

B. تمرينات

المسائل

أ) $\cos Px = P \sin x - 1 \Rightarrow P \sin^P + P \sin x - P = 0$ (1)

$1 - P \sin^P x$

$x = \frac{-P \pm \Delta}{2P}$

$-P x$

$\frac{1}{P} = \sin \frac{\pi}{4}$

$\Rightarrow x = \begin{cases} Pk\pi + \frac{\pi}{4} \\ Pk\pi + \frac{3\pi}{4} \end{cases}$

ب) $\cos Px + \cos x - P = 0 \rightarrow P \cos^P + \cos - P = 0 \Rightarrow x = \begin{cases} \frac{1}{P} x \\ -\frac{1}{P} x \end{cases}$

$P \cos^P - 1$

$\cos x = \cos \pi \Rightarrow x = Pk\pi \pm \pi = Pk\pi$

أ) $\sin^P x - \cos^P x = \sin Px \rightarrow -\cos Px = \sin Px \rightarrow$ (P)

$+(\sin^P x - \cos^P x) (\sin^P x - \cos^P x)$

$\cos Px + \sin Px = 0 \rightarrow \cos Px (1 + P \sin Px) = 0$

$\Rightarrow \begin{cases} \cos Px = 0 \rightarrow Px = Pk\pi + \frac{\pi}{2} \rightarrow x = k\pi + \frac{\pi}{2P} \\ \sin Px = -\frac{1}{P} \rightarrow Px = Pk\pi + \frac{\pi}{P} \rightarrow x = k\pi + \frac{\pi}{P} \\ Px = Pk\pi - \frac{\pi}{P} \rightarrow x = k\pi - \frac{\pi}{P} \end{cases}$

ب) $P \cos^P x + P \sin x \cos x = 1 \rightarrow \cos Px = -\sin Px$

$\rightarrow \cos Px = \sin(-Px) \rightarrow \cos Px = \cos \frac{\pi}{2} + Px \rightarrow Px = Pk\pi + \frac{\pi}{2} + Px$

$Px = Pk\pi - \frac{\pi}{P} \rightarrow x = \frac{k\pi}{P} - \frac{\pi}{P}$

$Px = Pk\pi - \frac{\pi}{P} - Px \rightarrow$

أ) at $(P \cos x + 1) = \frac{1}{\sin x} \xrightarrow{\sin x \neq 0} \cos x (P \cos x + 1) = 1$ (P)

$\rightarrow P \cos^P x + \cos x - 1 = 0 \Rightarrow x = \begin{cases} -1 \rightarrow Pk\pi \pm \pi \\ \frac{1}{P} \rightarrow x = Pk\pi \pm \frac{\pi}{P} \end{cases}$

ب) $1 - \cos Px - \frac{1}{P} \sin Px + \frac{1}{P} + \frac{1}{P} \cos Px = P \rightarrow$

$\cos Px + \sin Px + 1 = 0 \rightarrow P \sin(Px + \frac{\pi}{2}) = -1 \rightarrow \sin(Px + \frac{\pi}{2}) = -\frac{1}{P}$

$\rightarrow Px + \frac{\pi}{2} = \begin{cases} Pk\pi + \frac{\pi}{2} \rightarrow Px = Pk\pi \rightarrow x = k\pi + \frac{\pi}{P} \\ Pk\pi - \frac{\pi}{2} \rightarrow Px = Pk\pi - \frac{\pi}{P} \rightarrow x = k\pi - \frac{\pi}{P} \end{cases}$

$$\text{ا) } \cos\left(\frac{\pi}{\varepsilon} + x\right) \cos\left(x - \frac{\pi}{\varepsilon}\right) = \frac{1}{\varepsilon} \rightarrow -\sin\left(x - \frac{\pi}{\varepsilon}\right) \cos\left(x - \frac{\pi}{\varepsilon}\right) = \frac{1}{\varepsilon} \quad (\varepsilon$$

$$\sin\left(x - \frac{\pi}{\varepsilon}\right) = -\frac{1}{\varepsilon} \rightarrow -\cos x = -\frac{1}{\varepsilon} \rightarrow \cos x = \frac{1}{\varepsilon} \rightarrow \boxed{x = k\pi \pm \frac{\pi}{\varepsilon}}$$

$$\begin{aligned} \text{ب) } \cos\left(x - \frac{\pi}{\eta}\right) &= \sin(-x) \rightarrow \sin\left(\frac{\pi}{\eta} - x + \frac{\pi}{\eta}\right) = \sin(-x) \\ &\rightarrow \sin\left(\frac{2\pi}{\eta} - x\right) = \sin(-x) \rightarrow \frac{2\pi}{\eta} - x = x + k\pi + \pi \rightarrow \\ &-x = x + k\pi + \frac{\pi}{\eta} \rightarrow -x = \frac{k\pi}{\eta} + \frac{\pi}{\eta} \Rightarrow x = -\frac{k\pi}{\eta} - \frac{\pi}{\eta} \end{aligned}$$

$$\frac{\sin \varepsilon x + \sin x}{\sin x} = \sin^r x = a^r x \rightarrow 1 = r \cos rx + 1 \quad (\alpha)$$

$x \neq \frac{k\pi}{r}$
 $\sin rx \neq 0 \rightarrow \cos rx = 0 \rightarrow \boxed{x = k\pi \pm \frac{\pi}{\varepsilon}}$

$$\frac{\sin \frac{x}{r}}{1 + \cos \frac{x}{r}} = \frac{1 + \cos \frac{x}{r}}{\sin \frac{x}{r}} \xrightarrow[\sin \frac{x}{r} \neq 0]{\cos \frac{x}{r} \neq -1} \sin^r = 1 + \cos \frac{x}{r} + r \cos \frac{x}{r} \rightarrow$$

$$r \cos \frac{x}{r} + r \cos \frac{x}{r} = 0 \rightarrow r \cos \frac{x}{r} (\cos \frac{x}{r} + 1) = 0 \quad \begin{cases} \cos \frac{x}{r} = 0 \rightarrow \\ \cos \frac{x}{r} = -1 \times \end{cases}$$

$$\cos \frac{x}{r} = 0 \rightarrow \frac{x}{r} = k\pi \pm \frac{\pi}{2} \rightarrow x = \varepsilon k\pi \pm \frac{\pi}{2} \quad \left[-\frac{\pi}{2}, \frac{\pi}{2} \right] \rightarrow \{-\pi, \pi\}$$

$$\Rightarrow |\pi - (-\pi)| = 2\pi$$

$$1 - \sin^r - \sin^r x \cos rx = 1 \rightarrow \sin^r (1 + \cos rx) = 0 \quad (\nu)$$

$$\sin^r x = 0 \rightarrow k\pi, \quad \cos rx = -1 \rightarrow rx = k\pi + \pi \rightarrow x = \frac{k\pi}{r} + \frac{\pi}{r}$$

$$\Rightarrow \omega = \frac{1}{r} = \left\{ 0, \pi, 2\pi, \frac{\pi}{r}, \frac{2\pi}{r}, \dots \right\} \Rightarrow \boxed{-\frac{\pi}{2}, \frac{\pi}{2}}$$

$D = [0, 2\pi]$

$$\frac{1 - \tan x}{1 + \tan x} = \tan^r x \rightarrow \tan\left(\frac{\pi}{\varepsilon} - x\right) = \tan^r x \rightarrow rx = k\pi + \frac{\pi}{\varepsilon} - x \quad (\lambda)$$

$$\rightarrow rx = k\pi + \frac{\pi}{\varepsilon} \rightarrow \boxed{\frac{k\pi}{\varepsilon} + \frac{\pi}{\varepsilon} = x}$$

$$\sqrt{1 + \sin^2 x} = \sqrt{r} \cos x \rightarrow 1 + \sin^2 x = r \cos^2 x \quad (9)$$

$$\Rightarrow 1 + \sin^2 x = r - r \sin^2 x \rightarrow r \sin^2 x + \sin^2 x - 1 = 0$$

$$r = \begin{cases} -1 \\ \frac{1}{r} \end{cases} \rightarrow \begin{cases} r = rk\pi - \frac{\pi}{r} \rightarrow x = k\pi - \frac{\pi}{r} \\ r = rk\pi + \frac{\pi}{r} \rightarrow k\pi + \frac{\pi}{r} \\ r = rk\pi + \frac{2\pi}{r} \rightarrow k\pi + \frac{2\pi}{r} \end{cases} \xrightarrow{[0, \pi]} \left\{ \frac{\pi}{r}, \frac{\pi}{r}, \frac{2\pi}{r} \right\}$$

— لا π

$$\text{ج) } \sin^2 x - \cos^2 x = 1 \rightarrow -\cos^2 x = 1 \rightarrow \cos^2 x = -1 \quad (10)$$

$$\rightarrow r = rk\pi \pm \pi \rightarrow \boxed{x = k\pi \pm \frac{\pi}{r}} \xrightarrow{[0, \pi]} \left\{ \frac{\pi}{r}, \frac{\pi}{r} \right\}$$

$$\text{د) } \sin^3 x - \cos^3 x = -1 \rightarrow \begin{cases} \sin^3 x = 0, \cos^3 = 1 \\ \sin^3 x = -1, \cos^3 = 0 \end{cases}$$

$$\rightarrow \left\{ k\pi, \frac{\pi}{r} \right\}$$