

$$\cos^r x = r^r \sin^r x - 1 \rightarrow r^r \sin^r x = \cos^r x + 1 \quad \text{الف (۱)}$$

$$r^r \sin^r x = r^r \cos^r x = r^r (1 - \sin^r x)$$

$$r^r \sin^r x + r^r \sin^r x - r^r = 0 \quad \sin x = \frac{-r^r \pm \delta}{r^r} = \frac{1}{r^r} \text{ و } \frac{-r^r}{r^r}$$

$$\sin x = \frac{1}{r^r} \quad x = r^r k\pi + \frac{\pi}{4} \text{ و } r^r k\pi + \frac{3\pi}{4} \quad \text{ع.ق}$$

$$\cos^r x - \sin^r x + \cos x - r^r (\cos^r x + \sin^r x) = 0 \quad \text{ب}$$

$$-\cos^r x - r^r \sin^r x + \cos x = 0 \Rightarrow -\cos^r x - r^r (1 - \cos^r x) + \cos x$$

$$r^r \cos^r x + \cos x - r^r = 0 \Rightarrow \cos x = 1 \text{ و } \frac{-r^r}{r^r} \quad \text{ع.ق}$$

$$\cos x = 1 \quad x = r^r k\pi$$

$$(\sin^r x + \cos^r x)(\sin^r x - \cos^r x) = r^r \sin^r x \cos^r x \quad \text{الف (۲)}$$

$$r^r \sin^r x \cos^r x = -\cos^r x \quad \begin{cases} \cos^r x = 0 \\ r^r \sin^r x = -1 \end{cases}$$

$$\cos^r x = 0 \rightarrow r^r x = k\pi + \frac{\pi}{r^r}$$

$$\sin^r x = \frac{-1}{r^r} \quad r^r x = \left\{ r^r k\pi - \frac{\pi}{4}, r^r k\pi - \frac{3\pi}{4} \right\}$$

$$x = \frac{k\pi}{r^r} + \frac{\pi}{r^r} \quad \text{و} \quad x = \left\{ k\pi - \frac{\pi}{r^r}, k\pi - \frac{3\pi}{r^r} \right\}$$

$$x = \left\{ k\pi \pm \frac{\pi}{r^r} \right\} \quad \text{و} \quad \frac{k\pi}{r^r} + \frac{\pi}{r^r}$$

$$r^r \sin^r x \cos x = 1 - r^r \cos^r x = \sin^r x - \cos^r x \quad \text{ب}$$

$$\sin^r x = -\cos^r x$$

$$r^r x = k\pi + \frac{r^r \pi}{r^r} \Rightarrow x = \frac{k\pi}{r^r} + \frac{r^r \pi}{r^r}$$

$$\frac{\cos x}{\sin x} \times (\cos x + 1) = \frac{1}{\sin x} \quad \text{الف (م)}$$

$$\Rightarrow \cos^2 x + \cos x = 1 \Rightarrow \cos x = 1 - \cos^2 x$$

$$\cos x = \sin^2 x - \cos^2 x = -\cos 2x$$

$$\cos 2x = -\cos x = \cos(\pi - x)$$

$$2x = 2k\pi \pm (\pi - x)$$

$$\begin{cases} 2x = 2k\pi + \pi - x \rightarrow x = \frac{1}{3}2k\pi + \frac{\pi}{3} \\ 2x = 2k\pi - \pi + x \rightarrow x = 2k\pi - \pi \end{cases}$$

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$$y \sin^2 x - \sin x \cos x = y - \cos^2 x \quad \text{ب (ب)}$$

$$y \sin^2 x - \sin x \cos x = y \sin^2 x + \cos^2 x$$

$$\begin{cases} \cos x = 0 \rightarrow x = k\pi + \frac{\pi}{2} \\ \cos x = -\sin x \rightarrow x = k\pi - \frac{\pi}{4} \end{cases}$$

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$$\cos\left(\frac{\pi}{6} + x\right) \cos\left(x - \frac{\pi}{6}\right) = \frac{1}{4} \times (\cos 2x + \cos \frac{\pi}{3}) = \frac{1}{4} \quad \text{ج (ع)}$$

$$\Rightarrow \cos 2x + 0 = \frac{1}{4}$$

$$2x = 2k\pi \pm \frac{\pi}{2} \quad x = k\pi \pm \frac{\pi}{4}$$

$$-\sin 2x = \cos\left(2x + \frac{\pi}{2}\right) \quad \text{ب (ب)}$$

$$\Rightarrow \cos\left(2x - \frac{\pi}{4}\right) = \cos\left(2x + \frac{\pi}{2}\right)$$

$$2x - \frac{\pi}{4} = 2k\pi + 2x + \frac{\pi}{2} \rightarrow \text{جواب نادر}$$

$$\begin{cases} 2x - \frac{\pi}{4} = 2k\pi - 2x - \frac{\pi}{2} \Rightarrow 4x = 2k\pi - \frac{\pi}{4} \\ x = \frac{k\pi}{2} - \frac{\pi}{8} \end{cases}$$

$$x = \frac{k\pi}{2} - \frac{\pi}{8}$$

$$\frac{\sin \epsilon n + \sin \nu n}{\sin \nu n} = \frac{\nu \sin \nu n \cos \nu n + \sin \nu n}{\sin \nu n} \quad (3)$$

$$\frac{\sin \nu n (\nu \cos \nu n + 1)}{\sin \nu n} = \sin \nu n + \cos \nu n = 1$$

$$\Rightarrow \nu \cos \nu n = 0 \quad \nu n = k\pi + \frac{\pi}{\nu} \Rightarrow n = \frac{k\pi}{\nu} + \frac{\pi}{\epsilon}$$

$$\frac{\sin \frac{n}{\nu}}{1 + \cos \frac{n}{\nu}} \times \frac{1 - \cos \frac{n}{\nu}}{1 - \cos \frac{n}{\nu}} = \frac{\sin \frac{n}{\nu} \times (1 - \cos \frac{n}{\nu})}{1 - \cos \frac{n}{\nu}} \quad (4)$$

$$\left. \begin{aligned} \frac{\sin \frac{n}{\nu} \times (1 - \cos \frac{n}{\nu})}{\sin^2 \frac{n}{\nu}} &= \frac{1 - \cos \frac{n}{\nu}}{\sin \frac{n}{\nu}} \\ \frac{1}{\sin \frac{n}{\nu}} + \frac{\cos \frac{n}{\nu}}{\sin \frac{n}{\nu}} &= \frac{1 + \cos \frac{n}{\nu}}{\sin \frac{n}{\nu}} \end{aligned} \right\} \frac{1 - \cos \frac{n}{\nu}}{\sin \frac{n}{\nu}} = \frac{1 + \cos \frac{n}{\nu}}{\sin \frac{n}{\nu}}$$

$$1 - \cos \frac{n}{\nu} = 1 + \cos \frac{n}{\nu} \Rightarrow \nu \cos \frac{n}{\nu} = 0 \quad n = \nu k\pi + \pi$$

$$\text{مجموعه جواب} = \{-\pi, \pi\}$$

$$|\pi - (-\pi)| = \nu \pi$$

$$-\sin^2 n \cos \nu n = 1 - \cos^2 n = \sin^2 n \quad (5)$$

$$\begin{cases} \sin^2 n = 0 & n = k\pi \\ \cos^2 n = -1 & \nu n = \nu k\pi + \pi \quad n = \frac{\nu}{\epsilon} k\pi + \frac{\pi}{\epsilon} \end{cases}$$

$$[0, \nu\pi] \rightarrow \left\{0, \pi, \nu\pi, \frac{\pi}{\nu}, \frac{\nu\pi}{\nu}\right\} \quad \text{جواب}$$

$$\frac{1 - \tan n}{1 + \tan n} = \tan \left(\frac{\pi}{\epsilon} - n \right) \quad (6)$$

$$\tan \nu n = \tan \left(\frac{\pi}{\epsilon} - n \right)$$

$$\nu n = k\pi + \frac{\pi}{\epsilon} - n \Rightarrow \epsilon n = k\pi + \frac{\pi}{\epsilon}$$

$$n = \frac{k\pi}{\epsilon} + \frac{\pi}{14}$$

$$\sqrt{1 + 2 \sin \pi \cos \pi} = \sqrt{2} \cos \pi \rightarrow \cos \pi > 0 \quad (9)$$

توان $\rightarrow 1 + \sin 2\pi = 2 \cos^2 \pi = 2 \left(\frac{1 + \cos 2\pi}{2} \right)$

$$1 + \sin 2\pi = 1 + \cos 2\pi$$

$$\cos 2\pi = \sin 2\pi \quad , \quad \cos 2\pi = \sin \left(\frac{\pi}{2} - 2\pi \right)$$

$$\sin 2\pi = \sin \left(\frac{\pi}{2} - 2\pi \right)$$

$$\begin{cases} 2\pi = 2k\pi + \frac{\pi}{2} - 2\pi & n = \frac{k\pi}{2} + \frac{\pi}{4} \\ 2\pi = 2k\pi + \pi - \frac{\pi}{2} + 2\pi & n = -k\pi - \frac{\pi}{4} \end{cases}$$

مقادیر جواب دار $\{ \frac{\pi}{4}, \frac{5\pi}{4}, \frac{9\pi}{4} \}$ مجموعه جواب

مقادیر منفی $\frac{5\pi}{4}$ و $\frac{9\pi}{4}$ را $\cos \frac{5\pi}{4}$ مقدار منفی دارد

$$\sin^2 \pi - \cos^2 \pi = (\sin^2 \pi + \cos^2 \pi)(\sin^2 \pi - \cos^2 \pi) = 1 \quad (10)$$

$$\Rightarrow -\cos 2\pi = 1 \Rightarrow \cos 2\pi = -1$$

$$2\pi = 2k\pi + \pi \quad n = k\pi + \frac{\pi}{2}$$

مجموعه جواب $\{ \frac{\pi}{2}, \frac{3\pi}{2} \}$

$$\sin^2 \pi - \cos^2 \pi = (\sin \pi - \cos \pi)(1 + \sin \pi \cos \pi) \quad (11)$$

$$\sqrt{2} \times \sin \left(\pi - \frac{\pi}{4} \right) \times (1 + \sin \pi \cos \pi) = -1$$

$$R = (-\sqrt{2}, \sqrt{2})$$

$$= 1 + \frac{1}{2} \sin 2\pi$$

$$\rightarrow R = \left\{ \frac{1}{2}, \frac{3}{2} \right\}$$

$$\text{حد اکثر مقدار عبارت} = -\sqrt{2} \times \frac{1}{2} = \frac{-\sqrt{2}}{2}$$

جواب های این معادله همواره برقرار است - هستند معادله جواب ندارد