$$

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$$\text{ب) } y = \sqrt{\frac{x+r}{x^r - rx^r + rx - 1}} \rightarrow \sqrt{\frac{x+r}{(x-1)(x^r - x + 1)}}$$

$\hookrightarrow \text{مميز صفر}$

$\frac{x+r}{x-1} \geq 0$ if $x \neq 1$

$$D = (-\infty, -r] \cup (1, +\infty)$$

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$$y = \frac{r}{x^r - \delta|x-1| - rx + \delta} \rightarrow x^r - \delta|x-1| - rx + \delta = \underbrace{(x-1)^r}_T - \delta|x-1| + \delta$$

$$T^r - \delta T + \delta = 0 \rightarrow (T-1)(T-\delta) = 0$$

$|x-1|=1 \rightarrow x \neq 0 \leq r$
 $|x-1|=\delta \rightarrow x-r \leq \delta$

$$D = \mathbb{R} - \{-r, 0, r, \delta\}$$

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$$\text{الف) } \frac{x+r}{|rx+1| - |x+r|} \rightarrow |rx+1| - |x+r| \neq 0$$

$$|rx+1| = |x+r| \quad \hookrightarrow \quad |rx+1| = |x+r| = 0 \rightarrow D = \mathbb{R} - \left\{-\frac{r}{r}, r\right\}$$

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$$\text{ب) } y = \sqrt{|rx+1| - |x+r|} \rightarrow D(x) \geq 0 \rightarrow x \in (-\infty, -\frac{r}{r}] \cup [r, \infty)$$

$$D = (-\infty, -\frac{r}{r}] \cup [r, \infty)$$

المميز صفر

الف) $y = \log_r (1 - \log_r^n)$ $\rightarrow 1 - \log_r^n > 0 \rightarrow \log_r^n < 1 \rightarrow n < r$ -د
 $\log_r^n \rightarrow n > 0$ $D = (0, r)$

ب) $y = \log_r (1 - \log_{\frac{1}{r}}^n)$ $\rightarrow 1 - \log_{\frac{1}{r}}^n > 0 \rightarrow \log_{\frac{1}{r}}^n < 1 \rightarrow n > \frac{1}{r}$
 $\log_{\frac{1}{r}}^n \rightarrow n > 0$ $D = (\frac{1}{r}, +\infty)$

$n = \sqrt{\log_{a,d} \log_a (rn-1)}$ $\rightarrow rn-1 > 0 \rightarrow n > \frac{1}{r}$ -4
 $\log_a^{rn-1} \geq 0 \rightarrow rn-1 \leq 1 \rightarrow n \leq \frac{2}{r}$
 $\hookrightarrow \infty \rightarrow n \leq r$
 $D = (1, r]$

الف) $y = \log(r \cos n + 1)$ $\rightarrow r \cos n + 1 > 0 \rightarrow \cos n > -\frac{1}{r}$ -✓
 $D = \mathbb{R} - \left\{ \frac{r\pi}{r} + 2k\pi, \frac{3r\pi}{r} + 2k\pi \right\}$

ب) $y = \sqrt{\log \frac{n-1}{n+1}}$ $\rightarrow n \neq -1, \log(0) \geq 0, \frac{n-1}{n+1} \geq 1$
 $\hookrightarrow n < -1$
 $D = (-\infty, -1)$

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المعبر بالشرط

$f(x) = \sqrt{(a+r)x^2 + ax + b} \leftrightarrow (-\infty, r]$
 $\hookrightarrow x^2 \text{ غير } = 0 \rightarrow a = -r \rightarrow \text{معبر بالشرط}$
 $-rx + b \geq 0 \rightarrow x \leq \frac{b}{r} \rightarrow \frac{b}{r} = r \rightarrow b = r^2$

$f(x) = \sqrt{x^2 + rx + r - m^2} \leftrightarrow D = \mathbb{R}$ -9
 $\underbrace{x^2 + rx + r - m^2}_u \geq 0$
 $\min((n+1)^2 + 1 - m^2) = 1 - m^2 \geq 0 \rightarrow |m| \leq 1$
 $\begin{cases} \rightarrow \max m = 1 \\ \rightarrow \min m = -1 \end{cases} \left. \begin{matrix} 1 - (-1) = 2 \end{matrix} \right\} \textcircled{2}$

$$f(n) = \frac{\sqrt{4-n^2}}{[n] + [-n] + 1} \rightarrow 4-n^2 \geq 0 \Rightarrow |n| \leq 2$$

$$[n] + [-n] + 1 \rightarrow \text{صفر}$$

اعداد صحیح زوج = ۲ و ۰ و -۲
 و اعداد فرد = ۱ و -۱ و -۳

اصغر و بزرگ