

الف) $\tan \frac{11\pi}{8} + \sin \frac{15\pi}{8} \cdot \cos \frac{13\pi}{8}$

$$\frac{11\pi}{8} = 2\pi + \frac{5\pi}{8} \Rightarrow \tan\left(\frac{11\pi}{8}\right) \Rightarrow \tan\left(\frac{5\pi}{8}\right) = -1 \quad -\frac{\sqrt{2}}{2} \times -\frac{\sqrt{2}}{2} = \frac{1}{2} + (1) = \left(-\frac{1}{2}\right)$$

$$\sin\left(\frac{15\pi}{8}\right) \Rightarrow \sin\left(\frac{7\pi}{8}\right) = -\frac{\sqrt{2}}{2}, \quad \cos\left(\frac{13\pi}{8}\right) \Rightarrow \cos\left(\frac{5\pi}{8}\right) = -\frac{\sqrt{2}}{2}$$

ب) $\tan \frac{17\pi}{8} \times \sin \frac{11\pi}{8} + \cos \frac{10\pi}{8}$

$$\tan \frac{17\pi}{8} \Rightarrow \tan \frac{9\pi}{8} = -\frac{\sqrt{2}}{2}, \quad \sin \frac{11\pi}{8} \Rightarrow \sin \frac{5\pi}{8} = -\frac{\sqrt{2}}{2} \quad \left. \begin{array}{l} -\frac{\sqrt{2}}{2} \times -\frac{\sqrt{2}}{2} = \frac{1}{2} + (-\frac{1}{2}) = 0 \\ \cos \frac{10\pi}{8} \Rightarrow \cos \frac{5\pi}{4} = -\frac{1}{2} \end{array} \right\}$$

$\cot x = f \quad \frac{\cos x}{\sin x} = f \Rightarrow \cos x = fK, \sin x = K$

$$\frac{3\cos x - \sin x}{\cos x + \sin x} = \frac{3(fK) - K}{fK + K} = \frac{11K}{8K} = \left(\frac{11}{8}\right)$$

$\sin \alpha = 2\cos \alpha \Rightarrow \sin \alpha = 2c, \cos \alpha = c$

$$\sin^2 \alpha + \cos^2 \alpha = 1 \Rightarrow (2c)^2 + c^2 = 1 \Rightarrow 4c^2 + c^2 = 1 \Rightarrow 5c^2 = 1 \Rightarrow c^2 = \frac{1}{5}$$

$$\Rightarrow c = \pm \frac{1}{\sqrt{5}}, \quad \cos \alpha < 0 \Rightarrow \cos \alpha = \left(-\frac{1}{\sqrt{5}}\right)$$

$\cos\left(\frac{11\pi}{8} + \alpha\right) = \cos\left(\frac{9\pi}{8} + \alpha\right) = \cos \frac{9\pi}{8} \cos \alpha - \sin \frac{9\pi}{8} \sin \alpha$

$$\cos\left(\frac{11\pi}{8} + \alpha\right) = -\frac{\sqrt{2}}{2} \cos \alpha - \frac{\sqrt{2}}{2} \sin \alpha = -\frac{\sqrt{2}}{2} (\cos \alpha + \sin \alpha)$$

$$\cos \alpha + \sin \alpha = -\frac{\sqrt{2}}{10} + \frac{\sqrt{2}}{10} = -\frac{4\sqrt{2}}{10} = -\frac{2\sqrt{2}}{5} \Rightarrow \cos\left(\frac{11\pi}{8} + \alpha\right) = -\frac{\sqrt{2}}{2} \left(-\frac{2\sqrt{2}}{5}\right) = \left(\frac{2}{5}\right)$$

$\sin\left(\frac{13\pi}{8} + \alpha\right) \Rightarrow \sin\left(2\pi + \frac{\pi}{8} + \alpha\right) \Rightarrow \sin\left(\alpha + \frac{\pi}{8}\right)$

$$\sin \alpha = \frac{1}{\sqrt{1+2}} = \frac{1}{\sqrt{3}} = \frac{1}{\sqrt{3}}, \quad \cos \alpha = \frac{1}{\sqrt{3}} \Rightarrow \sin\left(\alpha + \frac{\pi}{8}\right) = \sin \alpha \cos \frac{\pi}{8} + \cos \alpha \sin \frac{\pi}{8}$$

$$\sin \frac{\pi}{8} = \cos \frac{\pi}{8} = \frac{\sqrt{2}}{2} \Rightarrow \sin\left(\alpha + \frac{\pi}{8}\right) = \frac{\sqrt{2}}{2} (\sin \alpha + \cos \alpha) = \sin\left(\alpha + \frac{\pi}{8}\right) = \frac{\sqrt{2}}{2} \times \frac{1}{\sqrt{3}} = \left(\frac{1}{\sqrt{6}}\right)$$

$\sin\left(\frac{13\pi}{8} + \alpha\right) = \left(-\frac{1}{\sqrt{6}}\right)$

$2\sin^2 x + \cos^2 x = \frac{5}{6} \Rightarrow \cos^2 x = 1 - \sin^2 x \Rightarrow 2\sin^2 x + (1 - \sin^2 x) = \frac{5}{6}$

$$\sin^2 x + 1 = \frac{5}{6} \Rightarrow \sin^2 x = \frac{5}{6} - 1 = -\frac{1}{6} \Rightarrow \sin^2 x = \frac{1}{6} \Rightarrow \cos^2 x = 1 - \sin^2 x = 1 - \frac{1}{6} = \frac{5}{6}$$

$$\tan^2 x = \frac{\sin^2 x}{\cos^2 x} \Rightarrow \frac{\frac{1}{6}}{\frac{5}{6}} = \left(\frac{1}{5}\right)$$

$$a = \sqrt{13}, b = 4, s = f_1 d$$

$$s = \frac{1}{f} ab \sin \alpha \Rightarrow f_1 d = \frac{1}{f} (\sqrt{13} \times 4) \sin \alpha = 4\sqrt{13} \sin \alpha = f_1 d$$

$$\sin \alpha = \frac{f_1 d}{4\sqrt{13}} = \frac{\sqrt{13}}{4} \Rightarrow \sin \alpha = \frac{\sqrt{13}}{4} \Rightarrow \alpha = \frac{\pi}{4} \text{ or } \alpha = \pi - \frac{\pi}{4} = \frac{3\pi}{4}$$

$$\alpha_{\min} = \frac{\pi}{4}, \alpha_{\max} = \frac{3\pi}{4} \Rightarrow \frac{\alpha_{\max}}{\alpha_{\min}} = \frac{\frac{3\pi}{4}}{\frac{\pi}{4}} = 3$$

$$\left. \begin{array}{l} s = \Delta f \\ \frac{a}{b} = \frac{r}{r} \\ \alpha = 120^\circ \end{array} \right\} \begin{array}{l} a = rx \\ b = rx \\ \Rightarrow s = ab \sin \alpha \Rightarrow \Delta f = (rx)(rx) \times \frac{1}{r} \Rightarrow x^2 = 11 \\ \Rightarrow x = \sqrt{11} \\ \alpha = rx = 4\sqrt{2}, b = rx = 9\sqrt{2} \\ \Rightarrow x = 3\sqrt{2} \end{array}$$

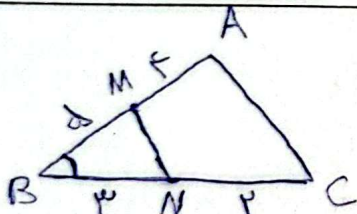
$$P = r(a+b) = r(4\sqrt{2} + 9\sqrt{2}) = r(13\sqrt{2}) = 13\sqrt{2}r$$

$$\left. \begin{array}{l} S_{ABC} = \frac{1}{2} \times \Delta \times \Delta \times \sin \hat{A} = 14\Delta \sin \hat{A} \\ S_{ADE} = \frac{1}{2} \times \Delta \times \Delta \times \sin \hat{A} = 1\Delta \sin \hat{A} \end{array} \right\} \Delta \sin \hat{A} = 14\Delta$$

$$\sin \hat{A} = \frac{14\Delta}{\Delta} = 14$$

$$\hat{A} = 90^\circ$$

$$\tan 30^\circ = \frac{1}{\sqrt{3}} = \frac{r}{\sqrt{13}} \Rightarrow \frac{1}{\sqrt{3}} = \frac{r}{\sqrt{13}}$$



$$\overline{BN} = \overline{NC} \Rightarrow \frac{\overline{BN}}{\overline{NC}} = \frac{r}{r} \Rightarrow \overline{BN} = r, \overline{NC} = r$$

$$S_{ABC} = 3 S_{BMN}$$

$$S_{ABC} = \frac{1}{2} ab \times bc \times \sin \hat{B}$$

$$S_{ABC} = \frac{1}{2} \times \Delta \times AB \Rightarrow \Delta AB$$

$$S_{BMN} = \frac{1}{2} \times r \times BM \Rightarrow \Delta BM \Rightarrow \frac{BM}{AB} = \frac{\Delta}{\Delta}$$

$$\frac{1}{\cos \alpha} - \tan \alpha = \frac{1 + \sin \alpha}{\cos \alpha} \Rightarrow -\tan \alpha = \frac{\sin \alpha}{\cos \alpha}$$

$$\left\{ \begin{array}{l} \cos \alpha > 0 \Rightarrow -\tan \alpha = \frac{\sin \alpha}{\cos \alpha} \Rightarrow -\sin \alpha / \cos \alpha = \sin \alpha / \cos \alpha \Rightarrow \sin \alpha = 0 \\ \cos \alpha < 0 \Rightarrow -\tan \alpha = \frac{\sin \alpha}{-\cos \alpha} \Rightarrow -\tan \alpha = -\tan \alpha \Rightarrow \sin \alpha = 0 \end{array} \right.$$

$$\cos \alpha > 0 \Rightarrow \sin \alpha = 0 \Rightarrow \alpha = 0^\circ, 180^\circ$$

$$\cos \alpha < 0 \Rightarrow 90^\circ < \alpha < 270^\circ$$

$$\frac{|\sin \alpha|}{\cos \alpha} = -\frac{1}{\cot \alpha} \Rightarrow \cot \alpha = \frac{\cos \alpha}{\sin \alpha} \Rightarrow \frac{1}{\cot \alpha} = \frac{\sin \alpha}{\cos \alpha} \Rightarrow \frac{|\sin \alpha|}{\cos \alpha} = \frac{-\sin \alpha}{\cos \alpha}$$

$$|\sin \alpha| = -\sin \alpha \Rightarrow \sin \alpha \leq 0$$