

$t_n = 0, 9, 13, 17, \dots$ $a_n \leq f_{n+1}$ $a_{10} = f(10) + 1 = f_1$	۱
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$t_n = 4, 10, 14, 18, \dots$ $s_{10} = \frac{n}{2} (2a_1 + (n-1)d)$ $s_{10} = \frac{10}{2} (12 + 9 \times 4) = 5(48) = 240$ $s_{10} = 240$	۲
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$1 + \sqrt{3}, 2, 3 - \sqrt{3}$ $d = \frac{a_m - a_n}{m - n} \rightarrow \frac{2 - 1 - \sqrt{3}}{2 - 1} = 1 - \sqrt{3}$ $a_n = a_1 + (n-1)d \rightarrow a_{3n} = 1 + \sqrt{3} + (n-1)(1 - \sqrt{3})$ $t_{40} - t_{32} = a + 32d - a + 32d = (2d) \rightarrow 2(1 - \sqrt{3}) = 2 - 2\sqrt{3}$	۳
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$3 \times 2 \times 10^x = 5^x \times 5^y \rightarrow 4 \times \cancel{5^x} = \cancel{5^x} \times 5^y$ $9 = 5^y \rightarrow 4 \leq xy \leq 6$	۴
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$2x - 4, 2x - 1, 4x \xrightarrow{\text{بازنویس}} 2(2x - 1) = 2x - 4 + 4x \Rightarrow x = \frac{1}{2}$ $\xrightarrow{\text{بازنویس}} -3, 0, 3$ $a_{24} = 6$	۵
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$$\begin{aligned}
 a_1 + a_r + a_p &= r1 \\
 a_1 + a_r + a_0 &= 100 \\
 \frac{a_r - a_r + a_1}{a} &= \frac{-1}{r} \\
 a + a + d + a + rd &= r1 \rightarrow ra + rd = r1 \rightarrow \boxed{a + d = r} \\
 a + a + rd + a + rd &= 100 \rightarrow ra + rd = 100 \rightarrow \boxed{a + rd = 100} \\
 \left\{ \begin{array}{l} a + rd = r \\ -a - d = -r \end{array} \right. \rightarrow \left\{ \begin{array}{l} d = r - a \\ -a - d = -r \end{array} \right\} \rightarrow \frac{a + rd - a - d + a}{a} = \frac{d + a = r - r}{-r}
 \end{aligned}$$

$$\begin{aligned}
 a_1 + a_r + a_p &= 10 \\
 a_r + a_0 &= 10 \\
 a + a + d + a + rd &= 10 \rightarrow ra + rd = 10 \rightarrow a + d = 5 \\
 a + rd + a + rd &= 10 \rightarrow ra + rd = 10 \rightarrow \frac{a + rd - a - d + a}{a} = \frac{d + a = 10 - 10}{-r} \\
 a_1 = a + rd &= r + 9(r) = r + 9r = \boxed{10}
 \end{aligned}$$

$$\begin{aligned}
 a_1 &= 11 \\
 a_v &= 50 \\
 d_a &= \frac{a_m - a_n}{m - n} = \frac{r2 - 11}{v - 1} = \boxed{r} \\
 a_n &= r n + r0 \\
 11, 12, 13, \dots & \\
 d_b &= \frac{b_2 - b_1}{2 - 1} = \boxed{-2} \\
 b_n &= b_1 + d(n-1) = b_n = r1 + (n-1)(-2) \\
 11 &= r1 + (n-1)(-2) \rightarrow -r2 = -2(n-1) \rightarrow 2n - 1 = \boxed{n-1}
 \end{aligned}$$

$$\begin{aligned}
 S_q &= r s_r \\
 S &= \frac{n}{r} (a_1 + a_q) \\
 S_q &= \frac{q}{r} (a_1 + a_q) \\
 S_r &= \frac{r}{r} (a_1 + a_q) \\
 \rightarrow \left[\frac{q}{r} (a_1 + a_q) \right] &= q \times \frac{r}{r} \left[\frac{r}{r} (a_1 + a_q) \right] \\
 \rightarrow \left[\frac{q}{r} (a_1 + a_q) \right] &= r \times \left[\frac{r}{r} (a_1 + a_q) \right] \rightarrow a_1 + rd = ra + rd \rightarrow \boxed{d = r}
 \end{aligned}$$

$$\frac{a_r}{a_v} \rightarrow \frac{a_1 + 19d}{a_1 + 8d} = \frac{a_1 + r1a_1}{a_1 + r1a_1} = \boxed{r}$$