

$\frac{t}{9}$

$$+t+t9 = 21$$

1

$$\frac{t}{9} \times t \times t9 = t^3 - 9t \Rightarrow t = 3$$

$$\frac{t}{9} + t + t9 = 21 \Rightarrow \frac{t}{9} + t9 = 14 \Rightarrow t + t9^2 = 149$$

$$t + t9^2 - 149 = 0 \rightarrow \boxed{9=3}$$

$$x^4 + 2x^3 - 8 = 4x^2 \rightarrow x^4 - 2x^3 - 8 = 0 \rightarrow x = \pm 2 \xrightarrow{x>0} x=2$$

$$SV = 8 \left(\frac{1 - (\frac{1}{2})^4}{\frac{1}{2}} \right) = \frac{12V}{8}$$

2

$$243 + 2439 + 2439^2 + 2439^3 + 2439^4 = 243(1 + 9 + 9^2 + 9^3 + 9^4) = 243 \times \frac{9^5 - 1}{9 - 1} = 3456$$

3

$$1, 0, 0, A, 0, 0, 4f \quad \frac{4f-1}{4} = \frac{43}{4} = d$$

$$1 + \frac{43}{4} \times 4 = 1 + 43 = 44, d = 11, a = 32, d$$

$$1, 0, 0, B, 0, 0, 4f \quad 4f = 9 \Rightarrow 2=9$$

$$\underbrace{1, 0, 0}_9 \quad 1 \times 9^3 = B \rightarrow B = 8 \quad 8 + 32, d = 40, d$$

4

$$-2f, -\frac{9d}{f}, \dots$$

$$-2f = -\frac{9d}{f} \quad d = \frac{1}{8f}$$

$$\frac{101}{f} - \frac{94}{f} = \frac{d}{f} = 11, d$$

$$128, a_2, a_3, a_4, \dots, a_n = \frac{a}{f}$$

$$\frac{a_n}{a} = 9^k = \frac{128}{a} = \frac{f \times 128}{a} = 9^k$$

$$d \cdot \frac{1}{f} \Rightarrow a_1 = -12 + 10 = 1$$

$$t^r, t^v, t^q$$

$$t+rd, t+qd, t+rd$$

$$\frac{t+qd}{t+rd} = \frac{t+rd}{t+rd} = (t+qd)^r = t^r + r t^r d + r^2 t^r d^2 + r^3 t^r d^3$$

$$\cancel{t^r + 12 t^r d + 36 t^r d^2} = \cancel{t^r} + 1 \cdot t^r d + 14 t^r d^2$$

$$r^2 t^r d + r^3 t^r d^2 = 0$$

$$(a+d)(a+vd) = (a+rd) \rightarrow r a d - r d^2 = 0 \Rightarrow a = d$$

$$q = \frac{br}{b} = \frac{rd}{rd} = r \Rightarrow br = \frac{1}{r} \times r^2 = r^2 = 121$$

$$ra^q + aq^r = raq^r \xrightarrow{q \neq 0} q = r + \sqrt{r}, q = r - \sqrt{r}$$

$$a_r = \frac{a}{r} \quad a_n = \frac{1}{r} \quad a_{1r} = -1 + (a + \frac{a}{r})(r-1) = (r + \frac{1}{r})^r$$

$$\frac{-x}{r} - \frac{r1}{14} = 0 \Rightarrow \frac{-r1}{r} \quad \text{h.w.} \rightarrow -r - a - \frac{ra}{r} \Rightarrow a = \frac{a}{r}$$

$$t + t q^r + t q^q = v^r \quad t \left(\frac{1 + q^r + q^q}{1 + q^{1r}} \right) = v^r$$

$$t + t d + t q d = v^r$$

$$t(1 + 1 \cdot d) = v^r$$

$$t(1 + d + qd) = v^r$$

$$1 \cdot d$$

$$\frac{1 + q^{1r}}{1 + 1 \cdot d} = 1$$

$$1 + q^r + q^q = v^r \Rightarrow q = r$$

$$d = v$$