

الف) $x^2 = y + 5$ $x = \pm \sqrt{y + 5}$ $y + 5 \geq 0$ $y \geq -5$ $R_f = [-5, +\infty)$

ب) $x^2 = y - 1$ $x = \pm \sqrt{y - 1}$ $R_f = \mathbb{R}$

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الف) $y = (x - 2)^2 + 2$ $(x - 2)^2 = y - 2$ $x = \pm \sqrt{y - 2} + 2$ $R_f = [2, +\infty)$

ب) $y = x^2 - 5$ $x + 1 + \frac{y}{x} - \frac{y}{x} = y = (x - \frac{5}{x})^2 - \frac{y}{x}$ $(x - \frac{5}{x})^2 = y + \frac{y}{x}$

$x = \pm \sqrt{y + \frac{y}{x}} + \frac{5}{x} \Rightarrow y \geq -\frac{y}{x}$ $R_f = [-\frac{y}{x}, +\infty)$

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الف) $x^2 = -(\frac{-2y - 3}{-y - 1})$ $x = \pm \sqrt{\frac{2y + 3}{-y - 1}}$ $\frac{-2y - 3}{-y - 1} \geq 0$ $R_f = (-\infty, -\frac{3}{2}] \cup (-1, +\infty)$

ب) $|x| = -(\frac{-2y - 3}{-y - 1})$ $|x| = \frac{2y + 3}{-y - 1}$ $\frac{-2y - 3}{-y - 1} \geq 0$ $R_f = (-\infty, -\frac{3}{2}] \cup (-1, +\infty)$

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$yx^2 - 4yx = 1$ $yx^2 - 4yx - 1 = 0$ $14y^2 + 4y + y(4y + 1)$

$x = \frac{4y \pm \sqrt{(-4y)^2 - (-4y)}}{2y} = \frac{4y \pm \sqrt{16y^2 + 4y}}{2y}$ $2y \Rightarrow y \neq 0$

$\frac{-1}{4y} \geq 0$

$R_f = (-\infty, 0) \cup [-\frac{1}{4}, +\infty)$

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الف) $\frac{b}{ra} = 3$ $9 - 18 + 2 = -7$ $\min \left| \frac{r}{-7} \right|$ $R_f = [-7, +\infty)$

ب) $\frac{b}{ra} = \frac{-r}{-r} = 2$ $-r + 18 + 2 = 4$ $\max \left| \frac{r}{4} \right|$ $R_f = (-\infty, 4]$

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الف) $\min \left| \frac{x}{-x} \right|$ $R = \sqrt{[-x, +\infty)} \Rightarrow R_f = [0, +\infty)$

ب) $\frac{b}{x} = \frac{-x}{-x} = 1$ $-x + \infty + 1 = 1$ $R = \sqrt{[-\infty, 1]}$ $R_f = [0, \sqrt{1}]$

الف) $R_f = \mathbb{R}$

ب) $R = \sqrt{\mathbb{R}} \Rightarrow R_f = [0, +\infty)$

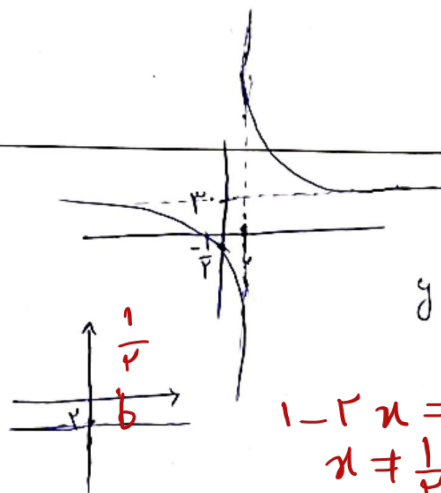
الف) $\frac{a}{c} = 2$ $R = \mathbb{R} - \{2\}$

ب) $\frac{a}{c} = 2$ $R = \sqrt{\mathbb{R} - \{2\}} = [0, +\infty) - \{2\}$

مجانبة $\frac{a}{c} = 2$ $\rightarrow$ $\frac{a}{c} = 2$

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ب) $y = \frac{2x-2}{-(2x-1)} \Rightarrow y = -2$



$1-2x \neq 0$
 $x \neq \frac{1}{2}$

$x=0 \rightarrow$
 $y = \frac{2x+1}{x-2} = \frac{1}{-2}$

1/2

الف) $\cos^n x > 0$

$R_f = [1, +\infty)$

ب) $y = \sqrt[n]{x + \frac{1}{n}}$

$R_f = (-\infty, \sqrt[n]{-1}] \cup [\sqrt[n]{1}, +\infty)$

$x > 0 \rightarrow [\sqrt[n]{1}, +\infty)$

$x < 0 \rightarrow (-\infty, \sqrt[n]{-1}]$

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