

ABD : : $A(-3, k)$: $B(t, m) \rightarrow m = \frac{1}{t}$: $y - k = \frac{1}{t}(x + 3) \rightarrow y = \frac{1}{t}x + k - \frac{3}{t} \xrightarrow{(t, m)} -t + k = m$

$\Rightarrow S = (AB)^2 : (\sqrt{(t+3)^2 + (m-k)^2})^2 = t^2 + (m-k)^2 = \frac{45}{1}$
 $(-t+k-k)^2 = 0$

①

$A(-1, 2)$: $B(3, 1)$: $C(n, y)$: $D(-1-n, y+3)$

 $\rightarrow A + C = B + D : -1 + n = 3 - 1 - n \rightarrow n = \frac{3}{2}$, $m_{AB} = \frac{1-2}{3-(-1)} = -\frac{1}{4} \Rightarrow m_{DC} = \frac{1}{4}$
 $\Rightarrow \frac{1}{4} = \frac{y-1}{\frac{3}{2}-3} \rightarrow -4 = 3y-3 \rightarrow y = -1$, $P = 2(\sqrt{1^2 + 9} + \sqrt{\frac{9}{4} + \frac{1}{4}})$
 $\sqrt{\frac{10}{4}} = \frac{\sqrt{10}}{2}$

$\Rightarrow 2 \times \frac{10}{2} = 10$

②

$\tan 45^\circ = \sqrt{3} = m' : 2mx + (m^2 - 1)y = 3 \rightarrow y = \frac{3 - 2mx}{m^2 - 1}$

$\Rightarrow m' = \frac{-2m}{m^2 - 1} = \sqrt{3} \rightarrow -2m = \sqrt{3}m^2 - \sqrt{3} : \sqrt{3}m^2 + 2m - \sqrt{3} = 0 \rightarrow (m-1)(m+3) = 0$
 $\hookrightarrow m = 1, -3 \pm \sqrt{3}, m = \frac{1}{\sqrt{3}}, -\sqrt{3}$

$\Rightarrow m_1 - m_2 : \frac{1}{\sqrt{3}} + \sqrt{3} : \frac{1+3}{\sqrt{3}} = \frac{4}{\sqrt{3}}$

③

$A \rightarrow (1, 9)$: $B \rightarrow (3, 3)$: $C \rightarrow (4, 1)$

 $\Rightarrow y_{BC} : y - 3 = \frac{1-3}{4-3}(x-3) : y = 2x - 3 \rightarrow y - 2x + 3 = 0$

$\Rightarrow d_A \text{ to } y_{BC} : \frac{|1 - 2 \times 1 + 3|}{\sqrt{5}} = \frac{2}{\sqrt{5}}$

④

$B \rightarrow V - 2m = \frac{-19 + \sqrt{41}}{2} : 12 - 6m = -19 + \sqrt{41} \rightarrow 11m = 31$
 $\frac{31}{11}, y = 1$

$\Rightarrow d_B \text{ to } y_{AC} : \frac{|1 - 9 + 8 - 17|}{5} = \frac{17}{5} = 3.4$

⑤

$$\left(-\frac{r}{\sqrt{r}}, 0\right) \rightarrow m = \frac{0 - r}{\frac{-r}{\sqrt{r}}} = \frac{-r \times \sqrt{r}}{-r} = \sqrt{r} \quad ; \quad y = -\sqrt{r}(x + \frac{r}{\sqrt{r}}) \rightarrow y = -\sqrt{r}x - r$$

$$y = n \quad ; \quad -\sqrt{r}x - r = n \rightarrow \sqrt{r}x = -r - n \quad ; \quad x = \frac{-r - n}{\sqrt{r}} \Rightarrow \frac{r}{\sqrt{r}} = \sqrt{r} \quad \text{then } \sqrt{r} = \sqrt{r} \rightarrow \frac{r}{\sqrt{r}}$$

⑥

Diagram: A line segment from (0,0) to (1,1) with a point (a,1+n) on it.

$$y_1 = 1 + an \rightarrow m = m' : a = \frac{1}{a} \rightarrow a = \pm 1$$

Case 1: $a = -1 \rightarrow y = -x + 1 \rightarrow (1,2) \checkmark$
 Case 2: $a = 1 \rightarrow y = x + 1 \rightarrow (1,2) \checkmark$
 Case 3: $a = 1 \rightarrow y = x \rightarrow (1,1) \checkmark$

$$y_1 \in d_A : \frac{1 + 1 + 1}{\sqrt{r}} = \frac{\sqrt{r}}{r} \Rightarrow \frac{3}{\sqrt{r}} = \frac{\sqrt{r}}{r} \Rightarrow \sqrt{r} = \frac{3}{\sqrt{r}} \Rightarrow r = \frac{9}{r} \Rightarrow r = 3$$

⑦

$$S_{\Delta x r} = S_{\square}$$

$$\Rightarrow \frac{\frac{r}{\sqrt{r}} \times \frac{\sqrt{r}}{r}}{2} \times r = \frac{r}{r} = 1$$

$$\frac{r}{\sqrt{r}} \times \frac{\sqrt{r}}{r} = \frac{r}{r} = 1$$

$$x - r y = 1 \Rightarrow x - 1 = 1 \Rightarrow x = 2$$

$$AC = \frac{r}{\sqrt{r}} : \frac{r}{\sqrt{r}} = \frac{r}{\sqrt{r}} \Rightarrow r = \frac{r}{\sqrt{r}} \Rightarrow r = \frac{r}{\sqrt{r}} \Rightarrow r = \frac{r}{\sqrt{r}}$$

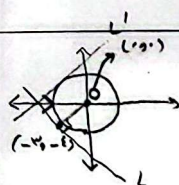
$$S = \frac{r}{\sqrt{r}} \times \frac{\sqrt{r}}{r} = \frac{r}{r} = 1$$

⑧

$$\left(-\frac{1}{r}, b\right), \left(-\frac{1}{r}, a\right) \Rightarrow m = \frac{b-a}{\frac{-1}{r} - \frac{-1}{r}} = \frac{r(b-a)}{0} \rightarrow b-a = \frac{\sqrt{r}}{r}$$

$$\Rightarrow d = \sqrt{\left(\frac{-1}{r} + \frac{1}{r}\right)^2 + (b-a)^2} = \frac{r}{r} = \frac{1}{r} = n \Rightarrow \sqrt{r} = \sqrt{r} \Rightarrow \frac{\sqrt{r}}{r}$$

⑨



$$m_L = \frac{r}{-r} \rightarrow m_{L'} = \frac{r}{r}$$

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