

$$x+1 \Rightarrow f(x) = f(x) \leq 3 + f(x) \Rightarrow f(x) \leq 3 \Rightarrow f(x) \leq 3$$

$$y = \sqrt{f(x) - x^2} = \sqrt{x - x^2} \Rightarrow \sqrt{-x^2 + x} \Rightarrow x \leq \frac{1}{4} \Rightarrow \frac{1}{4} \leq \frac{1}{4} \Rightarrow \frac{1}{4} \leq \frac{1}{4} \Rightarrow \frac{1}{4} \leq \frac{1}{4}$$

حاصل می شود

$$\Rightarrow R_y \leq [0, \frac{1}{4}]$$

$$\frac{x(x^2-1)}{x+1}, \frac{x(x-1)(x+1)}{x+1}, x(x-1) \Rightarrow x(x-1) \neq 1 \Rightarrow x \neq 1 \Rightarrow a \leq -1 \quad (1)$$

$$b \leq 1 \quad (2)$$

$$\Rightarrow x^2 - 1 \leq x \Rightarrow x \leq \frac{1}{4} \Rightarrow y_{min} \leq -1 \Rightarrow R_f \leq [-1, +\infty) \quad (3)$$

$$\Rightarrow (1), (2), (3) \Rightarrow f(\frac{1}{4}) = f(-1) \leq 3$$

$$\sqrt{x^3 + ax + b} - 1 \Rightarrow \sqrt{(x-1)^3} \leq x-1 \checkmark$$

در $x=1$ به خط می رسد

$$\Rightarrow (x-1)^3 \leq x-1 \Rightarrow x^3 - 3x^2 + 3x - 1 \leq x-1 \Rightarrow x^3 - 3x^2 + 2x \leq 0 \Rightarrow x(x-1)(x-2) \leq 0$$

$$R_f \leq [-1, 1]$$

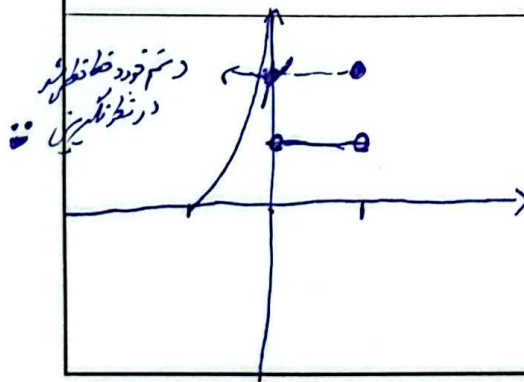
$$y = (\frac{x+1}{1-x})^{\frac{1}{2}} \Rightarrow y \geq 0 \Rightarrow \frac{x+1}{1-x} \geq 0 \Rightarrow D_f \leq [-1, 1)$$

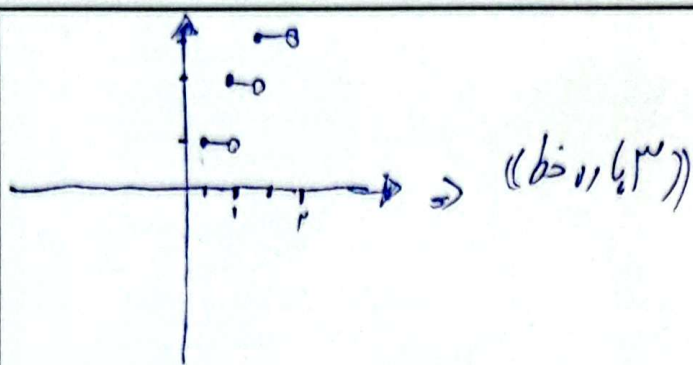
در $x=1$ به خط می رسد

$$y \leq \frac{ax-1}{x^2+b} \Rightarrow R \Rightarrow x \leq \sqrt{\frac{by-1}{y-a}} \Rightarrow D_{x \in [-1, 1)} \Rightarrow y \leq a \Rightarrow a \leq 1$$

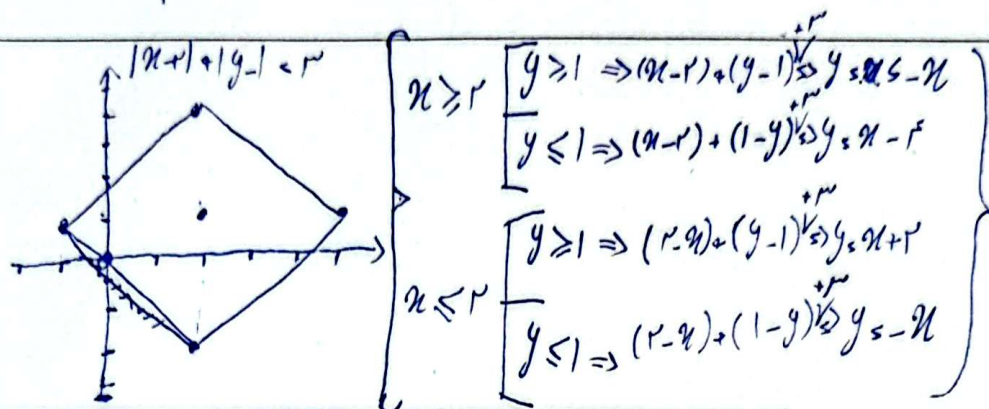
در $x=1$ به خط می رسد

$$\Rightarrow [-1] \Rightarrow b-1 \leq 0 \Rightarrow b \leq 1 \Rightarrow a+b \leq 2$$

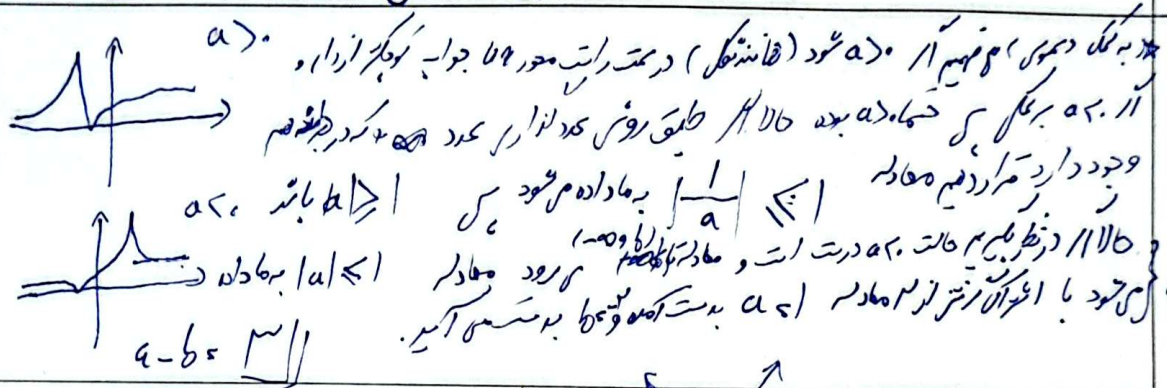




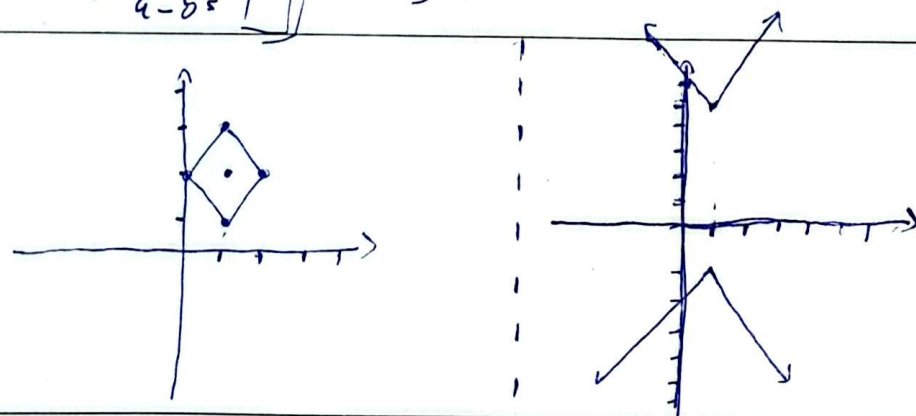
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