

سوال ۱

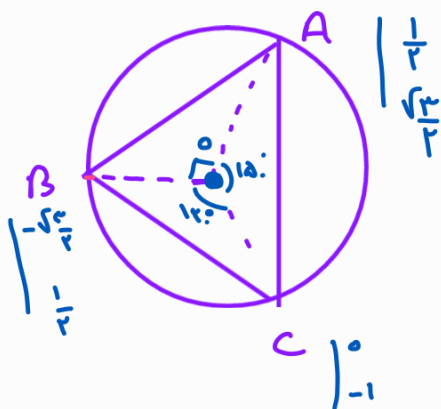
$$BT = \tan\left(\frac{\pi}{4} - \alpha\right) = \cot \alpha$$

OA و OT شعاع‌های دایره هستند
و طول آنها یکسان است.

$$OB^2 = OT^2 + BT^2 \rightarrow OB^2 = 1^2 + \cot^2 \alpha \rightarrow OB^2 = 1 + \cot^2 \alpha$$

$$OB^2 = \frac{1}{\sin^2 \alpha} \rightarrow OB = \frac{1}{|\sin \alpha|} \xrightarrow{\text{با توجه به } \alpha} OB = \frac{1}{\sin \alpha}$$

$$AB + 1 = \frac{1}{\sin \alpha} \rightarrow AB = \frac{1}{\sin \alpha} - 1 \leq \frac{1 - \sin \alpha}{\sin \alpha}$$



$$S_{AOC} = 1 \times 1 \times \frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$$

$$S_{OAR} = 1 \times 1 \times \frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$$

$$S_{OBC} = 1 \times 1 \times \frac{1}{2} \times \frac{\sqrt{2}}{2} = \frac{\sqrt{2}}{4}$$

$$S_{ABC} = \frac{1}{4} + \frac{1}{4} + \frac{\sqrt{2}}{4} = \frac{1 + \sqrt{2}}{2}$$

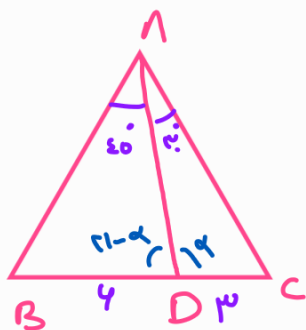
سوال ۳

$$BC^2 = 1^2 + 1^2 - 1 \times 1 \times 2 \times \frac{1}{2} = 1 + 1 - 1 = 1 \rightarrow BC = 1$$

$$AC^2 = 1^2 + 1^2 - 1 \times 1 \times 2 \times \frac{\sqrt{2}}{2} = 1 + 1 - \sqrt{2} \rightarrow AC = \sqrt{2 + \sqrt{2}}$$

$$AB^2 = 1^2 + 1^2 \rightarrow AB = \sqrt{2}$$

$$P_{ABC} = \sqrt{2} + \sqrt{2} + \sqrt{2 + \sqrt{2}}$$



$$ADC \rightarrow \frac{\sin \hat{\alpha}}{AC} = \frac{\sin \epsilon}{DC} \rightarrow AC = 4 \sin \hat{\alpha}$$

$$ABD \rightarrow \frac{\sin(\pi - \alpha)}{AB} = \frac{\sin \epsilon}{4} \rightarrow AB = 4 \sqrt{2} \sin \hat{\alpha}$$

$$\frac{AB}{AC} = \frac{4 \sqrt{2} \sin \hat{\alpha}}{4 \sin \hat{\alpha}} = \sqrt{2}$$

سوال ۲

سوال ۷

