

الف)  $\cos(x) + 1 \neq 0 \Rightarrow \cos(x) \neq -1 \Rightarrow \cos(x) \neq \frac{-1}{1}$   
 $\Rightarrow D_f = \mathbb{R} - \left\{ 2k\pi + \frac{\pi}{3}, 2k\pi + \frac{5\pi}{3} \right\}$   
 ب)  $\cos(x) - 1 \neq 0 \Rightarrow \cos(x) \neq 1 \Rightarrow D_f = \mathbb{R} - \{ 2k\pi \}$

الف)  $\tan(x) + 1 \neq 0 \Rightarrow \tan(x) \neq -1, \tan(x) \neq \text{undefined} \Rightarrow D_f = \mathbb{R} - \left\{ k\pi + \frac{\pi}{4}, k\pi + \frac{5\pi}{4} \right\}$   
 ب)  $\cot(x) - 1 \neq 0 \Rightarrow \cot(x) \neq 1, \cot(x) \neq \text{undefined} \Rightarrow D_f = \mathbb{R} - \left\{ k\pi, k\pi + \frac{\pi}{4} \right\}$

الف)  $-1 < 2^x - 1 < 1 \Rightarrow 1 < 2^x < 2 \Rightarrow 1 < x < \sqrt{1} \text{ یا } x > -\sqrt{1}$  ①  
 $\Rightarrow D_f = [-\sqrt{1}, -1] \cup [1, \sqrt{1}]$   
 ب)  $-1 < \sqrt{x} - 1 < 1 \Rightarrow 1 < \sqrt{x} < 2 \Rightarrow 1 < x < 4$   
 $\Rightarrow D_f = [1, 4]$

الف)  $-1 < |x| - 1 < 1 \Rightarrow 1 < |x| < 2 \Rightarrow D_f = [-2, -1] \cup [1, 2]$   
 ب)  $-1 < x(x+3) < 0 \Rightarrow -1 < x < 0 \text{ و } (x+1)(x+2) > 0$  ①  
 $\Rightarrow x < -2 \text{ و } x > -1$  ②  $\Rightarrow D_f = [-2, -1] \cup [-1, 0]$

ب)  $1 - |x| > 0 \Rightarrow 1 > |x| \Rightarrow D_f = (-1, 1)$   
 الف)  $x^2 - 1 > 0 \Rightarrow x^2 > 1 \Rightarrow x > 1 \text{ یا } x < -1$  ①  
 $\Rightarrow D_f = (-\infty, -1) \cup (1, +\infty)$  ②

الف)  $\alpha - n > 0 \Rightarrow \alpha > n, n - \beta > 0 \Rightarrow n > \beta$

ب)  $n - \beta \neq 1 \Rightarrow n \neq \beta \Rightarrow D_f = (\beta, \alpha) - \{ \beta \}$

ج)  $|n - 1| > 0 \Rightarrow n > 1 \Rightarrow n > 1 \wedge n < -1, n + \beta > 0 \Rightarrow n > -\beta$   
 $n + \beta \neq 1 \Rightarrow n \neq -\beta \Rightarrow D_f = [-\beta, -1) \cup (1 + \infty)$

الف)  $\frac{(n - \beta)(n - 1)}{n - \beta} > 0 \Rightarrow \frac{1}{-1} + \frac{1}{\beta} + \frac{1}{\beta} = \frac{2}{\beta} - \frac{1}{1}$

$\Rightarrow D_f = (1, \beta) \cup (\beta, +\infty) - \{1, \beta\}$

ب)  $\frac{n + \beta}{n - \beta} > 0 \Rightarrow \frac{-\beta}{1} + \frac{\beta}{\beta} + \frac{1}{\beta} = \frac{1}{\beta} \Rightarrow (\frac{\infty}{\beta} - \beta) \cup (\beta, +\infty)$

ج)  $n + \alpha > 0 \Rightarrow n > -\alpha, n + \alpha \neq 1 \Rightarrow n \neq -\beta \Rightarrow D_f = (-\alpha, -\beta) \cup (\beta, +\infty) - \{-\beta\}$

الف)  $n - \beta > 0 \Rightarrow n > \beta$

$\beta - \log_2(n - \beta) > 0 \Rightarrow \beta > \log_2(n - \beta) \Rightarrow 1 > \log_2$

$\Rightarrow D_f = (\beta, 1]$

ب)  $n > 0, \beta \log_2 n - 1 > 0 \Rightarrow \log_2 n > \frac{1}{\beta} \Rightarrow n > \sqrt{\beta}$

$\Rightarrow D_f = (\sqrt{\beta}, +\infty)$

الف)  $r^n \neq -1 \Rightarrow D_f = \mathbb{R}$

ب)  $r^n \neq \beta$

$\Rightarrow \log_2 r^n \neq \beta$

$\Rightarrow D_f = \mathbb{R} - \{n | n \in \mathbb{R}, \log_2 r^n \neq \beta\}$

ب)  $r^n \neq 1 \Rightarrow D_f = \mathbb{R} - \{0\}$

ج)  $r^n \neq \beta \Rightarrow D_f = \mathbb{R} - \{1\}$

الف)  $r^{n+1} = k \Rightarrow n = \frac{k-1}{r} \Rightarrow D_f = \{n | n = \frac{k-1}{r}, k \in \mathbb{N}\}$

ب)  $\frac{r^n - \beta}{r^n - \alpha} = k \Rightarrow r^n k - \alpha k = r^n - \beta$

$\Rightarrow r^n k - r^n = \alpha k - \beta \Rightarrow n = \frac{\alpha k - \beta}{r k - r}$

$\Rightarrow D_f = \{n | n = \frac{\alpha k - \beta}{r k - r}, k = 1, 2, \dots, r k - \beta\}$