

$$\lim_{x \rightarrow \infty} \frac{x - a}{x^2 + bx + c} \Rightarrow \begin{aligned} & x \rightarrow \infty \quad x^2 + bx + c = 1 \quad \text{---} \\ & x \rightarrow \infty \quad x^2 + bx + c = 1 \quad \text{---} \end{aligned} \quad \begin{aligned} & \text{---} \\ & \text{---} \end{aligned}$$

$$x^2 + bx + c = (x - r)^2 \rightarrow x^2 - 2rx + r^2 \rightarrow a = -r, b = r \rightarrow \dots$$

$$\lim_{x \rightarrow \sqrt{c}} \frac{x}{x^2 + bx + c} = \infty \rightarrow x^2 + bx + c = 0 \quad \checkmark \quad \text{---}$$

$$\rightarrow (x - \sqrt{c})^2 = x^2 - 2\sqrt{c}x + c \Rightarrow a = -\sqrt{c}, b = \sqrt{c}$$

$$\left\{ \frac{b}{a} \right\} = \left\{ \frac{\sqrt{c}}{-\sqrt{c}} \right\} = -1$$

$$\lim_{x \rightarrow \left(\frac{1}{\sqrt{c}}\right)^+} \frac{\{x\} + a}{\left| \frac{1}{\sqrt{c}} + a \right| + a} = -\infty = \frac{-1 + a}{\left| \frac{1}{\sqrt{c}} + a \right| + a} = -\infty \rightarrow \dots$$

$$\left| \frac{1}{\sqrt{c}} + a \right| + a = 0 \rightarrow \frac{1}{\sqrt{c}} + a = -a \rightarrow a = -\frac{1}{2\sqrt{c}} \rightarrow \dots$$