

$$\frac{4}{\sin 45} = \frac{AB}{\sin(\pi - \alpha)} \Rightarrow \frac{4}{\sin 45} = \frac{AB}{\sin \alpha} \rightarrow \sin \alpha = \frac{\sin 45 \cdot AB}{4}$$

$$\frac{3}{\sin 30} = \frac{AC}{\sin \alpha} \quad \sin \alpha = \frac{\sin 45 \cdot AC}{4} = \frac{\sin 45 \cdot AB}{4}$$

$$AC = \sin 45 \cdot AB$$

$$\frac{AB}{AC} = \frac{1}{\frac{\sqrt{2}}{2}} = \frac{2}{\sqrt{2}} = \sqrt{2} \quad \checkmark$$

$$A = \frac{\pi}{4} \Rightarrow A \left| \frac{1}{\frac{\sqrt{2}}{2}} \right. \quad B = \frac{3\pi}{4} \rightarrow B \left| \frac{-\sqrt{2}}{1} \right. \quad C = \frac{\pi}{2} \rightarrow C \left| \begin{smallmatrix} 0 \\ -1 \end{smallmatrix} \right.$$

$$\frac{1}{\sqrt{2}} \begin{vmatrix} \frac{1}{\sqrt{2}} & \frac{-\sqrt{2}}{1} & 0 \\ \frac{\sqrt{2}}{1} & \frac{1}{1} & -1 \\ 1 & 1 & 1 \end{vmatrix} = \frac{1}{\sqrt{2}} + \frac{\sqrt{2}}{\sqrt{2}} + 0 - 0 + \frac{1}{\sqrt{2}} + \frac{\sqrt{2}}{\sqrt{2}} = \frac{4}{\sqrt{2}} \times \frac{1}{\sqrt{2}} = \frac{4}{2} = 2$$

$$AC = \sqrt{\frac{1}{2} + (\frac{\sqrt{2}}{2} + 1)^2} =$$

$$S_{ABC} = \frac{1}{2} AB \cdot AC \cdot \sin \alpha = \frac{1}{2} \times \frac{1}{\sqrt{2}} \times \frac{1}{\sqrt{2}} \times \frac{1}{\sqrt{2}} \times \frac{1}{\sqrt{2}} = \frac{1}{2} \times \frac{1}{\sqrt{2}} \times \frac{1}{\sqrt{2}} \times \frac{1}{\sqrt{2}} \times \frac{1}{\sqrt{2}} = \frac{1}{8}$$

$$m = \cos \alpha$$

$$r \cos^2 \alpha - \cos^2 \alpha = \sin^2 \alpha (r \sin^2 \alpha - 1)$$

$$r \cos^2 \alpha - \cos^2 \alpha = \sin^2 \alpha (r \sin^2 \alpha - 1)$$

$$\cos^2 \alpha (r \cos^2 \alpha - 1) = \sin^2 \alpha (r \sin^2 \alpha - 1) = \sin^2 \alpha + \cos^2 \alpha$$