

کلاس: دفتر دهم

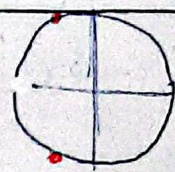
باستفاده شریعی تلفظ شماره: ۲۵

آشنا و خاضی: استاد سید میری

الف) $y = \frac{\sin x - 2}{\cos x + 1} \neq 0$

$\cos x + 1 \neq 0 \rightarrow \cos x \neq -1$

$D_f = R - \{2k\pi + \frac{3\pi}{2}, 2k\pi + \frac{5\pi}{2}\}$

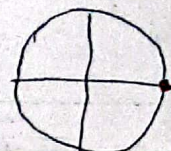


ب) $y = \frac{\sin x + 2}{\cos x - 1} \neq 0$

$\cos x - 1 \neq 0 \rightarrow \cos x \neq 1$

$2k\pi \neq 0, 2\pi$

$D_f = R - \{k\pi\}$



الف) $y = \frac{2\sin x + 1}{\tan x + 1} \neq 0$

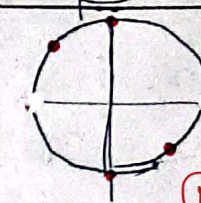
$\tan x + 1 \neq 0 \rightarrow \frac{\sin x}{\cos x} + 1 \neq 0$

$\frac{\sin x}{\cos x} \neq -1$

$\frac{\sin x}{\cos x} \rightarrow \frac{-\frac{\sqrt{2}}{2}}{\frac{\sqrt{2}}{2}} = -1$

$\cos x \neq 0$

$D_f = R - \{k\pi + \frac{\pi}{4}, k\pi - \frac{\pi}{4}\}$



ب) $y = \frac{\cos x + 1}{\cot x - 1} \neq 0$

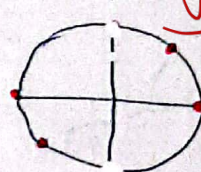
$\cot x - 1 \neq 0 \rightarrow \frac{\cos x}{\sin x} \neq 1$

$\frac{\cos x}{\sin x} \neq 1$

$\frac{\cos x}{\sin x} \rightarrow \frac{\frac{\sqrt{2}}{2}}{\frac{\sqrt{2}}{2}} = 1$

$\frac{\cos x}{\sin x} \rightarrow \frac{-\frac{\sqrt{2}}{2}}{-\frac{\sqrt{2}}{2}} = 1$

$D_f = R - \{k\pi, k\pi + \frac{\pi}{2}\}$



الف) $\sin y = x^2 - 2 \rightarrow -1 \leq x^2 - 2 \leq 1$

$+2 \rightarrow 1 \leq x^2 \leq 3 \rightarrow \sqrt{1} \leq x \leq \sqrt{3}$

$D_f = [1, \sqrt{3}] \cup [-\sqrt{3}, -1]$

$-1 \leq x \leq -\sqrt{3}$

ب) $y = \arccos(\sqrt{x} - 2) \rightarrow -1 \leq \sqrt{x} - 2 \leq 1$

$+2 \rightarrow 1 \leq \sqrt{x} \leq 3 \rightarrow \sqrt{1} \leq x \leq 9$

$D_f = [1, 9]$

الف) $\cos y = |x| - 2 \rightarrow -1 \leq |x| - 2 \leq 1 \rightarrow 1 \leq |x| \leq 3$

$D_f = [1, 3] \cup [-3, -1]$

$1 \leq x \leq 3$

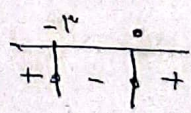
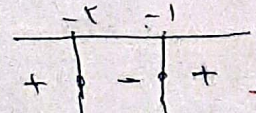
$-3 \leq x \leq -1$

ب) $y = \arcsin(x^2 + 3x + 1)$

$-1 \leq x^2 + 3x + 1 \leq 1 \rightarrow x^2 + 3x + 1 \leq 1$

$x^2 + 3x + 1 \leq 1 \rightarrow (x+1)(x+2) \leq 0$

$x^2 + 3x + 1 \geq -1 \rightarrow x^2 + 3x + 2 \geq 0$



$x(x+2) \geq 0$
 $x \leq -2$ or $x \geq 0$

$D_f = [-3, -2] \cup [-1, 0]$

الف) $y = \log_{\frac{1}{2}}(x^2 - 2) \rightarrow x^2 - 2 > 0 \rightarrow x^2 > 2 \rightarrow x > \sqrt{2}$

$D_f = (\sqrt{2}, +\infty) \cup (-\infty, -\sqrt{2})$

ب) $y = \log_{\frac{1}{2}}(x^2 - 1)$

$x^2 - 1 > 0 \rightarrow x^2 > 1 \rightarrow x > 1$

$D_f = (-1, 1)$

الف) $y = \log_{x-2}^{5-x}$

$5-x > 0 \Rightarrow x < 5$ $x-2 > 0 \Rightarrow x > 2$ $x-2 \neq 1 \Rightarrow x \neq 3$
 $D_f = (2, 5) - \{3\}$

ب) $y = \log_{x+2}^{x^2-1}$

$x^2-1 > 0 \Rightarrow x < -1$ $x > 1$ $x+2 > 0 \Rightarrow x > -2$ $x+2 \neq 1 \Rightarrow x \neq -1$
 $D_f = (-1, +\infty) \cup (-2, -1) - \{-1\}$

الف) $y = \log \frac{x^2-4x+3}{x-2} > 0$

$(x-1)(x-3) > 0$ $x-2 > 0 \Rightarrow x > 2$

$D_f = (1, 2) \cup (3, +\infty)$

ب) $y = \log \frac{x+2}{x-2}$

$\frac{x+2}{x-2} > 0$ $x+2 > 0 \Rightarrow x > -2$ $x-2 \neq 0 \Rightarrow x \neq 2$

$D_f = (-2, 2) \cup (2, +\infty) - \{2\}$

الف) $y = \sqrt{2 - \log_2(x-1)} > 0$

$\log_2(x-1) < 2 \Rightarrow x-1 < 4 \Rightarrow x < 5$

$x-1 > 0 \Rightarrow x > 1$

$D_f = (1, 5]$

ب) $y = \log(2 \log_2 x - 1)$

$x > 0$ $2 \log_2 x - 1 > 0 \Rightarrow \log_2 x > \frac{1}{2} \Rightarrow x > \sqrt{2}$

$\log_2 x > \frac{1}{2} \Rightarrow x > \sqrt{2}$

$D_f = (\sqrt{2}, +\infty)$

الف) $y = \frac{x}{x^2+1}$

$x^2+1 \neq 0 \Rightarrow x^2 \neq -1$ $D_f = \mathbb{R}$

ب) $y = \frac{x}{x^2-1}$

$x^2-1 \neq 0 \Rightarrow x^2 \neq 1 \Rightarrow x \neq \pm 1$ $D_f = \mathbb{R} - \{0\}$

ج) $y = \frac{x}{x^2-2}$

$x^2-2 \neq 0 \Rightarrow x^2 \neq 2 \Rightarrow \log_2 x \neq \log_2 \sqrt{2}$ $D_f = \mathbb{R} - \{\log_2 \sqrt{2}\}$

د) $y = \frac{x}{x^2-4}$

$x^2-4 \neq 0 \Rightarrow x^2 \neq 4 \Rightarrow \log_2 x \neq \log_2 2$ $D_f = \mathbb{R} - \{\log_2 2\}$

الف) $y = (kx+1)!$

$kx+1 \in \mathbb{W} \Rightarrow kx \in \mathbb{W}-1 \Rightarrow x \in \frac{\mathbb{W}-1}{k}$

$D_f = \{x \mid x = \frac{k-1}{k}, k \in \mathbb{W}\}$

ب) $y = (\frac{kx-r}{rx-d})!$

$\frac{kx-r}{rx-d} \in \mathbb{W} \Rightarrow kx-r = rxw-dw$

$kx-r = rxw-dw \Rightarrow x(k-rw) = -dw+r$

$x = \frac{-dw+r}{k-rw} = x = \frac{dw-r}{rw-k} \Rightarrow D_f = \{x \mid x = \frac{dw-r}{rw-k}, k \in \mathbb{W}\}$