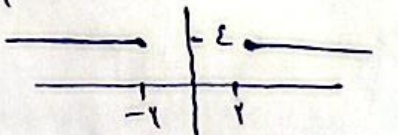


(۱) $D_f = \mathbb{R} - \{0\}$ $D_g = \mathbb{R} - \{0\}$ $f(x) = g(x)$ توابع با هم برابر اند ✓	$\sin x \neq \frac{x}{x} \Rightarrow D_f = \mathbb{R} \setminus \{0\}$ $D_g = \mathbb{R}$ $f(x) = \frac{\sin x}{x}$ $f(x) = g(x) = \sin x$ توابع با هم برابر هستند ✓	(۲) $D_f = \mathbb{R}, D_g = \mathbb{R}$ $f(x) = \frac{x^2 + 2x + 1}{x^2 + 6x + 5}$ $f(x) = \frac{x^2 + 2x + 1}{x^2 + 6x + 5} = 1$ $f(x) = g(x) = 1$ توابع با هم برابر اند. ✓	(الف) $D_f = \mathbb{R} \cup \{0\}$ $D_g = \mathbb{R}$ $D_g \neq D_f$ توابع با هم برابر نیستند ✓
$D_f = \mathbb{R}$ $D_g = \mathbb{R}$ $f(x) = \frac{x(x+1)}{x+1}$ $f(x) = x+1$ $f(x) = g(x)$ ✓ توابع برابر هستند.	(ج) $D_f = \mathbb{R} \Rightarrow \emptyset$ $D_g = \mathbb{R} \Rightarrow \mathbb{R}^+$ $D_f \neq D_g \Rightarrow$ توابع برابر نیستند ✓	(ب) $[x_n] \neq 0 \Rightarrow 0 < x_n < \frac{1}{x}$ $D_f = \mathbb{R} - [0, \frac{1}{x})$ $[x_n] \neq 0 \Rightarrow 0 < x_n < 1$ $D_g = \mathbb{R} - [0, 1)$ $D_f \neq D_g \Rightarrow$ توابع با هم برابر نیستند. ✓	(الف) $D_f = \mathbb{R}$ $D_g = \mathbb{R}$ $f(x) = g(x) = 0$ توابع برابر اند ✓
۳ $\begin{cases} f(x) + g(x) = x^2 + x + 1 \\ f(x) - g(x) = x^2 - x + 1 \end{cases}$ $\begin{cases} 2f(x) = 2x^2 + 2 \Rightarrow f(x) = x^2 + 1 \\ g(x) = x \end{cases}$ $f^2(x) + g^2(x) = x^4 + 2x^2 + 1 + x^2 = x^4 + 3x^2 + 1$			
۴ $f \cdot g = (x - \sqrt{x^2 - 2})(x + \sqrt{x^2 - 2}) = x^2 - (x^2 - 2) = 2$ $f \cdot g = 2 \Rightarrow D_f = \begin{cases} x \geq 2 \\ x \leq -2 \end{cases} \Rightarrow D_f = [2, +\infty) \cup (-\infty, -2]$ 			
۵ $g(x) \Rightarrow 2x^2 - 3x - 6 \Rightarrow x^2 - 3x - 3 = 0 \Rightarrow x = \frac{3 \pm \sqrt{9 + 12}}{2} = \frac{3 \pm \sqrt{21}}{2}$ $f(x) = \frac{ax + 2}{x^2 - \frac{3}{2}x - \frac{6}{2}} \Rightarrow m = \frac{3}{2}, n = -\frac{6}{2} \Rightarrow 2x^2 - 3x - 6 = 2(x^2 - \frac{3}{2}x - 3)$ $g(x) = \frac{x - b}{(2x - 6)(x + 1)} \Rightarrow \begin{cases} x \neq -1 \\ x \neq \frac{3}{2} \end{cases} \Rightarrow D_g = \mathbb{R} - \{-1, \frac{3}{2}\} \Rightarrow \frac{x - b}{2x^2 - 3x - 6} = \frac{ax + 2}{x^2 - \frac{3}{2}x - 3}$ $2ax + 2 = x - b \Rightarrow \begin{cases} x=0 \Rightarrow -b = 2 \Rightarrow b = -2 \\ x=1 \Rightarrow 2a + 2 = -6 \Rightarrow a = -4 \end{cases} \Rightarrow am - bn = \frac{1}{2} \cdot \frac{3}{2} - (-2)(-\frac{6}{2}) = \frac{3}{4} - 6 = -\frac{21}{4}$ $\frac{3}{4} - \frac{21}{4} = -\frac{18}{4} = -\frac{9}{2}$			

$$\frac{ba+2}{1a+b} \Rightarrow \text{فرض کنیم } a=1 \text{ و } b=1 \Rightarrow b^2=14 \Rightarrow b=\pm 2 \Rightarrow g(a)=f(a) \Rightarrow \frac{ba+2}{1a+b}=c \Rightarrow$$

$$1ac+bc=ba+2 \Rightarrow \begin{cases} b=2 \rightarrow c=\frac{1}{2} \\ b=-2 \rightarrow c=-\frac{1}{2} \end{cases} \Rightarrow a \neq a \Rightarrow$$

$$b=2 \rightarrow 1a+2 \neq 0 \rightarrow (2a+2) \neq 0 \rightarrow a \neq a \neq -\frac{1}{2} \Rightarrow a=-\frac{1}{2} \Rightarrow \frac{ab}{c} = \frac{\frac{1}{2} \cdot 2}{\frac{1}{2}} = 2 \Rightarrow -2$$

$$b=-2 \rightarrow 1a-2 \neq 0 \rightarrow a \neq a \neq \frac{1}{2} \Rightarrow a=\frac{1}{2} \Rightarrow \frac{ab}{c} = \frac{\frac{1}{2} \cdot (-2)}{-\frac{1}{2}} = 2 \Rightarrow 2$$

$$f = \{(-1, 2), (2, 1), (2, -1), (0, 1)\} \Rightarrow f = \{(-1, 2), (2, 1), (2, -1), (0, \frac{1}{2})\}$$

$$f+g = \{(-1, -2), (2, 1), (2, 2)\}$$

$$\frac{fg}{f+g} = \{(-1, 2), (2, 1), (2, 2)\} \Rightarrow R_f = \{1, 2, 3\}$$

$$f(a)=g(a) \Rightarrow a=-1, \quad 2a-2b=1 \Rightarrow -2-2b=1 \rightarrow 2b=2$$

$$b=-1 \Rightarrow a=d=-1 \Rightarrow c=a-2b \Rightarrow c=-1+2=1$$

$$c+d=1-1=0$$

$$D_f = -a^2 + a - m \geq 0 \Rightarrow -(a^2 - a + m) \geq 0 \Rightarrow a^2 - a + m \leq 0$$

$$a^2 - a + m \leq 0 \Rightarrow 0 = 1 - 4m = 0 \Rightarrow 4m = 1 \Rightarrow m = \frac{1}{4}$$

$$a = \frac{-1}{-2} = \frac{1}{2} \Rightarrow f(a) = \sqrt{-a^2 + a - m} \Rightarrow f(\frac{1}{2}) = \sqrt{-\frac{1}{4} + \frac{1}{2} - \frac{1}{4}} = \sqrt{0} = 0$$

$$\left. \begin{matrix} a=a=\frac{1}{2} \\ b=f(a)=0 \end{matrix} \right\} a+b = \frac{1}{2} + 0 = \frac{1}{2}$$

$$D_g = 12 - 4c \Rightarrow D_f(a) = 12 - 4b = 0 \Rightarrow$$

نیز می‌توانیم به روش دیگر

$$12 = 4b \Rightarrow b=3 \Rightarrow f(a) = \frac{2a+a}{a^2+4a+4} = \frac{3a+a}{(a+2)^2} \Rightarrow (a+2)^2 \neq 0 \Rightarrow$$

$$a \neq -2 \Rightarrow D_f = 12 - 4c \Rightarrow D_f = D_g \Rightarrow c = -3 \Rightarrow f(a) = g(a)$$

$$\frac{2a+a}{(a+2)(a+2)} = \frac{3}{a+2} \Rightarrow (2a+a)(a+2) = 3(a+2)(a+2) \Rightarrow$$

$$2a+a=3 \Rightarrow a=1 \Rightarrow a+b+c = 1+3-3=1$$