

$$y = \sqrt{x f(x)} \quad Df = [-5, -1] \cup [1, 5]$$

$$x f(x) \geq 0$$

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$$y = \sqrt{\frac{-x}{f(x)}} \quad Df = (-3, 0) \cup (0, 2)$$

$$\frac{-x}{f(x)} \geq 0 \text{ و } f(x) \neq 0$$

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$$f(x) - 2f(2) = x^2 - 3x + 4$$

$$x = 2 \Rightarrow f(2) - 2f(2) = 4 - 6 + 4 = 2 \Rightarrow f(2) = -2 \Rightarrow -2f(2) = 4$$

$$x = -2 \Rightarrow f(-2) + 4 = 4 + 6 + 4 = 14 \Rightarrow f(-2) = 10$$

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$$f(f(5)) + f(f(1))$$

$$f(x) = \begin{cases} x - \sqrt{x+4} & ; x > 3 \\ 2x + 3 & ; x \leq 3 \end{cases}$$

$$x = 2 \Rightarrow 4 + 3 = 7 \Rightarrow f(2) + 2 = 7 + 2 = 9$$

$$x = 1 \Rightarrow 2 + 3 = 5$$

$$x = 5 \Rightarrow 5 - \sqrt{9} = 2$$

$$\Rightarrow f(f(5)) + f(f(1)) = f(2) + 2 = 9$$

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$$f(n-1) - f(n) = 9n + 2$$

$$a(n-1)^2 - b(n-1) + 2 - an^2 + bn - 2 = 9n + 2$$

$$an^2 + a - 2an^2 - bn + b + 2 - an^2 + bn - 2 = 9n + 2$$

$$a = -3 \quad a - b = -3 - 5 = -8$$

$$b = 5$$

$$f(\sqrt{3}-2) = \frac{V - \cancel{2\sqrt{3}} + \cancel{4} - 1 + 4}{V - \cancel{2\sqrt{3}} + \cancel{4} - 1 + V} = \boxed{\frac{V-1}{V-2}}$$

$$(\sqrt{3}-2)^2 = 3 - 2\sqrt{3} + 4 = V - 2\sqrt{3}$$

$$2(\sqrt{3}-2) = 2\sqrt{3}-4$$

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$$f\left(x - \frac{1}{x}\right) = \frac{x^2+1}{x^2} = \frac{x^2 + \frac{1}{x^2}}{x^2} = x^2 + \frac{1}{x^2}$$

$$\Rightarrow \left(x - \frac{1}{x}\right)^2 - 2 = f\left(x - \frac{1}{x}\right) \Rightarrow x - \frac{1}{x} = -2$$

$$f(-2) = (-2)^2 - 2 = \boxed{2} = V$$

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$$\frac{f}{g} = \left\{ \left(2, \frac{0}{2}\right), \left(0, \frac{2}{\sqrt{5}}\right), \left(V, \frac{1}{\sqrt{1}}\right) \right\}$$

$$\frac{g}{f} = \left\{ \left(2, \frac{3}{2}\right), \left(0, \frac{\sqrt{5}}{2}\right), \left(V, \sqrt{1}\right) \right\}$$

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الف) $2f(x) = \{(2, 2), (3, 1), (-5, 4), (1, -2)\}$

ب) $f(x)+1 = \{(2, 2), (3, 5), (-5, 3), (1, -1)\}$

ج) $3f^2(x)+1 = \{(2, 4), (3, 9), (-5, 13), (1, 13)\}$

د) $f(2x) = \left\{ \left(1, 1\right), \left(\frac{3}{2}, 4\right), \left(-\frac{5}{2}, 2\right), \left(\frac{1}{2}, -2\right) \right\}$

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الف) $f-g = \{(2, 2), (1, 4), (3, 2)\}$

ب) $\frac{2f}{g} = \{(2, 4), (1, 2), (3, -2)\}$

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