

دار، دكم بيسر

تکلیف سماره ۲۳

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$$g(\alpha) = f(\tan \alpha + \sqrt{r} \cos \alpha) \Rightarrow g'(\alpha) = (r \tan \alpha \times \frac{1}{\cos^2 \alpha} - \sqrt{r} \sin \alpha) f'(\tan \alpha + \sqrt{r} \cos \alpha)$$

$$\Rightarrow g'(\frac{\pi}{4}) = (r \times r - 1) f'(r) = \sqrt{r} \Rightarrow f'(r) = \frac{\sqrt{r}}{r} \quad \checkmark$$

$$f(\alpha) = \frac{1 + \cos^3 \alpha}{r - \cos^2 \alpha} = \frac{(1 + \cos \alpha)(\cos^2 \alpha - r \cos \alpha + r)}{(r - \cos \alpha)(r + \cos \alpha)} = \frac{\cos^2 \alpha - r \cos \alpha + r}{r - \cos \alpha}$$

$$g(\alpha) = \frac{r}{r - \cos \alpha} \Rightarrow f(\alpha) = r g(\alpha) = \frac{r \cos^2 \alpha - r \cos \alpha + r}{r - \cos \alpha} = \frac{r}{r - \cos \alpha}$$

$$= \frac{\cos \alpha (\cos \alpha - r)}{r - \cos \alpha} = -\cos \alpha \Rightarrow (-\cos \alpha)' \sin \alpha \xrightarrow{\alpha = \frac{\sqrt{7}}{4}} \sin \frac{\sqrt{7}}{4} = \frac{1}{r}$$

$$f(\alpha) = |r \alpha - r \sqrt{\alpha}| \begin{cases} \alpha > \frac{r}{r} \rightarrow (r \alpha - r) \sqrt{\alpha} \rightarrow f'(\alpha) = r \sqrt{\alpha} \rightarrow r \sqrt{\frac{r}{r}} = r \quad \checkmark \\ \alpha < \frac{r}{r} \rightarrow (r - r \alpha) \sqrt{\alpha} \rightarrow f'(\alpha) = -r \sqrt{\alpha} \rightarrow -r \sqrt{\frac{r}{r}} = -r \quad \checkmark \end{cases}$$

$$r \sqrt{\frac{r}{r}} - (-r \sqrt{\frac{r}{r}}) = r \sqrt{4} = 2r \Rightarrow a = \frac{1}{r} \quad \checkmark$$

$$y = -\alpha x + r \Rightarrow y' = -\alpha \xrightarrow{\text{در } x=1} f'(1) = -\alpha, f(1) = -\alpha + r$$

$$\Rightarrow f(1) + f'(1) = -\alpha + r = -1 \Rightarrow \alpha = \frac{r}{\omega} \Rightarrow f'(1) = -\frac{r}{\omega} \quad \checkmark$$

$$\sqrt{y} - x = \omega \Rightarrow y = \frac{x + \omega}{\sqrt{y}} \Rightarrow \frac{x + \omega}{\sqrt{y}} = \frac{\omega x - 1}{\sqrt{y} - 1} \Rightarrow \sqrt{y} + 14\omega + \omega = \sqrt{y} - 1$$

$$\Rightarrow \sqrt{y} + (14\omega) \omega + 1 = 0 \Rightarrow \omega + \frac{14 - \sqrt{y}}{14 - \sqrt{y}} \omega \xrightarrow{\omega = \frac{14 - \sqrt{y}}{r}} \frac{14 - \sqrt{y}}{r} = -r$$

$$\Rightarrow 14 - \sqrt{y} = -r \Rightarrow \sqrt{y} = 14 + r \Rightarrow a = \frac{1}{r} \quad \checkmark$$

$$f(x), x^r \tan b \Rightarrow f'(x), r x^{r-1} \tan a, f'(x) = 0 \quad (4)$$

$$\Rightarrow r(x)^{r-1} \tan a = 0 \Rightarrow a = -\frac{\pi}{2}, f(x) = 0 \Rightarrow f(x), r(x)^{r-1} \tan(-\frac{\pi}{2}) = 0$$

$$\Rightarrow b = -\frac{\pi}{2} \Rightarrow b - a = -\frac{\pi}{2} - (-\frac{\pi}{2}) = 0 \quad (5)$$

$$f(x) = \sin^n(x) \Rightarrow f'(x) = r \sin^{r-1}(x) (\cos x)$$

$$\Rightarrow \lim_{x \rightarrow 0} \frac{f(x) f'(x)}{(1 - \cos x)^m} = \frac{(r \sin^{r-1}(x) \cos x) (\sin^{r-1}(x))}{(1 - \cos x)^m} \quad (6)$$

$$\frac{r \sin^{r-1}(x)}{r^m} = \frac{(r \times r^m) (\sin^{r-1}(x))}{r^m} \Rightarrow r^m \sin^{r-1}(x) \Rightarrow n = r$$

$$n \times r^m = r^{m+1} \Rightarrow n = r \Rightarrow m = r-1 \Rightarrow m = 2, n = 3 \Rightarrow r = 3$$

$$f(x) = \frac{\sqrt{x+1}}{\sqrt{x-1}} \Rightarrow f'(x) = \left(\frac{x+1}{x-1} \right)^{-\frac{1}{2}} \Rightarrow (f'(x)) = \frac{1}{2} \left(\frac{x+1}{x-1} \right)^{-\frac{3}{2}} \quad (7)$$

$$\Rightarrow (f'(x)) = \frac{1}{2} \left(\frac{x+1}{x-1} \right)^{-\frac{3}{2}} \Rightarrow -\frac{1}{2} \quad (8)$$

$$f(x) = \frac{f(0) - f(-1)}{0 - (-1)} = \frac{1 - 0}{1} = 1 \Rightarrow a = -\frac{1}{r} \Rightarrow$$

$$f(x) = (x+1)^r \left(-\frac{1}{r} (x+1) \right)$$

$$\Rightarrow f'(x) = r(x+1)^{r-1} \left(-\frac{1}{r} (x+1) \right) - \frac{1}{r} (x+1)^r \Rightarrow f'(1) = r \times \frac{1}{r} - \frac{1}{r} = \frac{r-1}{r} \quad (9)$$

$$f(x) = \sin x \cos x = \sin x (1 - \sin^2 x) = \sin x - \sin^3 x$$

$$g(x) = \sin^2 x - \cos^2 x = (\sin^2 x - \cos^2 x) (\sin^2 x + \cos^2 x) = \sin^2 x - \cos^2 x$$

$$= \sin^2 x - \cos^2 x$$

$$\frac{f(\frac{\pi}{2}) - f(\frac{\pi}{4})}{g(\frac{\pi}{2}) - g(\frac{\pi}{4})} = \frac{f(\frac{\pi}{2}) - f(\frac{\pi}{4})}{g(\frac{\pi}{2}) - g(\frac{\pi}{4})} = \frac{1 - 0}{1 - 0} = 1 \quad (10)$$