

... و $\{2, 3, 4\}$ و $\{1\}$

مجموعه آخر $n^2 \Rightarrow$ مجموعه آخر دسته $= 9^2 = 81$ ✓
 تعداد دسته n^2
 مجموعه اول $=$ مجموعه آخر $+ 1 = (n-1)^2 + 1 = (9-1)^2 + 1 = 64 + 1 = 65$ ✓
 تعداد دسته قبل
 واسطه حسابی $\Rightarrow \frac{81+65}{2} = 73$ ✓
 (۲)

... و $\{12, 13, \dots, 14\}$ و $\{1, 2, 3\}$ و $\{4\}$

مجموعه اول $= 1, 2, 3, 4, 12, 13, 14 \Rightarrow$ مجموعه آخر $= 12, 13, 14 \Rightarrow$ مجموعه آخر دسته $\Rightarrow 12, 13, 14$ ✓
 تعداد دسته (۱) (۲) (۳) (۴) (۵)
 مجموع اعداد $= \frac{12+14}{2} \times 3 = 36$ ✓
 مجموع اعداد $= \frac{1+4}{2} \times 3 = 6$ ✓
 مجموع اعداد $= \frac{12+14}{2} \times 3 + \frac{1+4}{2} \times 3 = 42$ ✓
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$a_0, a_3, a_6, a_9 \rightarrow$ ضابطه اول
 $a_1, a_4, a_7 \rightarrow$ ضابطه دوم
 $a_2, a_5, a_8 \rightarrow$ ضابطه سوم

$\left[\frac{n}{k+2} \right] - 2 \xrightarrow{n=3k+2} \left[\frac{3k+2}{k+2} \right] - 2 =$
 $\left[2 + \frac{k-2}{k+2} \right] - 2 = \left[\frac{k-2}{k+2} \right]$

به ازای هر k و n برابر است و به ازای بقیه اعداد صفر است پس جواب (۲) ✓

$S_{10} = 1 + 4(1+a) + 2 + (1+4a) + 4+0 + (2+a) + 1 = 19 \Rightarrow a = -2$ ✓

$an = an^2 + bn + c$

$2a + 4b + c = 14$
 $4a + 7b + c = 17.2$
 از هم کم کنیم $\Rightarrow 2a + 3b = 3.2 \Rightarrow a = 1.6 - 1.5b$
 $b = 4 \Rightarrow c = -1 \Rightarrow$

$a_1 = -0.2 + 4 - 1 = 3.8$
 $a_{10} = -0.2(100) + (4 \times 10) - 1 = 14$
 $a = \frac{1}{10} \times (-14) = -1.4$ ✓
 (۲) $a_{10} = -0.2(100) + (4 \times 10) - 1 = 14$
 $\frac{14}{3.8} = 3.68$ ✓

$a_4 = b_2$
 $a_1 = b_5$
 $a_1 + 3d = b_1 + d$
 $a_1 + 4d = b_1 + 4d$

$b_{10} = 0 \Rightarrow b_1 + 9d = 0 \Rightarrow b_1 = -9d$
 $b_1 + \frac{14}{5}d = 0 \Rightarrow b_1 = -\frac{14}{5}d$ ✓

$d = d \Rightarrow d = \frac{1}{5}d$ ✓
 $b_{10} = \frac{-\frac{14}{5}d + \frac{14}{5}d}{d} = \frac{0}{d} = 0$ ✓
 (۲)

$$y(a_1+d) = 0 \Rightarrow a_1(a_1+d) + \bar{a}_1(a_1+d) \Rightarrow$$

(2)

$$a_1^2 + \bar{a}_1 d + \bar{a}_1 d = a_1^2 + 10a_1 d + \bar{a}_1^2 + \bar{a}_1 d \rightarrow \bar{a}_1 + a_1 d - \bar{a}_1 d = 0 \Rightarrow$$

$$a = \frac{-d \pm \sqrt{d^2 + 10d^2}}{1} = \frac{-d \pm \sqrt{11}d}{1} \Rightarrow \begin{cases} a = \frac{\sqrt{11}d}{1} \Rightarrow \frac{a}{d} = \frac{\sqrt{11}d}{d} = \sqrt{11} \\ a = -d \Rightarrow \frac{a}{d} = \frac{-d}{d} = -1 \end{cases}$$

$$a_n: a \cdot b \cdot c$$

$$b_n: b \cdot \frac{a}{1} \cdot \frac{c}{1} \xrightarrow{\text{لحساب}} c \cdot \bar{a} \cdot \bar{b} \leq b \cdot \frac{b-d}{1} \cdot \frac{b+d}{1} \Rightarrow$$

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$$\frac{1}{1} (b-d)^2 = \frac{b}{1} (b+d) \Rightarrow d^2 - 10bd = 0 \Rightarrow d \cdot (d - 10b) = 0 \Rightarrow d = 0 \text{ or } d = 10b$$

$$a_n: b \cdot b \cdot b \Rightarrow b_n = b \cdot b \cdot b \Rightarrow q = -1 \Rightarrow \bar{q} = 1$$

$$a \cdot b \cdot c \Rightarrow b = aq, c = aq^2$$

$$b \cdot \bar{a} \cdot \bar{c} \xrightarrow{\text{لحساب}} aq \cdot \bar{a} \cdot \bar{a}q^2 \Rightarrow \bar{a} - \bar{a}aq^2 = aq^2 - \bar{a} \Rightarrow$$

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$$aq^2 + \bar{a}aq - \bar{a} = 0 \Rightarrow a(q^2 + \bar{q} - 1) = 0 \xrightarrow{a \neq 0} (q+1)(q-1) = 0 \Rightarrow q = -1 \text{ or } q = 1$$

$$\frac{aq}{aq} = \frac{aq^2}{aq^2} = q = -1$$

$$\frac{aq^2}{aq^2} + \frac{aq}{aq} = 1 \Rightarrow \left(\frac{q^2}{a^2}\right) + \frac{q}{a} - 1 = 0 \Rightarrow \frac{q}{a} = u \Rightarrow u^2 + u - 1 = 0 \Rightarrow (u+1)(u-1) = 0 \Rightarrow u = -1 \text{ or } u = 1$$

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$$\frac{q}{a} = 1 \Rightarrow \frac{a}{aq} = 1, \frac{q}{a} = -1 \Rightarrow \frac{a}{q} = -1$$

$$a_p = aq^p$$

$$a_f = aq^f = (aq^p)^f \Rightarrow aq^f = a^f q^{pf} \Rightarrow aq^f = 1$$

$$a_d = aq^f = 1$$

$$\frac{1}{1} - \frac{1}{1} = 0 \Rightarrow aq = 1 \Rightarrow a = \frac{1}{q}$$

$$\frac{aq^f}{aq^f} = \frac{1}{1} = 1 \Rightarrow q^f = 1 \Rightarrow q = 1$$