

الف) $\cos 2u = 2 \sin u - 1 \rightarrow 1 - 2 \sin u = 2 \sin u - 1 \rightarrow 2 \sin u + 2 \sin u - 2 = 0$
 $= (\sin u + \frac{1}{2})(\sin u - \frac{1}{2}) = 0$ $\begin{cases} \sin u = -\frac{1}{2} & \text{غیر قابل حل} \\ \sin u = \frac{1}{2} \end{cases} \rightarrow \begin{cases} u = 2k\pi + \frac{\pi}{6} \\ u = 2k\pi + \frac{5\pi}{6} \end{cases}$

ب) $\cos 2u + \cos u - 2 = 0 \rightarrow (\cos u + \frac{1}{2})(\cos u - \frac{3}{2}) = 0$ $\begin{cases} \cos u = -\frac{1}{2} & \text{غیر قابل حل} \\ \cos u = 1 \end{cases} \rightarrow \boxed{u = 2k\pi}$

الف) $\sin u - \cos u = \sin 2u \rightarrow (\sin u - \cos u)(\sin u + \cos u) = 2 \sin u \cos u$
 $\sin u - \cos u = 2 \times \sin u \times (\cos u \times (-1)) \rightarrow \sin u \times (\cos u - 2) = -\frac{1}{2} \rightarrow$
 $\frac{1}{2} \sin 2u = -\frac{1}{2} \rightarrow \sin 2u = -1 \rightarrow \boxed{u = k\pi + \frac{3\pi}{4}}$

ب) $2 \cos^2 u + 2 \sin u \cos u - 1 = 0 \rightarrow \cos 2u + \sin 2u = 0 \rightarrow \cos 2u = -\cos(\frac{\pi}{2} - 2u)$
 $2u = -2k\pi - \frac{\pi}{2} \rightarrow 2u = -2k\pi \rightarrow \boxed{u = -k\pi}$
 $2u = -2k\pi + \frac{\pi}{2} \rightarrow u = -k\pi + \frac{\pi}{4}$

الف) $\cot u (2 \cos u + 1) = \frac{1}{\sin u} \rightarrow \frac{\cos u}{\sin u} (2 \cos u + 1) = \frac{1}{\sin u} \rightarrow 2 \cos^2 u + \cos u - 1 = 0$
 $(\cos u + \frac{1}{2})(\cos u - 1) = 0 \rightarrow \begin{cases} \cos u = -\frac{1}{2} \rightarrow \sin u = 0 & \text{غیر قابل حل} \\ \cos u = 1 \end{cases} \rightarrow \boxed{u = 2k\pi + \frac{\pi}{3}}$

ب) $2 \sin^2 u - \sin u \cos u + \cos^2 u = 2 \rightarrow 2 - 2 \cos^2 u - \sin u \cos u + \cos^2 u - 2 = 0$
 $-\cos^2 u - \sin u \cos u = 0 \rightarrow -\cos u (1 + \sin u) = 0$ $\begin{cases} \cos u = 0 \rightarrow \boxed{u = k\pi + \frac{\pi}{2}} \\ \sin u = -1 \rightarrow \boxed{u = k\pi + \frac{3\pi}{2}} \end{cases}$

الف) $\cos(\frac{\pi}{2} + u) \cos(u - \frac{\pi}{2}) = \frac{1}{2} \rightarrow \cos(\frac{\pi}{2} + u) \sin(\frac{\pi}{2} - (u - \frac{\pi}{2})) = \frac{1}{2}$
 $\frac{1}{2} \sin(\frac{\pi}{2} + 2u) = \frac{1}{2} \rightarrow \cos(2u) = \frac{1}{2} \rightarrow 2u = 2k\pi \pm \frac{\pi}{3} \rightarrow \boxed{u = k\pi \pm \frac{\pi}{6}}$

ب) $\cos(2u - \frac{\pi}{4}) = -\sin 2u \rightarrow \sin(\frac{\pi}{2} - (2u - \frac{\pi}{4})) = -\sin 2u$
 $\sin(-2u + \frac{3\pi}{4}) = -\sin 2u \rightarrow \sin(2u - \frac{3\pi}{4}) = \sin 2u$ $\begin{cases} 2u - \frac{3\pi}{4} = 2k\pi + 2u \rightarrow \boxed{u = k\pi + \frac{3\pi}{4}} \\ 2u - \frac{3\pi}{4} = 2k\pi + \pi - 2u \rightarrow \boxed{u = k\pi + \frac{7\pi}{4}} \end{cases}$

$\frac{\sin 2u + \sin 4u}{\sin 2u} - \sin^2 u = \cos^2 u \rightarrow \frac{2 \sin 3u \cos u}{\sin 2u} = \cos^2 u - \sin^2 u$

$2 \cos 2u + 2 = \cos 2u \rightarrow \cos 2u = -2$ $2u = 2k\pi + \pi \rightarrow u = k\pi + \frac{\pi}{2}$
 $2u = 2k\pi - \pi \rightarrow u = k\pi - \frac{\pi}{2}$
 $\boxed{u = k\pi \pm \frac{\pi}{2}}$

$$|\pi - 0| = \boxed{\pi} \quad \text{جواب} \quad \pi \text{ و } 0 \leftarrow \left[-\pi, \pi \right]$$

$$\frac{\sin \frac{n}{r}}{1 + \cos \frac{n}{r}} = \frac{1}{\sin \frac{n}{r}} + \cot \frac{n}{r} \rightarrow \frac{\sin \frac{n}{r}}{1 + \cos \frac{n}{r}} = \frac{1 + \cos \frac{n}{r}}{\sin \frac{n}{r}} \rightarrow \sin \frac{n}{r} = (1 + \cos \frac{n}{r})^r$$

$$1 - \cos \frac{n}{r} = \cos^r \frac{n}{r} + 1 + r \cos \frac{n}{r} \rightarrow r \cos^r \frac{n}{r} + r \cos \frac{n}{r} = 0 \rightarrow r \cos \frac{n}{r} (\cos^r \frac{n}{r} + 1) = 0$$

$$\cos \frac{n}{r} = 0 \rightarrow \frac{n}{r} = r \left(k\pi + \frac{\pi}{r} \right) \rightarrow n = r \left(k\pi + \frac{\pi}{r} \right) \rightarrow |n| = r \left(k\pi + \frac{\pi}{r} \right)$$

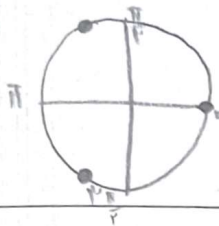
$$\cos \frac{n}{r} = -1 \rightarrow \frac{n}{r} = r \left(k\pi + \pi \right) \rightarrow n = r \left(k\pi + \pi \right) \rightarrow |n| = r \left(k\pi + \pi \right)$$

$$\cos^r n - \sin^r n \cos^r n = 1 \rightarrow \sqrt[r]{\sin^r n - \sin^r n \cos^r n} = 1$$

$$-\sin^r n (1 + \cos^r n) = 0$$

$$\sin^r n = 0 \rightarrow \sin n = 0 \rightarrow n = r \left(k\pi \right)$$

$$\cos^r n = -1 \rightarrow r n = r \left(k\pi + \pi \right) \rightarrow n = \frac{r}{r} \left(k\pi + \pi \right)$$



جواب

$$\boxed{\frac{r}{r} \left(k\pi + \pi \right)}$$

$$\frac{1 - \tan n}{1 + \tan n} = \tan^r n \rightarrow \frac{\tan \frac{\pi}{2} - \tan n}{1 + \tan \frac{\pi}{2} \tan n} = \tan \left(\frac{\pi}{2} - n \right) = \tan^r n$$

$$r n = k\pi + \frac{\pi}{2} - n$$

$$\boxed{n = \frac{k\pi}{2} + \frac{\pi}{2r}}$$

$$\sqrt{1 + \sin^r n} = r^r \cos^r n \rightarrow \sqrt{\sin^r n + \cos^r n + r \sin n \cos n} = \sqrt{(\sin^r n + \cos^r n)}$$

$$|\sin n + \cos n| = r^r (\cos^r n - \sin^r n) (\cos n + \sin n) \rightarrow \frac{r^r}{r} = \cos n - \sin n \leftarrow \sin + \cos > 0$$

$$\rightarrow \frac{r^r}{r} = \sin n - \cos n \leftarrow \sin + \cos < 0$$

$$\text{الف) } \sin^r n - \cos^r n = 1 \rightarrow (\sin^r n + \cos^r n) (\sin^r n - \cos^r n) = 1 \rightarrow \cos^r n - \sin^r n = -1$$

$$\cos^r n = -1 \rightarrow r n = r \left(k\pi + \pi \right) \rightarrow |n| = \frac{k\pi}{r} + \frac{\pi}{r} \quad \text{جواب} \quad \frac{\pi}{r} > \frac{r\pi}{r}$$

$$\sin^r n - \cos^r n = -1 \rightarrow (\sin^r n - \cos^r n) (\sin^r n + \sin^r n \cos^r n + \cos^r n) = -1 \quad (\sin n - \cos n) \left(1 + \frac{\sin^r n}{r} \right) = -1$$