

$$d_a = 2 \rightarrow d_{a_1} = 4 \rightarrow t_n = a_n - 2 = 4n - 1$$

$$d_b = 2 \rightarrow t_1 = 2$$

$$b_{r_0} = 2(19) + 2 = 40$$

$$a_{r_0} = 2(19) \cdot 2 = 76$$

$$4n - 1 \leq 76$$

$$4n \leq 77 \rightarrow n \leq 19$$

6

$$a_p = V \rightarrow \text{sub}$$

$$d_p = 20$$

$$a_1 + V + 20 = 71 \rightarrow a_1 = 51$$

$$\frac{51 - V - 20}{-20} = \frac{V}{20} = \frac{1}{20} \cdot 71$$

7

$$a_p = 0 \rightarrow t_1 + d$$

$$a_p \cdot d = 20 \rightarrow 2t_1 + 2d = 20 \rightarrow$$

$$t_1 + d = 10 \rightarrow \begin{cases} 2t_1 + 2d = 20 \\ 2t_1 + 2d = 20 \end{cases}$$

$$\frac{2d = 20}{2} \rightarrow d = 10$$

$$t_1 = 0$$

$$t_{10} = 2(10) = 20$$

8

$$S_1 = 9S_3 \rightarrow S_1 \cdot 2 = 18S_3 \rightarrow 9a_1 + 18d = 18a_3 + 18d$$

$$9a_1 = 18a_3 \rightarrow a_1 = 2a_3$$

$$\frac{a_1}{a_3} = \frac{2a_3}{a_3} = 2$$

9

$$t_1 + t_v = t_p + t_f \rightarrow t_p = 22 \rightarrow 31 + 2d = 22 \rightarrow d = -5$$

$$a_p = 31 + (-5) = 26$$

$$\frac{26 - 31}{-5} = -1 \rightarrow -20 = -5k - 20 \rightarrow 0 = -5k$$

$$k = 0$$

10

$$t_n = \underbrace{\omega}_{\frac{1}{2}} \cdot \underbrace{9}_{\frac{1}{2}} \cdot \underbrace{12}_{\frac{1}{2}} \cdot \underbrace{17}_{\frac{1}{2}} \cdot \dots \quad d = 4 \quad t_1 = \omega \quad t_{(n-1)} + \omega = 1 + 4n \quad (الف)$$

$$t_0 = 4(10) + 1 = 41$$

$$t_n = \underbrace{4}_{\frac{1}{2}} \cdot \underbrace{9}_{\frac{1}{2}} \cdot \underbrace{12}_{\frac{1}{2}} \cdot \underbrace{17}_{\frac{1}{2}} \cdot \dots \quad d = 4 \quad t_1 = 4 \quad \frac{1}{\frac{1}{2}} \left(\frac{12 + (9 \cdot 4)}{2 + 4 \cdot 4} \right) = 16 \quad (الف)$$

$$a_{19} + a_{20} + a_{21} + a_{22} = \frac{1}{2} \rightarrow \frac{1}{2} (a_{19} + a_{22}) = \frac{1}{2} \left(\frac{12 + 14}{2 + 4} \right) = 16$$

$$a_{19} = 4 + 4(18) = 76$$

$$a_{22} = 4 + 4(21) = 88$$

$$1 + \sqrt{3}, 2, 3 + \sqrt{3} \rightarrow d = 1 - \sqrt{3} \quad t_n = (1 - \sqrt{3})(n - 1) + 1 + \sqrt{3}$$

$$t_{13} = (1 - \sqrt{3}) + 1 + \sqrt{3} = 2$$

$$t_{10} = 1 + \sqrt{3} + 2(1 - \sqrt{3}) = 2 - \sqrt{3}$$

$$t_{10} - t_{11} = \frac{2 - \sqrt{3} - 2 + \sqrt{3}}{1 - \sqrt{3}} = \frac{0}{1 - \sqrt{3}} = 0$$

$$d = 3\omega - 2\omega = \omega \quad \omega = 1 \rightarrow 3\omega - 2\omega = 1 \rightarrow \omega = 1$$

$$y = 2x + 1 \rightarrow \frac{2x + 1 + x}{2} = 1 \rightarrow 3x + 1 = 2 \rightarrow 3x = 1 \rightarrow x = \frac{1}{3} \rightarrow y = 2$$

$$\frac{4x + 2x - 2}{2} = 2x - 1 \rightarrow 4x - 2 = 2x - 1 \rightarrow 2x = 1 \rightarrow x = \frac{1}{2}$$

$$-3, 9, 2 \rightarrow d = 12 \quad t_1 = -3 \rightarrow t_n = -3 + (n - 1) \cdot 12 = 12n - 12$$

$$t_{10} = 12 \cdot 10 - 12 = 108$$