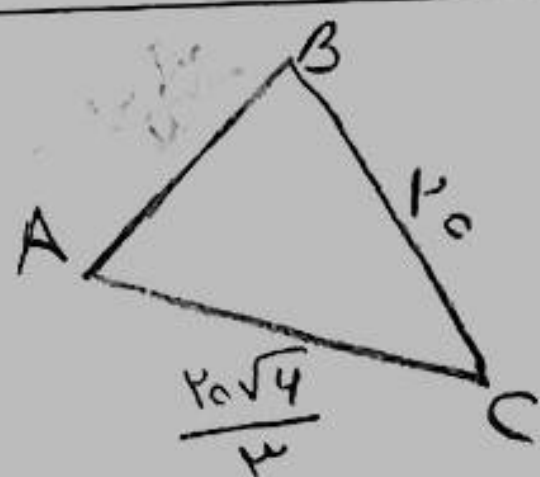




$$\hat{B} + \hat{C} = 120^\circ \Rightarrow \hat{B} = 120^\circ - \hat{C} \Rightarrow A = 40^\circ$$

$$\frac{BC}{\sin A} = \frac{AC}{\sin B} \Rightarrow \frac{10\sqrt{4}}{3} \sin 40^\circ = \frac{10}{\sin B} \Rightarrow \sin B = \frac{\sqrt{12}}{4} = \frac{3\sqrt{3}}{4} = \frac{\sqrt{3}}{4}$$

$$\Rightarrow \boxed{B = 45^\circ} \text{ و } \boxed{C = 75^\circ}$$

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$$A' = 40^\circ$$

$$\frac{CP}{\sin 60^\circ} = \frac{AC}{\sin 40^\circ} \Rightarrow \frac{10\sqrt{3}}{2} = \frac{AC}{\sin 40^\circ} \Rightarrow AC = 10\sqrt{3}$$

$$\frac{AC}{\sin B} = \frac{a}{\sin 40^\circ} \Rightarrow \frac{10\sqrt{3}}{1} = \frac{a}{\frac{\sqrt{3}}{4}} \Rightarrow \boxed{a = 40}$$

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$$\frac{c}{\sin C} = \frac{b}{\sin B} \Rightarrow \frac{\sin C}{\sin B} = \frac{c}{b} = \frac{c}{b^2 - 1} \Rightarrow b^2 - 1 = b \Rightarrow b^2 - b - 1 = 0$$

$$\Rightarrow (b - 2)(b + 1) = 0 \Rightarrow \begin{cases} b = -1 \times \\ b = 2 \sqrt{\end{cases}$$

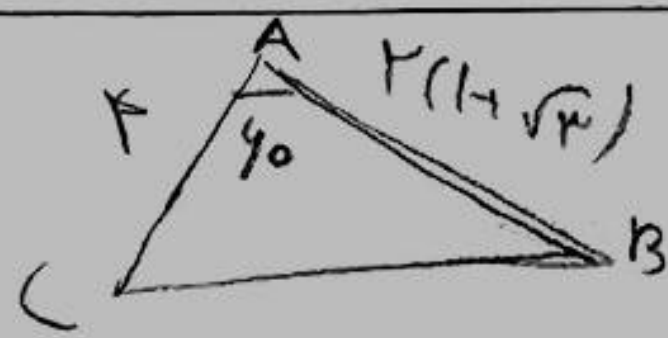
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$$a^2 = b^2 + c^2 - 2bc \cos A \Rightarrow 13^2 = 11^2 + 10^2 - 2 \times 11 \times 10 \cos B \Rightarrow$$

$$169 = 121 + 100 - 220 \cos B \Rightarrow 220 \cos B = 52 \Rightarrow \cos B = \frac{13}{55} \Rightarrow \sin^2 B + \cos^2 B = 1$$

$$\Rightarrow \sin^2 B = 1 - \frac{169}{3025} = \frac{9}{3025} \Rightarrow \boxed{\sin B = \frac{3}{55}}$$

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$$a^2 = 10^2 + (10(1+\sqrt{3}))^2 - 2 \times 10 \times 10(1+\sqrt{3}) \cdot \cos 40^\circ$$

$$\Rightarrow a^2 = 100 + 100(1+\sqrt{3})^2 - 200(1+\sqrt{3}) \cdot \frac{\sqrt{3}}{4} \Rightarrow a^2 = 100 + 100(1+2\sqrt{3}+3) - 50\sqrt{3}(1+\sqrt{3})$$

$$a^2 = (10 + 10\sqrt{3})^2 + (10)^2 - 2 \times 10 \times 10 \times \frac{1}{2} (1 + \sqrt{3})$$

$$a^2 = 100 + 100 + 100\sqrt{3} + 100 - 100 - 100\sqrt{3} \Rightarrow a^2 = 200 \Rightarrow a = 10\sqrt{2}$$

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$$\frac{10\sqrt{3}}{\sin 40^\circ} = \frac{10}{\sin B} \Rightarrow \sin B = \frac{10}{10\sqrt{3}} \Rightarrow \hat{B} = 30^\circ, \hat{C} = 110^\circ$$

مثلاً
کریم

$$a^2 = c^2 + b^2 - 2bc \cos \alpha \Rightarrow 1 = 1 + 1 - 2 \cos \alpha \Rightarrow 2 \cos \alpha = 1 \Rightarrow \cos \alpha = \frac{1}{2}$$

مثلاً
نیر

$$a^2 = d^2 + e^2 - 2de \cos \alpha \Rightarrow a^2 = 3^2 + 4^2 - 2 \times 3 \times 4 \times \frac{1}{2} = 5 \Rightarrow a = \sqrt{5} = \boxed{2\sqrt{5}}$$

$$\frac{1}{r} b \cdot c \times \sin A = \frac{1}{r} \times \frac{1}{r} \times \frac{1}{r} = \frac{1}{r} \sqrt{r} = \frac{1}{\sqrt{r}}$$

$$a^2 = b^2 + c^2 - 2bc \cos \hat{A} \Rightarrow a^2 = 10^2 + 1^2 - 2(10)(1)(\cos \hat{A})$$

$$= 101 - 20 \cos \hat{A} = 1 \Rightarrow \cos \hat{A} = \frac{100}{20} = 5 \Rightarrow \boxed{a = 10}$$

$$(b+c)^2 = b^2 + 2bc + c^2 \Rightarrow (b+c)^2 - a^2 = b^2 + 2bc + c^2 - a^2, a^2 = b^2 + c^2 - 2bc \cos A$$

$$\Rightarrow \cancel{b^2} + 2bc + \cancel{c^2} - \cancel{b^2} - \cancel{c^2} + 2bc \cos A = 2bc + 2bc \cos A = 2bc(1 + \cos A)$$

$$\Rightarrow \frac{(b+c)^2 - a^2}{bc(\cos A + 1)} = \frac{2bc(1 + \cos A)}{bc(\cos A + 1)} = \boxed{2}$$

$$a^2 = \frac{a^3 + b^3 - c^3}{a+b-c} \Rightarrow a^3 + a^2b - a^2c = a^3 + b^3 - c^3 \Rightarrow a^2b - a^2c = b^3 - c^3$$

$$\Rightarrow a^2(b-c) = b^3 - c^3 \Rightarrow a^2(\cancel{b-c}) = (\cancel{b-c})(b^2 + bc + c^2) \Rightarrow a^2 = b^2 + bc + c^2$$

$$b^2 + bc + c^2 = b^2 + c^2 - 2bc \cos A \Rightarrow \cancel{b^2} + \cancel{c^2} + bc = -2bc \cos A \Rightarrow \cos A = -\frac{1}{2}$$

$$\frac{1}{r} (1 - \cos \theta)(1 + 2 \cos \theta) \times \frac{1}{r} = 1 \Rightarrow 1 + 2 \cos \theta - \cos \theta - 2 \cos^2 \theta = 1$$

$$\Rightarrow 2 \cos^2 \theta - 1 \cos \theta + 0 = 0 \Rightarrow \cos \theta = \frac{1}{2} \Rightarrow \cos A = \frac{1}{2}$$

$$AB = 1$$

$$AC = 1 \Rightarrow a^2 = 1^2 + 1^2 - 2 \times 1 \times 1 \times \cos 120^\circ = 1 + 1 - 2 \times (-\frac{1}{2}) = 2 \Rightarrow \boxed{a = \sqrt{2}}$$