

1  $(0,1) (3,0) \Rightarrow m = \frac{0-1}{3-0} = \frac{-1}{3} \Rightarrow f'(x) = \frac{-1}{3}$

2  $(-1,1), (2,2) \Rightarrow m = f'(A) = \frac{2-1}{2-(-1)} = \frac{1}{3} \Rightarrow y-2 = \frac{1}{3}(x-2) \Rightarrow y = \frac{1}{3}x + \frac{4}{3} \Rightarrow \sqrt{ax-1} = \frac{1}{3}x + \frac{4}{3}$   
 $\Rightarrow ax-1 = \frac{1}{9}x^2 + \frac{8}{9}x + \frac{16}{9} \Rightarrow \frac{1}{9}x^2 + (\frac{8}{9}-a)x + \frac{16}{9} + 1 = 0 \Rightarrow \Delta = (\frac{8}{9}-a)^2 - 4(\frac{1}{9})(\frac{16}{9}+1) = 0 \Rightarrow (\frac{8}{9}-a)^2 = \frac{100}{81} \Rightarrow \begin{cases} \frac{8}{9}-a = \frac{10}{9} \Rightarrow a = -\frac{2}{9} \\ \frac{8}{9}-a = -\frac{10}{9} \Rightarrow a = \frac{18}{9} = 2 \end{cases}$   
 $a = \frac{2}{9} \Rightarrow f'(x) = \frac{a}{2\sqrt{ax-1}} = \frac{\frac{2}{9}}{2\sqrt{\frac{2}{9}x-1}} = \frac{1}{3\sqrt{\frac{2}{9}x-1}} \neq \frac{1}{3}$  *مستطقی نیست*  
 $a = 2 \Rightarrow \frac{2}{2\sqrt{2x-1}} = \frac{1}{3} \Rightarrow x = 5 \Rightarrow \boxed{f(5) = 3}$

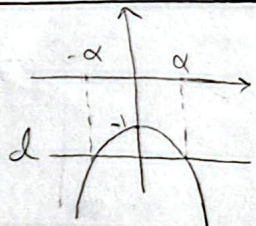
3  $fy - 3^n = n \Rightarrow y = \frac{3^n}{f}x + \frac{n}{f} \Rightarrow \frac{1+m+1}{f} = \frac{3^n}{f} + \frac{n}{f} \Rightarrow 1+m = 3^n + n \Rightarrow m = n+1$   
 $y' = \frac{(3^{n+m})(n+1) - (n+1+m+1)}{(n+1)^2} \Rightarrow \frac{(3^{n+m})(1) - (n+1+m)}{1 \cdot 2} = \frac{3^n}{f} \Rightarrow n+3^m-2-m = 12 = 3^m+2 \Rightarrow m=2 \Rightarrow n=1 \Rightarrow \boxed{m+n=3}$

4  $3g(x) = \frac{9}{3+\sin x} - f(x) = \frac{(3-\sin x)(9+\sin^2 x + 3^2 \sin x)}{(3-\sin x)(3+\sin x)} = \frac{\sin^2 x + 3^2 \sin x + 9}{3+\sin x} \Rightarrow h(x) = 3g(x) - f(x) = \frac{-(\sin^2 x + 3^2 \sin x)}{3+\sin x}$   
 $= -\sin x \Rightarrow h'(x) = -\cos x \Rightarrow h'(\frac{\pi}{2}) = \boxed{-1}$

5  $f \log(x) = \frac{1}{\sqrt{\frac{1}{x^2+1} + \frac{1}{x^2+1}}} \stackrel{\sqrt{2}}{=} \frac{-1}{\sqrt{\frac{1}{2x^2} + \frac{1}{2x^2}}} = \frac{-1}{\sqrt{\frac{1}{x^2}}} = -x \Rightarrow (f \log(\sqrt{x}))' = \boxed{-1}$

6  $f'(0) = \lim_{x \rightarrow 0} \frac{xg(x)+1}{x-0} = \lim_{x \rightarrow 0} g(x) = \dots$   
 $f'(x) = 2 \left( \frac{\sin x - 1}{\sin x + 1} \right) \left( \frac{2}{(\sin x + 1)^2} \right) \times \cos x \Rightarrow f'(0) = 2 \times -1 \times 2 \times 1 = \boxed{-4}$

7  $y = x^2 + 1 \Rightarrow y = -x^2 - 1 \Rightarrow y' = -2x \Rightarrow (-2\alpha)(-2(-\alpha)) = -4\alpha = -1 \Rightarrow \alpha^2 = \frac{1}{4} \Rightarrow \alpha = \pm \frac{1}{2}$   
 $\Rightarrow |y| = \left| \frac{1}{4} - 1 \right| = \left| \frac{-3}{4} \right| = \boxed{\frac{3}{4}}$



8  $f(x) = 2\sqrt{x}(x^2+r) \Rightarrow f(b) = 2\sqrt{b}(b^2+r) = ab$   
 $d: y = ax$   
 $f'(x) = \frac{1}{\sqrt{x}}(2x^2+r) + 2x(2x) \Rightarrow f'(b) = \frac{1}{\sqrt{b}}(2b^2+r) + 4b\sqrt{b} = a$   
 $\Rightarrow 2b^2+r = 2b\sqrt{b} + 4b\sqrt{b} \Rightarrow 2b^2+r = 6b\sqrt{b} \Rightarrow r = 6b\sqrt{b} - 2b^2$   
 $\Rightarrow 2b^2 + 6b\sqrt{b} - 2b^2 = 2b\sqrt{b} \Rightarrow 2b\sqrt{b} = 2b\sqrt{b} \Rightarrow b^2 = \frac{1}{4} \Rightarrow b = \frac{1}{2}$   
 $D_f: [0, +\infty) \Rightarrow f'(\frac{1}{2}) = \sqrt{2}\left(\frac{1}{2}\right) + 4\left(\frac{1}{2}\right)\left(\frac{1}{2}\right) = \boxed{\sqrt{2}} = a$

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$$1. f_{og}(n) = \left( \frac{1}{\sqrt{n^2-1}} \left[ \frac{1}{\sqrt{n^2-1}} \right] \right)^n$$

$$\lim_{n \rightarrow \left(\frac{\omega}{\gamma}\right)^-} \frac{\left(\frac{1}{\sqrt{n^2-1}} [ \gamma^+ ]\right)^n - (\gamma \times \gamma)^n}{n - \frac{\sqrt{\omega}}{\gamma}} \stackrel{\frac{0}{0}}{=} \stackrel{H.o.P}{=} \frac{\gamma \left(\frac{\gamma}{\sqrt{n^2-1}}\right)^n \times \frac{-2n\gamma}{\gamma \sqrt{n^2-1}} \times \frac{1}{n^2-1}}{1} = \frac{-1 \times -\omega \sqrt{\omega}}{\boxed{L.H.A}}$$