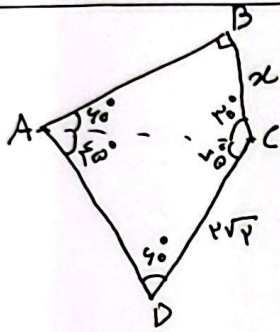


$$\frac{B+C+A}{180} = \frac{180}{180} \rightarrow A = 40^\circ$$

$$\frac{20}{\sin A} = \frac{20\sqrt{3}}{\sin B} \rightarrow \sin B = \frac{20\sqrt{3} \times \sqrt{3}}{20 \times 2} = \frac{3\sqrt{3}}{2} = \frac{\sqrt{3}}{2} \rightarrow \hat{B} = 70^\circ$$

$$C+B=120 \rightarrow C+70=120 \rightarrow C=50^\circ$$



$$\hat{A} + \hat{B} + \hat{C} + \hat{D} = 360^\circ \rightarrow \hat{A} + 90 + 40 + 100 = 360 \rightarrow \hat{A} = 100^\circ$$

$$\frac{2\sqrt{3}}{\sin 100^\circ} = \frac{AC}{\sin 40^\circ} \rightarrow \frac{2\sqrt{3}}{\frac{\sqrt{3}}{2}} = \frac{AC}{\frac{\sqrt{3}}{2}} \rightarrow AC = 2\sqrt{3}$$

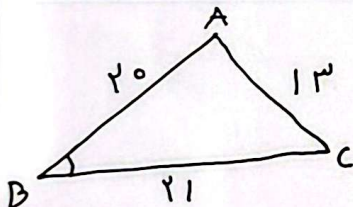
$$\sin 40^\circ = \frac{x}{AC} = \frac{\sqrt{3}}{2} \rightarrow \frac{x}{2\sqrt{3}} = \frac{\sqrt{3}}{2} \rightarrow x = 3$$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} = k \rightarrow b = k \sin B, c = k \sin C$$

$$\frac{(b^2 - 2) \sin C}{\sin B} = c \rightarrow \frac{cb^2 - 2}{\sin B} = k \sin C \rightarrow b^2 - 2 = k \sin B = b$$

$$\rightarrow b^2 - b - 2 = 0 \rightarrow \begin{cases} b = 2 \\ b = -1 \end{cases}$$

داده ضلع نمی تواند منفی باشد

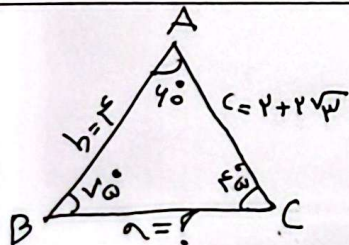


$$AC^2 = BC^2 + BA^2 - 2BA \cdot BC \cos B$$

$$10^2 = 20^2 + 20^2 - 2 \times 20 \times 20 \cos B$$

$$100 = 400 + 400 - 800 \cos B \rightarrow 800 \cos B = 700 \rightarrow \cos B = 7/8$$

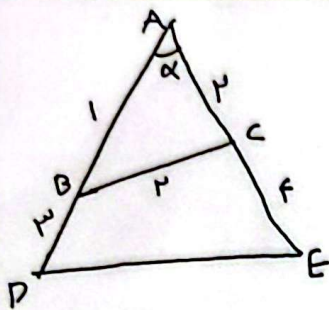
$$\cos^2 B + \sin^2 B = 1 \rightarrow \frac{49}{64} + \sin^2 B = 1 \rightarrow \sin^2 B = \frac{15}{64} \rightarrow \sin B = \frac{\sqrt{15}}{8}$$



$$a = \sqrt{AB^2 + AC^2 - 2AB \cdot AC \cos 40^\circ} = \sqrt{14^2 + 14^2 + 14\sqrt{3}} = \sqrt{28 + 14\sqrt{3}} = 2\sqrt{7}$$

$$\frac{2\sqrt{7}}{\sin 40^\circ} = \frac{f}{\sin C} \rightarrow \frac{2\sqrt{7}}{2} = \sin C \rightarrow \sin C = \frac{\sqrt{7}}{2} \rightarrow \hat{C} = 70^\circ$$

$$\hat{C} + \hat{A} + B = 180 \rightarrow 70 + 40 + B = 180 \rightarrow B = 70^\circ$$

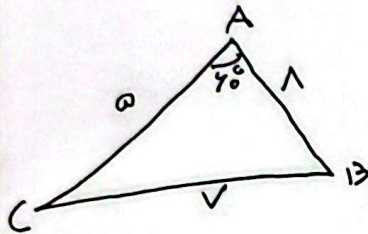


$$BC^2 = AB^2 + AC^2 - 2AB \cdot AC \cos \alpha$$

$$f = f + 1 - f \cos \alpha \rightarrow \cos \alpha = \frac{1}{f}$$

$$DE^2 = AD^2 + AE^2 - 2AD \cdot AE \cos \alpha = 1 + 1 - f \times \frac{1}{f}$$

$$= f_0 \rightarrow DE = \sqrt{f_0} = \sqrt{10}$$

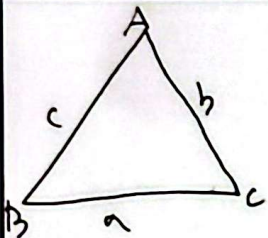


$$BC^2 = AC^2 + AB^2 - 2AC \cdot AB \cos 40^\circ$$

$$= 1 + 1 - 2 \times 1 \times \frac{1}{f} = f_0 \rightarrow BC = \sqrt{f_0}$$

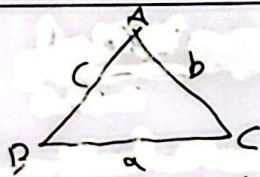
$$S = \frac{1}{2} \times AC \times AB \times \sin 40^\circ$$

$$= \frac{1}{2} \times 1 \times 1 \times \frac{\sqrt{f_0}}{f} = \frac{10\sqrt{f_0}}{f}$$



$$\frac{(b+c)^2 - a^2}{bc \cos A + 1} = \frac{b^2 + c^2 + 2bc - a^2}{bc \cos A + 1} = \frac{b^2 + c^2 + 2bc - (b^2 + c^2 - 2bc \cos A)}{bc \cos A + 1}$$

$$= \frac{4bc \cos A}{bc \cos A + 1} = \frac{4bc \cos A}{bc \cos A + 1} = 4$$



$$a^2 = b^2 + c^2 - 2bc \cos A$$

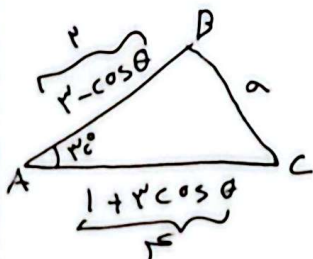
$$\frac{a^2 + b^2 - c^2}{a + b - c} = a \rightarrow a^2 + b^2 - c^2 = a^2 + a^2 b - a^2 c$$

$$\rightarrow b^2 - c^2 = a^2 (b - c) \rightarrow b^2 + c^2 + bc = a^2$$

$$(b+c)(b^2 + c^2 + bc) = a^2$$

$$b^2 + c^2 + bc = b^2 + c^2 - 2bc \cos A$$

$$\rightarrow \cos A = -\frac{1}{2}$$



$$S = \frac{1}{2} \times AB \times AC \times \sin \theta \rightarrow \frac{1}{2} \times 1 \times 1 \times \sin \theta = \frac{1}{2} \times 1 \times 1 \times \sin \theta$$

$$\rightarrow \sin \theta = \frac{1}{2} \rightarrow \theta = 30^\circ$$

$$\rightarrow \cos \theta = \frac{\sqrt{3}}{2}$$

$$a^2 = AB^2 + AC^2 - 2AB \cdot AC \cos \theta = 1 + 1 - 2 \times 1 \times \frac{\sqrt{3}}{2} = 2 - \sqrt{3}$$

$$a = \sqrt{2 - \sqrt{3}}$$

$$a^2 = AB^2 + AC^2 - 2AB \cdot AC \cos \theta = 1 + 1 - 2 \times 1 \times \frac{\sqrt{3}}{2} = 2 - \sqrt{3}$$