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الف) $D_f = \mathbb{R} - \{1, 1, \omega, \omega^2\}$ ✓

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ب) توان مرتب‌سازی ج. توان فرد ؛ $D_f = \mathbb{R} - \{-1, -\frac{1}{2}, 2\}$

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الف) $x - \sqrt{x-2} \neq 0 \Rightarrow x \neq \sqrt{x-2} \Rightarrow x^2 \neq x-2$

$\Rightarrow x^2 + 2x - 2 \neq 0 \Rightarrow (x+2)(x-1) \neq 0 \Rightarrow D_f = \mathbb{R} - \{-2, 1\}$

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جواب ظاهری

ب) $x \neq \sqrt{x-2} \Rightarrow x^2 \neq x-2 \Rightarrow x^2 - 3x + 2 \neq 0$ $Q_f = (-\infty, \frac{3}{2}] - \{1\}$

$2x - 2 \geq 0$ $x \geq \frac{2}{3}$ $(x-2)(x-1) \neq 0 \Rightarrow D_f = \mathbb{R} - \{1, 2\}$

$Q_f = (\frac{2}{3}, +\infty) - \{1, 2\}$

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الف) $2\cos x \neq 1$

$\cos x \neq \frac{1}{2}$

$D_f = \mathbb{R} - \{2k\pi + \frac{\pi}{3}, 2k\pi - \frac{\pi}{3}\}$ ✓

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ب) $2\sin x \neq -1$

$\sin x \neq -\frac{1}{2}$ $2k\pi - \frac{\pi}{6}$

$D_f = \mathbb{R} - \{2k\pi + \frac{7\pi}{6}, 2k\pi + \frac{11\pi}{6}\}$ ✓

ج) $\cot x \neq 1$ $\frac{k\pi}{2}$

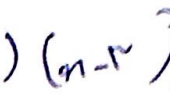
$D_f = \mathbb{R} - \{k\pi, k\pi + \frac{\pi}{4}\}$ ✓

د) $4\sin^2 x \neq 3$

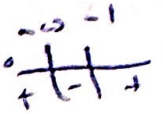
$\sin^2 x \neq \frac{3}{4}$

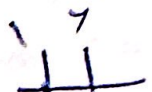
$\sin x \neq \pm\frac{\sqrt{3}}{2}$

$D_f = \mathbb{R} - \{k\pi \pm \frac{\pi}{3}, k\pi + \frac{2\pi}{3}\}$ ✓

ب) $(x-1)(x-3) \geq 0 \Rightarrow$  $\Rightarrow (-\infty, 1] \cup [3, +\infty)$ ✓

ج) $(x-1)(x-3) < 0 \Leftrightarrow$  $(1,3)$ ✓

د) $(x+1)(x+3) \geq 0$  $(-\infty, -3] \cup [-1, +\infty)$ ✓ (۲)

ه) $(x-1)(x-7) \leq 0$  $\Rightarrow [1,7]$ ✓

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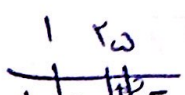
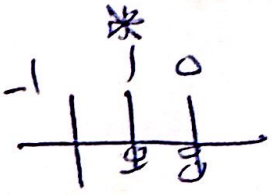
الف)  $(-\infty, 1) \cup (3, \infty)$ ✓



ب) $\frac{(x-1)(x+1)}{(x-1)(x-5)}$ $(-\infty, -1] \cup [5, +\infty)$ ✓ (۲)

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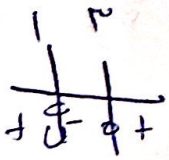
الف) $\frac{(x-1)(x-3)}{(x-1)(x^2+x+1)}$  $\Rightarrow [3, +\infty)$ ✓ (۲)

ب) $\sqrt[3]{\frac{(x-1)(x-2)}{(x-1)(x+1)}}$ $D_f = \mathbb{R} - \{-1, 1\}$ ✓

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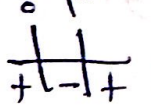
الف) $x^2 - 3x > 0 \Rightarrow x(x-3) > 0$  $= (-\infty, 0) \cup (3, +\infty)$ ✓

ب) $|x| - 2 > 0 \Rightarrow |x| > 2 \quad x > \pm 2$ $\Rightarrow (2,4) \cup (-3, -2) - \{-3, 2\}$ ✓

ج) $\frac{(x-3)(x-4)}{x-2} > 0$ $1. - x > 0$, $1. - x \neq 1$ $\Rightarrow (2, 10) - \{9\}$ ✓ (۲)

د) $(x-4)(x-1) \geq 0$, $x^2 - x > 0$, $x > 0$, $x \neq 1$ $\Rightarrow (0, 4] - \{1\}$ ✓

$$\frac{x^{3}-x}{x^{2}+x} = \frac{x(x-1)}{x(x+1)}$$

x^2-x : $-$ | $-$ | $+$ | $+$

x^2+x : $+$ | $-$ | $-$ | $+$

$f(x)$: $+$ | $-$ | $+$ | $-$ | $+$

-1 ، 0 ، 1

$+$ | $-$ | $+$

-1 ، 1

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$D_f = (-\infty, -1) \cup (-1, 1) \cup (1, \infty)$

$R_f = (-2, -1] \cup (2, 3]$

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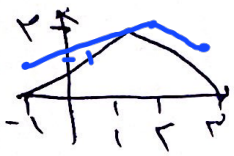
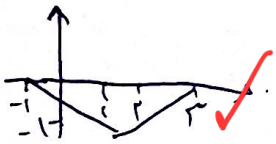
الف)



ب)

ج)



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