

الف) $x' = y + 5 \xrightarrow{\sqrt{\quad}} x = \pm \sqrt{y+5} \leadsto y+5 \geq 0 \rightarrow y \geq -5 \quad \text{یا} \quad R_f = [-5, +\infty)$

ب) $x'' = y - 1 \rightarrow x = \sqrt[3]{y-1} \leadsto R_f = R$

درج اولی ← بیرون گشتن x

الف) $y = x^2 - 4x + 4 \xrightarrow{a>0} \Rightarrow y = x^2 - 4x + 4 \rightarrow R_f = [2, +\infty)$
 $\hookrightarrow x = \frac{-b}{2a} = \frac{4}{2} = 2$

ب) $y = x^2 - 5x + 1$

$\hookrightarrow a > 0 \leadsto x = -\frac{-5}{2} = \frac{5}{2} \leadsto y = (\frac{5}{2})^2 - (5 \times \frac{5}{2}) + 1 = \frac{25}{4} - \frac{25}{2} + 1 = \frac{25 - 50 + 4}{4} = \frac{-21}{4}$

$a > 0$ من
 $R_f = [\frac{-21}{4}, +\infty)$

الف) $y x' - 2y = x^2 + 3 \rightarrow y x' - x^2 = 2y + 3$

$x'(y-1) = 2y+3 \leadsto x' = \frac{2y+3}{y-1} \Rightarrow x = \pm \sqrt{\frac{2y+3}{y-1}}$

ب) $y|x| - 4y = 2|x| + 1 \rightarrow y|x| - 2|x| = 1 + 4y$
 $|x|(y-2) = 1 + 4y$

$\frac{1+4y}{y-2} = |x|$
 $\frac{1}{y-2} = \frac{1}{|x|}$

$\frac{-\frac{1}{2}}{1} = \frac{1}{|x|}$
 $|x| = -\frac{1}{2}$

$R_f = (-\infty, -\frac{1}{2}] \cup (2, +\infty)$

$y = \frac{1}{x^2 - 4x} \Rightarrow y x^2 - 4x y = 1 \leadsto y x^2 - 4x y - 1 = 0 \leadsto x = \frac{4y \pm \sqrt{16y^2 + 4y}}{2}$

$\Rightarrow 4y \pm \sqrt{16y^2 + 4y} \leadsto 4y \pm \sqrt{4y(4y+1)}$
 $4y(4y+1) \geq 0 \rightarrow \frac{1}{4} \quad \frac{0}{+ \quad - \quad +} \leadsto R_f = (-\infty, -\frac{1}{4}] \cup (0, +\infty)$

الف) $x = \frac{-b}{2a} = -\frac{-4}{2} = 2 \leadsto 9 - 18 + 2 = -7 = y$



$R_f = [-7, +\infty)$

$a > 0 \rightarrow \min$

$\Rightarrow a < 0 \rightarrow \max$

$x = \frac{-b}{2a} = \frac{-4}{-2} = 2 \leadsto -4 + 8 + 2 = 6 \quad R_f = (-\infty, 6]$



الف) $y = \sqrt{x^2 - 4x + 2}$ $a > 0$ $\begin{cases} -\frac{b}{2a} = \frac{4}{2} = 2 \\ y = 4 - 18 + 2 = -12 \end{cases} \Rightarrow R_f = \sqrt{[-12, +\infty)} = [0, +\infty)$

ب) $y = \sqrt{-x^2 + 4x + 10}$ $a < 0$ $\begin{cases} -\frac{b}{2a} = \frac{-4}{-2} = 2 \\ y = -4 + 18 + 10 = 24 \end{cases} \Rightarrow \sqrt{(-\infty, 24]} \Rightarrow R_f = (0, \sqrt{24}]$

الف) $R_f = R_i$ (بذلك يكون من (v))

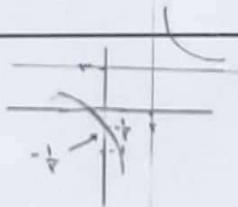
ب) $R_f = \sqrt{R} \rightsquigarrow R_f = [0, +\infty)$

الف) $R = \left\{ \frac{2x}{x} \right\} \rightsquigarrow R_f = R - \{2\}$

ب) $R_f = [0, +\infty) - \left\{ \frac{\sqrt{2x}}{x} \right\} \rightsquigarrow R_f = [0, +\infty) - \{2\}$

ب) $R_f = \sqrt{R - \{2\}}$

الف) $\begin{cases} \text{مماس} = \text{نقطة} = 2 \\ \text{انق} = y = \frac{a}{c} = 2 \end{cases}$



ب) $y = \frac{2x-2}{-2x+1} = \frac{2(x-1)}{-(2x-1)} = -2 \rightsquigarrow y = -2$



الف) $\cos > 0$ $R_f = [2, +\infty)$

ب) $\frac{x^2}{x} + \frac{1}{x} \rightarrow x + \frac{1}{x} \rightsquigarrow \sqrt{(-\infty, -2] \cup [2, +\infty)} \rightsquigarrow R_f = (-\infty, \sqrt{-2}] \cup [\sqrt{2}, +\infty)$

سواء في