

$$\begin{aligned}
 & \frac{x+r}{r^2x^2 - r^2x + r^2 - 1} \\
 & \frac{x+r}{(x-r)(x-r)(x-1)} \\
 & \frac{x+r}{r^2x^2 - r^2x - 1} \\
 & \frac{x+r}{(x-r)(x-r)(x+1)} \\
 & D_f = R - \left\{1, \frac{r}{r}, \frac{r}{r}\right\} \\
 & D_f = R - \left\{\frac{r}{r}, r-1\right\}
 \end{aligned}$$

$$\begin{aligned}
 & \frac{x+1}{x - \sqrt{r^2 - r^2x}} \\
 & x - \sqrt{r^2 - r^2x} \neq 0 \\
 & x \neq \sqrt{r^2 - r^2x} \\
 & x^2 \neq r^2 - r^2x \\
 & x^2 - r^2 + r^2x \neq 0 \\
 & (x+r)(x-1) \neq 0 \\
 & D_f = (-\infty, \frac{r}{r}] - \{1\}
 \end{aligned}$$

$$\begin{aligned}
 & \frac{x+r}{x - \sqrt{r^2x - r^2}} \\
 & x - \sqrt{r^2x - r^2} \neq 0 \\
 & x \neq \sqrt{r^2x - r^2} \\
 & x^2 \neq r^2x - r^2 \\
 & x^2 - r^2x + r^2 \neq 0 \\
 & (x-1)(x-r) \neq 0 \\
 & D_f = \left[\frac{r}{r} = 1\right) \cup (1, r) \cup (r, +\infty)
 \end{aligned}$$

$$\begin{aligned}
 & \frac{\sin x}{r \cos x - 1} \\
 & r \cos x - 1 \neq 0 \\
 & \cos x \neq \frac{1}{r} \\
 & D_f = R - \left\{rk\pi + \frac{\pi}{r}, rk\pi - \frac{\pi}{r}\right\} \\
 & \frac{\cos x + 1}{r \sin x + 1} \\
 & r \sin x + 1 \neq 0 \\
 & \sin x \neq -\frac{1}{r} \\
 & D_f = R - \left\{rk\pi - \frac{\pi}{r}, rk\pi - \frac{\pi}{r}\right\} \\
 & \frac{\tan x + r}{\cot x - 1} \\
 & \cot x - 1 \neq 0 \\
 & \cot x \neq 1 \\
 & D = R - \left\{\frac{\pi}{4} + rk\pi, rk\pi - \frac{\pi}{4}\right\} \\
 & \frac{\sin x}{\cos x} \neq \pm \frac{1}{r} \\
 & \sin x \neq \pm \frac{1}{r} \\
 & D_f = R - \left\{k\pi + \frac{\pi}{r}, k\pi - \frac{\pi}{r}\right\}
 \end{aligned}$$

$$\begin{aligned}
 & x^2 - 2x + 1 > 0 \\
 & (x-1)(x-1) > 0 \\
 & \frac{1}{1+\frac{1}{x}} - \frac{1}{1+\frac{1}{x}} \\
 & D_f = (-\infty, 1) \cup (1, +\infty)
 \end{aligned}$$

$$\begin{aligned}
 & x^2 - 4x + 4 < 0 \\
 & (x-1)(x-3) < 0 \\
 & \frac{1}{1+\frac{1}{x}} - \frac{1}{1+\frac{1}{x}} \\
 & D_f = (1, 3)
 \end{aligned}$$

$$\begin{aligned}
 & x^2 + 4x + 4 \geq 0 \\
 & (x+1)(x+3) \geq 0 \\
 & \frac{1}{1+\frac{1}{x}} - \frac{1}{1+\frac{1}{x}} \\
 & D_f = (-\infty, -1] \cup [-3, +\infty)
 \end{aligned}$$

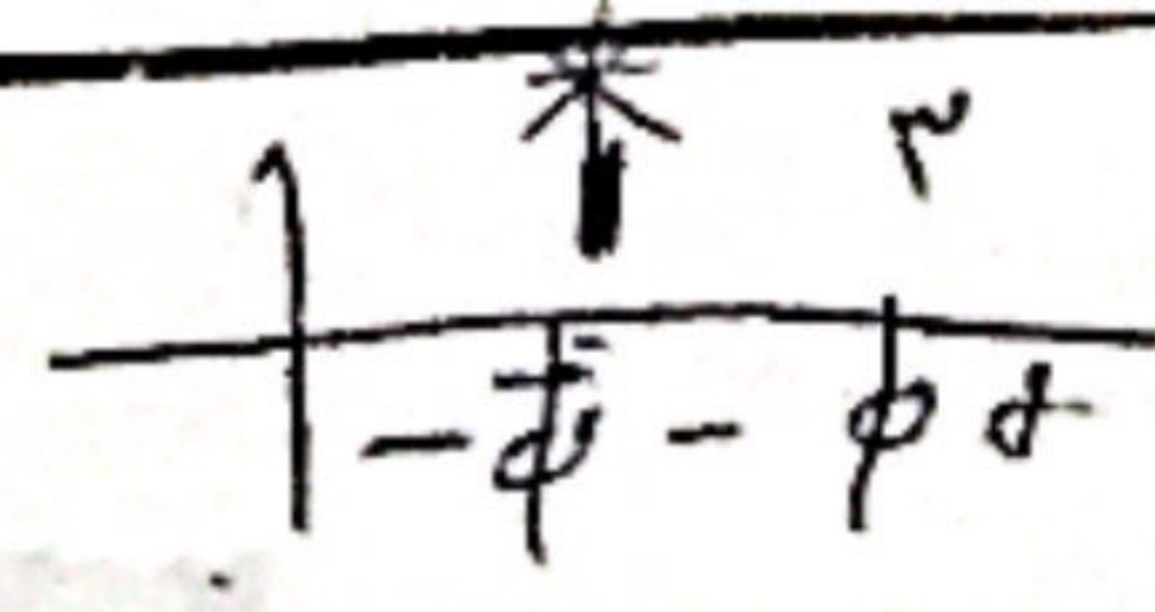
$$\begin{aligned}
 & x^2 - 4x + 4 \leq 0 \\
 & (x-1)(x-3) \leq 0 \\
 & \frac{1}{1+\frac{1}{x}} - \frac{1}{1+\frac{1}{x}} \\
 & D_f = [1, 3]
 \end{aligned}$$

$$\begin{aligned}
 & \frac{x^2 - x + 1}{x - 1} < 0 \\
 & \frac{(x-1)(x-1)}{x-1} < 0 \\
 & \frac{1}{1+\frac{1}{x}} - \frac{1}{1+\frac{1}{x}} \\
 & D_f = (-\infty, 1) \cup (1, +\infty)
 \end{aligned}$$

$$\begin{aligned}
 & \frac{x^2 - 1}{x^2 - x + 1} \geq 0 \\
 & \frac{(x-1)(x+1)}{(x-1)(x-1)} \geq 0 \\
 & \frac{1}{1+\frac{1}{x}} - \frac{1}{1+\frac{1}{x}} \\
 & D_f = (-\infty, -1] \cup (1, +\infty)
 \end{aligned}$$

$$y = \sqrt{\frac{x^2 - 4x + 3}{x^2 - 1}} \Rightarrow y = \sqrt{\frac{(x-1)(x-3)}{x^2 - 1}}$$

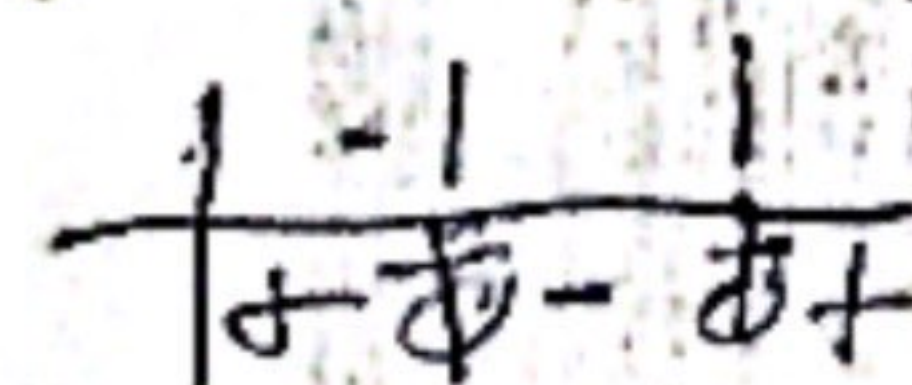
$$\frac{(x-1)(x-3)}{x^2 - 1} \geq 0$$



$$D_f = [-3, +\infty)$$

$$y = \sqrt{\frac{x^2 - 4x + 3}{x^2 - 1}} \Rightarrow y = \frac{(x-1)(x-3)}{(x-1)(x+1)}$$

$$(x-1)(x+1) \neq 0$$

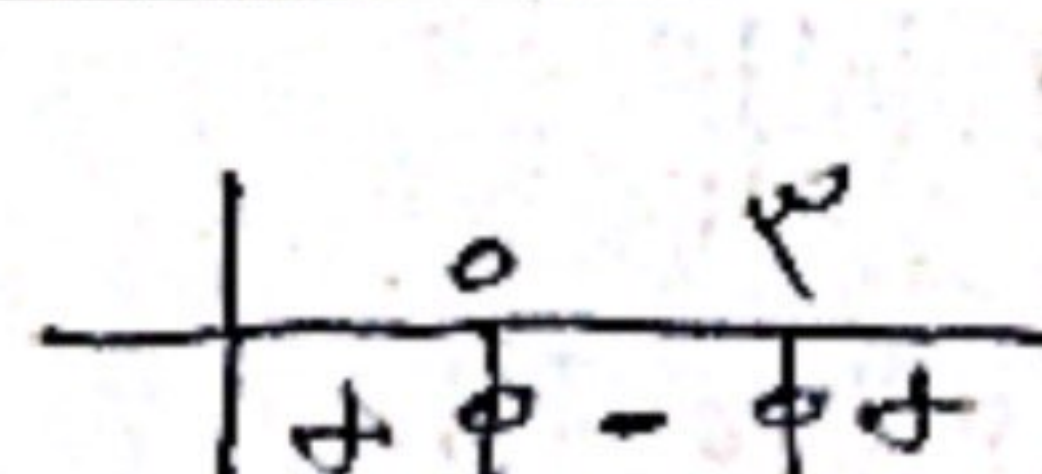


$$D_f = \mathbb{R} - \{-1, 1\}$$

$$y = \log(x^2 - 4x)$$

$$x^2 - 4x > 0$$

$$x(x-4) > 0$$



$$D_f = (-\infty, 0) \cup (4, +\infty)$$

$$y = \log \frac{14-x^2}{|x|-2}$$

$$14-x^2 > 0$$

$$14 > x^2$$

$$|x| < \sqrt{14}$$

$$|x|-2 > 0$$

$$|x| > 2$$

$$x < -2 \text{ or } x > 2$$

$$|x|-2 \neq 1$$

$$|x| \neq 3$$

$$x \neq -3 \text{ or } x \neq 3$$

$$D_f = ((-\sqrt{14}, -2) \cup (2, \sqrt{14})) - \{-3, 3\}$$

$$y = \log \frac{x^2 - 4x + 1}{x-3}$$

$$1 = x$$

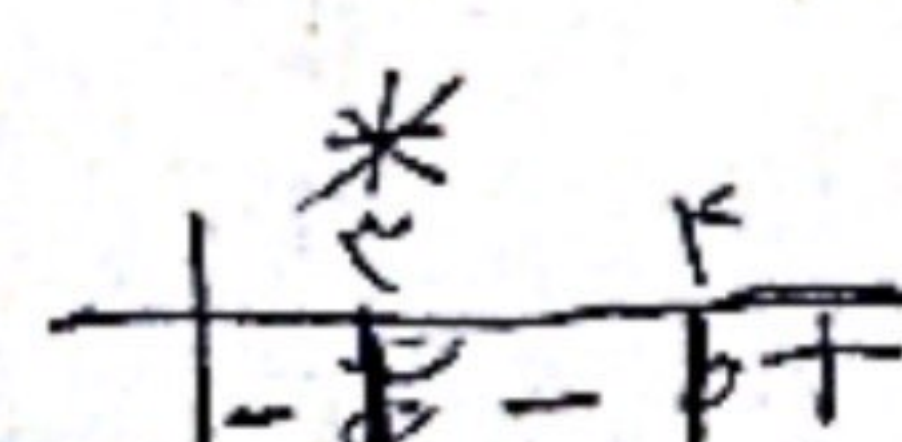
$$\frac{x^2 - 4x + 1}{x-3} > 0$$

$$10 - 4x > 0$$

$$10 > 4x$$

$$10 \neq 4x$$

$$\frac{(x-2)(x-4)}{x-3}$$



$$D_f = (x < 10) - \{9\}$$

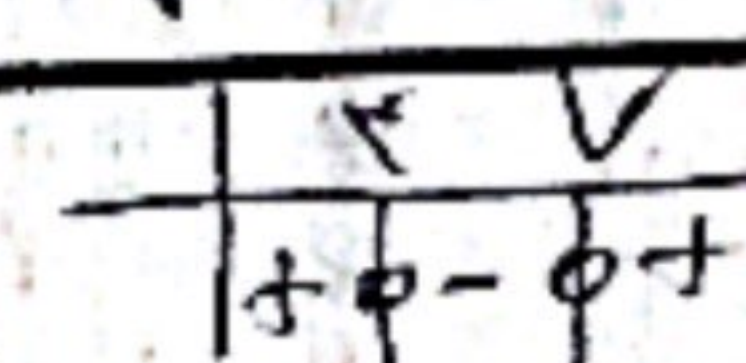
$$y = \sqrt{x^2 - 11x + 18} + \log \sqrt{4-x^2}$$

$$(x-4)(x-5) \geq 0$$

$$\sqrt{4-x^2} > 0$$

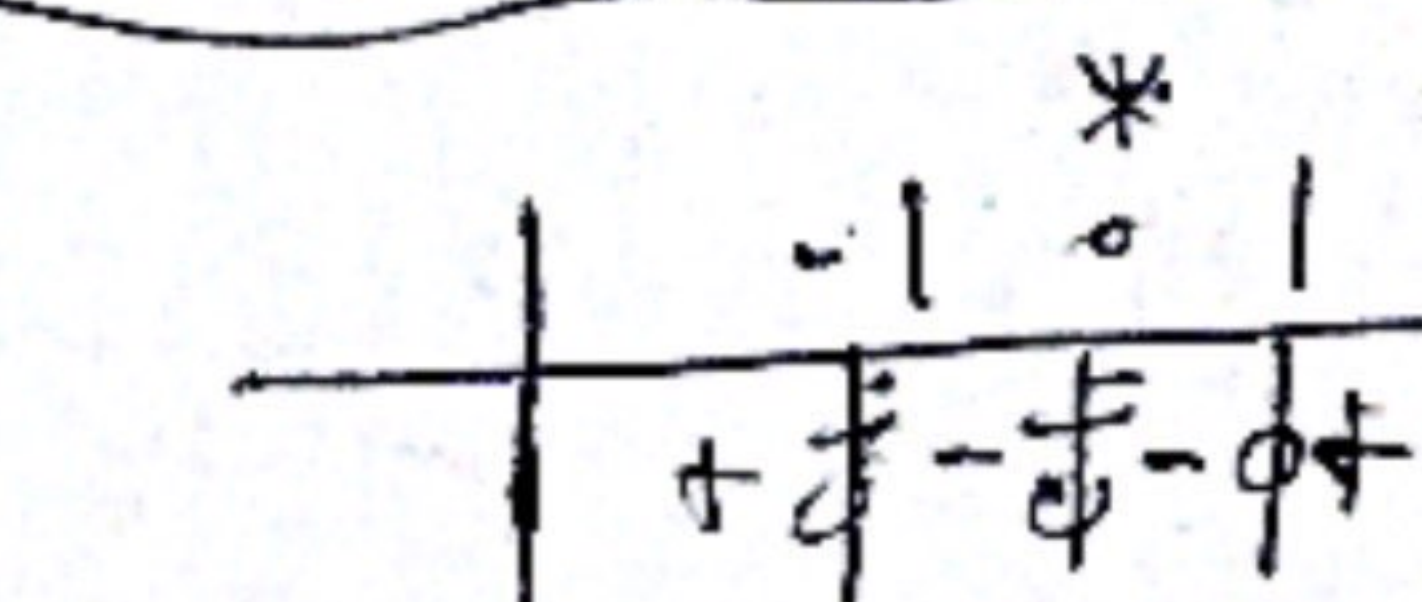
$$4-x^2 > 0$$

$$2 > |x|$$



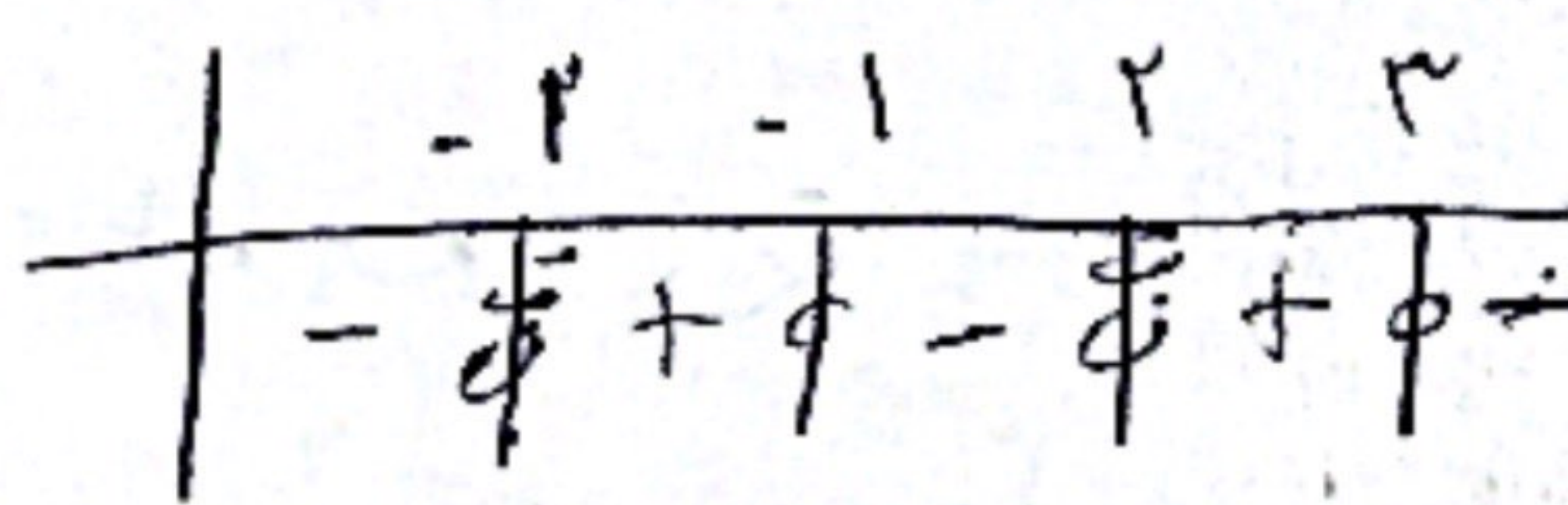
$$D_f = (-\infty, 4] \cup [5, +\infty)$$

|                             |    |   |   |
|-----------------------------|----|---|---|
| $\frac{x^2 - 9x}{x^2 + 9x}$ | -1 | 0 | 1 |
| $\frac{x^2 - 9x}{x^2 + 9x}$ | +  | + | - |
| $\frac{x^2 + 9x}{x^2 + 9x}$ | +  | - | + |
| $\frac{x^2 + 9x}{x^2 + 9x}$ | +  | - | + |

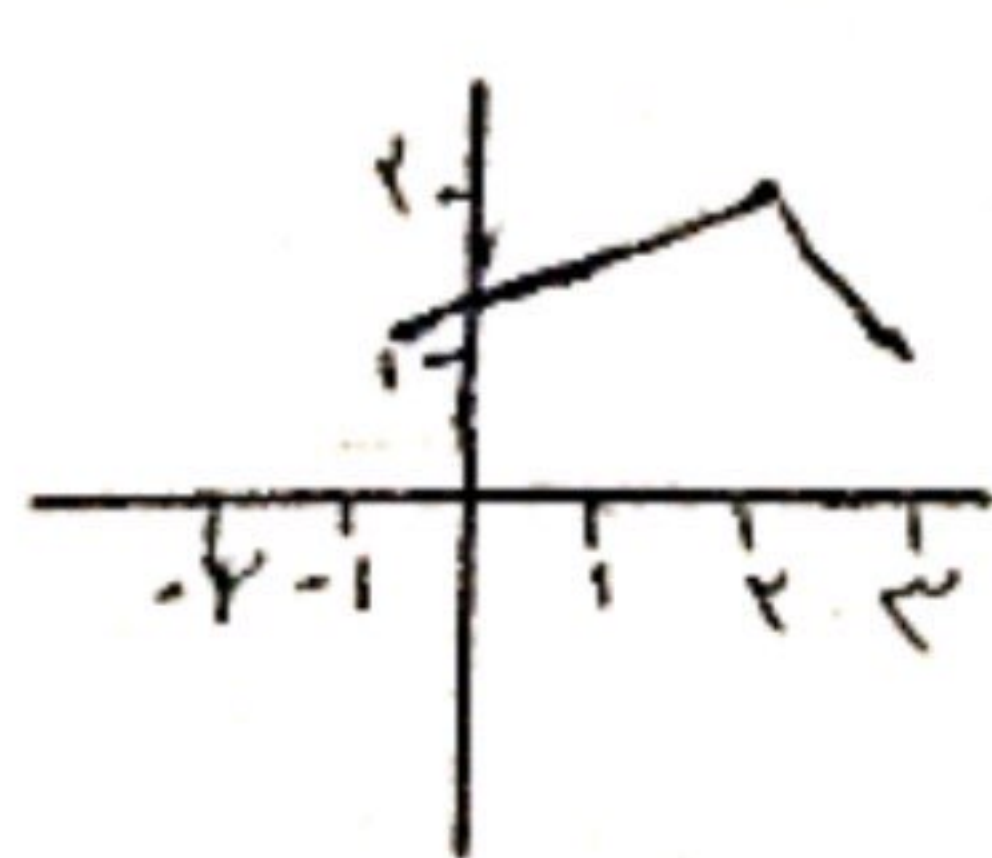


$$D_f = (0, 4] - \{1\}$$

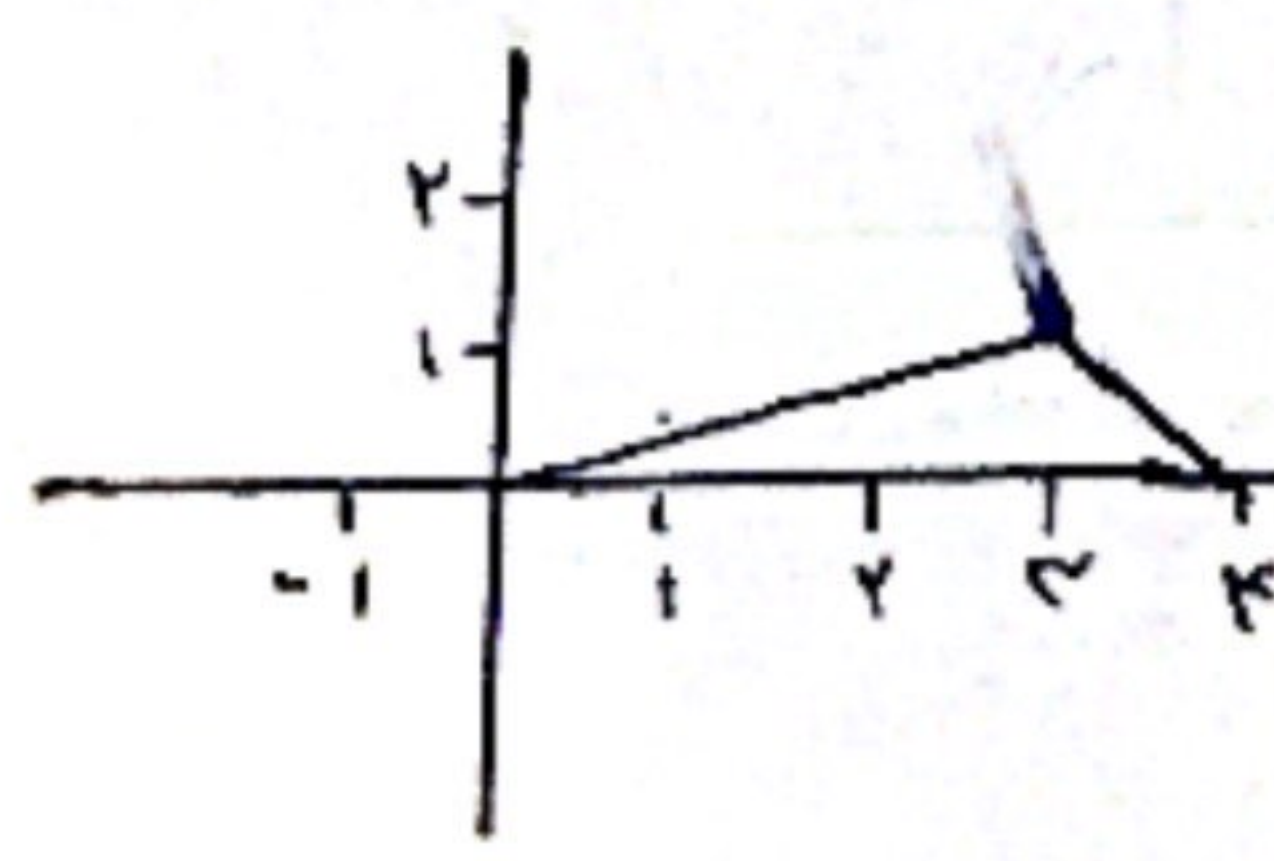
$$\sqrt{\frac{x-1}{x}} \Rightarrow$$



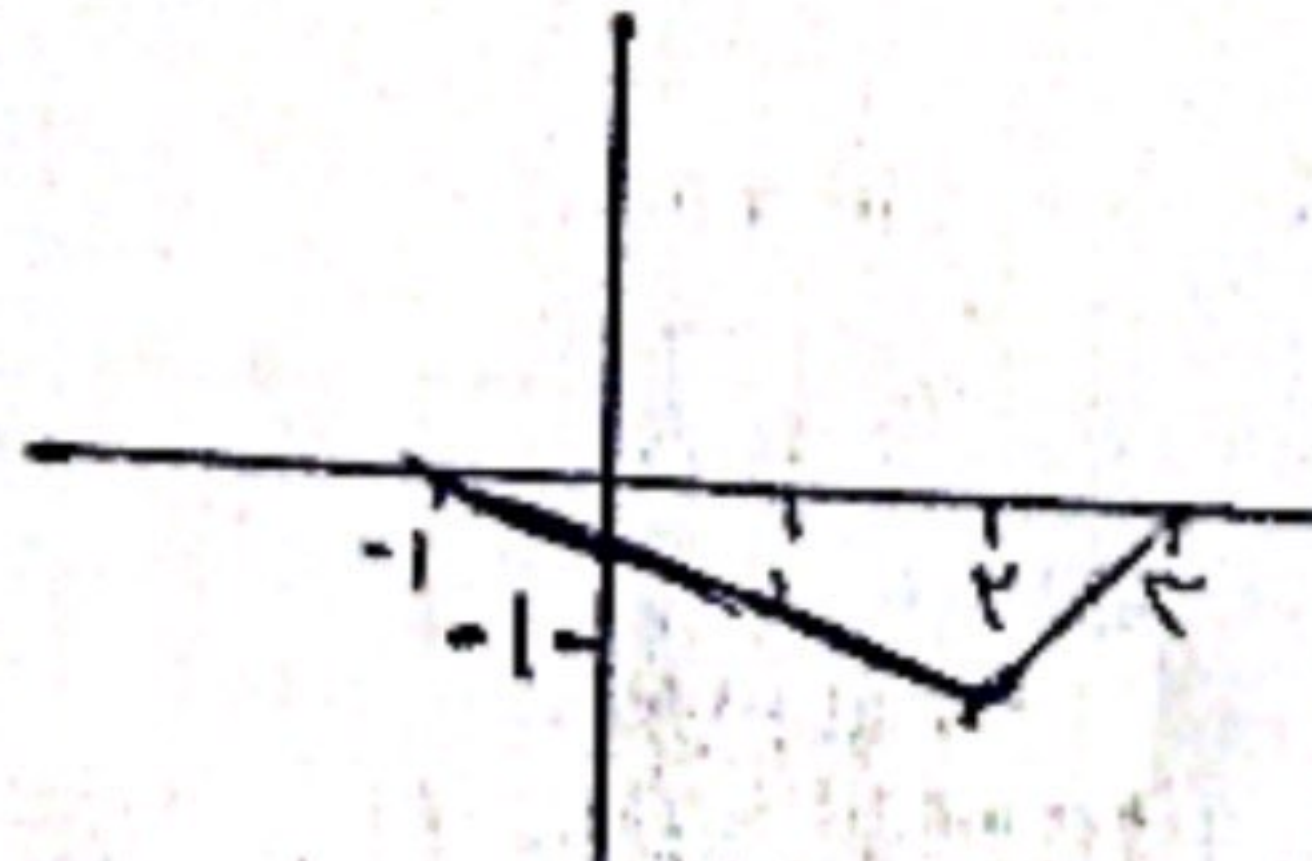
$$D_f = (-2, 1] \cup (2, 3]$$



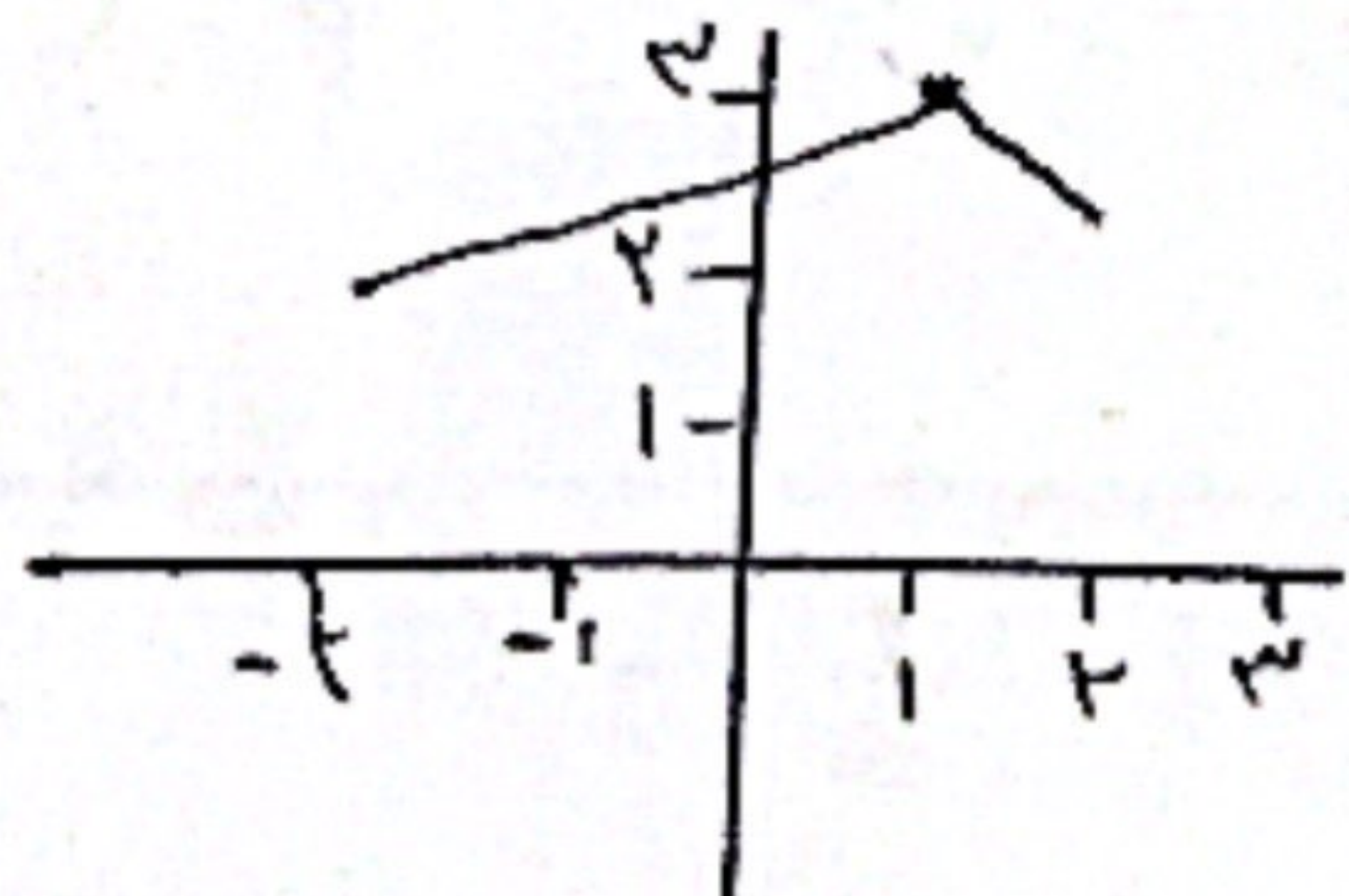
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