

$$\Lambda \cos x - \tan x = 1 \rightarrow \Lambda \cos x = 1 + \tan x \rightarrow \Lambda \cos x = \frac{1}{\cos x} \rightarrow \Lambda \cos^2 x = 1$$

①

$$\rightarrow \cos^2 x = \frac{1}{\Lambda} \rightarrow \cos x = \frac{1}{\sqrt{\Lambda}}$$



جواب ۲

$$\Lambda \sin^2 x + \sqrt{\Lambda} \cos^2 x = -1 \rightarrow \Lambda \sin^2 x + \sqrt{\Lambda} \cos^2 x + 1 = 0 \rightarrow \Lambda \sin^2 x + \sqrt{\Lambda} (\cos^2 x + 1) = 0$$

②

$$\Lambda \sin^2 x + \sqrt{\Lambda} \cos^2 x = 0$$

$$\rightarrow \sin x = 0 \rightarrow x = k\pi$$

$$\sqrt{\Lambda} \cos^2 x = 0 \rightarrow \cos x = 0$$

$$\rightarrow \cos^2 x = 0 \rightarrow \frac{x}{\sqrt{\Lambda}} = k\pi + \frac{\pi}{\sqrt{\Lambda}} \rightarrow x = k\pi + \frac{\pi}{\sqrt{\Lambda}} \rightarrow x = \frac{k\pi}{\sqrt{\Lambda}} + \frac{\pi}{\sqrt{\Lambda}}$$

③

$$\textcircled{1} \cap \textcircled{2} = \left\{ \pi, -\pi \right\}$$

جواب ۲

$$\sqrt{\Lambda} \sin x \cos^2 x + \sin x = 1 \rightarrow \sqrt{\Lambda} \sin^2 x - \sqrt{\Lambda} \sin x + 1 = 0 \rightarrow (\sin x + 1)(\sqrt{\Lambda} \sin x - \sqrt{\Lambda} \sin x + 1) = 0$$

④

$$\sin x = -1$$

$$\sin x = \frac{1}{\sqrt{\Lambda}}$$

$$x = \frac{k\pi}{\sqrt{\Lambda}}, \frac{\pi}{\sqrt{\Lambda}}, \frac{3\pi}{\sqrt{\Lambda}}$$

$$\frac{1}{\sin\left(\frac{k\pi}{\sqrt{\Lambda}}\right)} + \frac{1}{\cos\left(\frac{k\pi}{\sqrt{\Lambda}}\right)} = 0 \rightarrow \frac{1}{\sin\left(\frac{k\pi}{\sqrt{\Lambda}}\right)} + \frac{1}{-\sin\left(\frac{k\pi}{\sqrt{\Lambda}}\right)} = 0$$

$$\frac{-\sin\left(\frac{k\pi}{\sqrt{\Lambda}}\right) + \sin\left(\frac{k\pi}{\sqrt{\Lambda}}\right)}{-\sin\left(\frac{k\pi}{\sqrt{\Lambda}}\right) \cdot \sin\left(\frac{k\pi}{\sqrt{\Lambda}}\right)} = 0 \rightarrow \sin\left(\frac{k\pi}{\sqrt{\Lambda}}\right) = \sin\left(\frac{k\pi}{\sqrt{\Lambda}}\right)$$

⑤

$$\sin x = \frac{k\pi}{\sqrt{\Lambda}} + \frac{\pi}{\sqrt{\Lambda}} \rightarrow x = k\pi + \frac{\pi}{\sqrt{\Lambda}}$$

$$\sin x = \frac{k\pi}{\sqrt{\Lambda}} + \frac{\pi}{\sqrt{\Lambda}} - \frac{\pi}{\sqrt{\Lambda}} - \frac{\pi}{\sqrt{\Lambda}} \rightarrow x = \frac{k\pi}{\sqrt{\Lambda}} + \frac{\pi}{\sqrt{\Lambda}}$$

$$x = \frac{k\pi}{\sqrt{\Lambda}}, \frac{\pi}{\sqrt{\Lambda}}, \frac{3\pi}{\sqrt{\Lambda}}, \frac{5\pi}{\sqrt{\Lambda}}$$

جواب ۲

$$x = \frac{k\pi}{\sqrt{\Lambda}} + \frac{\pi}{\sqrt{\Lambda}} \rightarrow \tan \frac{k\pi}{\sqrt{\Lambda}} = -\tan \frac{\pi}{\sqrt{\Lambda}} = -\frac{\sqrt{\Lambda}}{\sqrt{\Lambda}}$$

$$m(\cos x - \sin x) - \sqrt{\Lambda} \sin x = \sqrt{\Lambda}$$

⑥

$$\cos\left(m\frac{\pi}{\sqrt{\Lambda}}\right) = \frac{1}{\sqrt{\Lambda}} \rightarrow \frac{\sqrt{\Lambda}}{\sqrt{\Lambda}} \cos x - \frac{\sqrt{\Lambda}}{\sqrt{\Lambda}} \sin x = \frac{1}{\sqrt{\Lambda}} \rightarrow \cos - \sin = \frac{1}{\sqrt{\Lambda}} = \frac{\sqrt{\Lambda}}{\sqrt{\Lambda}} \frac{\sqrt{\Lambda}}{\sqrt{\Lambda}}$$

$$(\cos - \sin)^2 = 1 - \sin^2 x = \left(\frac{\sqrt{\Lambda}}{\sqrt{\Lambda}}\right)^2 = \frac{\Lambda}{\Lambda} \rightarrow \sin^2 x = \frac{1}{\Lambda} \rightarrow m\left(\frac{\sqrt{\Lambda}}{\sqrt{\Lambda}}\right) - \sqrt{\Lambda} = \sqrt{\Lambda} \Rightarrow m = 4$$

$$\frac{m\sqrt{\Lambda}}{\sqrt{\Lambda}} = \sqrt{\Lambda}$$

$$\sin\left(n + \frac{\pi}{4}\right) \cos\left(n - \frac{\pi}{4}\right) = 1 \rightarrow \frac{1}{2} \sin\left(n + \frac{\pi}{4}\right) = 1 \rightarrow \sin\left(n + \frac{\pi}{4}\right) = \frac{1}{2} = \sin \frac{\pi}{6}$$

$$= \cos\left(\frac{\pi}{4} - n\right)$$

$$n + \frac{\pi}{4} = 2k\pi + \frac{\pi}{4} \rightarrow n = 2k\pi$$

$$n + \frac{\pi}{4} = 2k\pi + \pi - \frac{\pi}{4} \rightarrow n = 2k\pi + \frac{3\pi}{2}$$

$$\boxed{-\frac{1}{2} \neq \frac{1}{2}}$$

$$n = 0, 2\pi, \frac{3\pi}{2}$$

$$\sin n + \sqrt{3} \cos n = \sqrt{2} \rightarrow \frac{1}{2} \sin n + \frac{\sqrt{3}}{2} \cos n = \frac{\sqrt{2}}{2} \rightarrow \sin\left(n + \frac{\pi}{6}\right) = \frac{\sqrt{2}}{2} = \sin \frac{\pi}{4}$$

$$n + \frac{\pi}{6} = 2k\pi + \frac{\pi}{6} \rightarrow n = 2k\pi$$

$$n = -\frac{\pi}{12}, \frac{5\pi}{12}, \frac{13\pi}{12}, \frac{19\pi}{12}$$

$$n + \frac{\pi}{6} = 2k\pi + \pi - \frac{\pi}{6} \rightarrow n = 2k\pi + \frac{5\pi}{6}$$

$$\frac{4\pi}{3} = \frac{8\pi}{6} = \frac{16\pi}{12} = \frac{16\pi}{12}$$

$$\sin n \cdot \sin\left(\frac{5\pi}{6} - n\right) = -\sin n \cos n = 1 \rightarrow -\sin 2n = 1 \rightarrow \sin 2n = -\frac{1}{2} = \sin\left(-\frac{\pi}{6}\right)$$

$$2n = 2k\pi - \frac{\pi}{6} \rightarrow n = k\pi - \frac{\pi}{12}$$

$$n = \frac{11\pi}{12}, \frac{17\pi}{12}, \frac{23\pi}{12}, \frac{29\pi}{12}$$

$$2n = 2k\pi + \pi - \frac{\pi}{6} \rightarrow n = k\pi + \frac{5\pi}{12}$$

$$\frac{11\pi}{12} = \frac{11\pi}{12}$$

$$(1 + \cos 2\alpha)(1 + \cos 2\alpha)(1 + \cos 2\alpha) = \frac{1}{\lambda}$$

$$(2\cos^2 \alpha)(2\cos^2 \alpha)(2\cos^2 \alpha) = \frac{1}{\lambda} \rightarrow (2\cos^2 \alpha)^3 = \frac{1}{\lambda} \rightarrow \cos^2 \alpha = \frac{1}{2\sqrt{\lambda}} \rightarrow \sin^2 \alpha = \frac{1}{2\sqrt{\lambda}}$$

$$\frac{\frac{1}{2\sqrt{\lambda}} \sin^2 \alpha}{\sin^2 \alpha} = \frac{1}{2\sqrt{\lambda}} \rightarrow \sin^2 \alpha = \sin^2 \alpha \rightarrow \cos 2\alpha = \cos 4\alpha$$

$$2\alpha = 2k\pi \pm 4\alpha \rightarrow \alpha = k\pi \pm 2\alpha \rightarrow \alpha = \frac{2k\pi}{3} \rightarrow \alpha = \frac{2\pi}{3}$$

$$\tan 3n \cdot \tan n = 1$$

$$\tan 3n = \frac{1}{\tan n} = \cot n \rightarrow \tan 3n = \tan\left(\frac{\pi}{2} - n\right)$$

$$3n = k\pi + \frac{\pi}{2} - n \rightarrow n = \frac{k\pi}{4} + \frac{\pi}{4}$$

$$n = \frac{9\pi}{4}, \frac{11\pi}{4}, \frac{13\pi}{4}, \frac{15\pi}{4} \rightarrow \frac{9\pi}{4} = \frac{9\pi}{4}$$