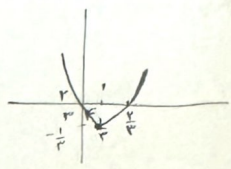


۲۵

① $\Delta = b^2 - 4ac = 0$ \Rightarrow $\frac{b^2}{4} = ac$ \Rightarrow $\frac{1}{4} = \frac{1}{3} \cdot c$ \Rightarrow $c = \frac{3}{4}$

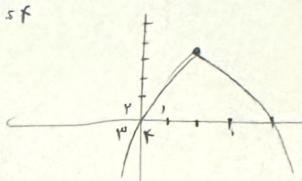
الف) $y = 3x^2 - 2x$ \Rightarrow $\alpha = \frac{-b}{2a} = \frac{1}{3}$ \Rightarrow $\beta = \frac{-c}{a} = -\frac{1}{3}$



الف) در ناحیه $0 < x < 1$ منفی دارد

ب) $y = -x^2 + 4x$ \Rightarrow $\alpha = 2$ \Rightarrow $\beta = 4$

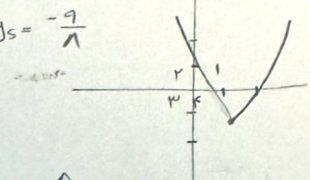
$\alpha = 2 \Rightarrow \beta = 4$ \Rightarrow $y = -x^2 + 4x$



ب) در ناحیه $0 < x < 4$ مثبت دارد

② $\Delta = 16 - 14 = 2$ \Rightarrow $\alpha = \frac{2}{4} = \frac{1}{2}$ \Rightarrow $\beta = \frac{-9}{1} = -9$

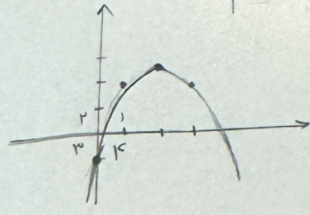
الف) $y = 2x^2 - 9x + 1$ \Rightarrow $\alpha = 2 \Rightarrow \beta = 1$



الف) در ناحیه $0 < x < 1$ مثبت دارد

ب) $y = -x^2 + 4x - 1$ \Rightarrow $\alpha = 2 \Rightarrow \beta = 1$

$\alpha = 2 \Rightarrow \beta = 1$ \Rightarrow $y = -x^2 + 4x - 1$



ب) در ناحیه $0 < x < 4$ مثبت دارد

③ $\alpha^2 - \alpha - 3 = 0$ \Rightarrow $\alpha, \beta \Rightarrow$ $\frac{-b}{a} = \frac{-1}{1} = -1$ \Rightarrow $\frac{\sqrt{\Delta}}{|a|} = \frac{\sqrt{13}}{1} = \sqrt{13}$

الف) $\frac{\alpha + \beta}{\alpha - \beta} = \frac{1}{\sqrt{13}} = \frac{\sqrt{13}}{13}$

$\alpha + \beta = -1$ \Rightarrow $\alpha - \beta = \sqrt{13}$

ب) $\alpha^2 + \beta^2 = 5^2 - 2p = 1 - 2(-3) = 1 + 6 = 7$

$p = \frac{c}{a} = -3$

ج) $\alpha^3 + \beta^3 = 5^3 - 3ps = 1 - 3(-3)(1) = 1 + 9 = 10$

د) $\alpha^3 - \beta^3 = (\alpha - \beta)(\alpha^2 + \alpha\beta + \beta^2) = \sqrt{13}(4) = 4\sqrt{13}$

④ $y = (x-2)(x^2 - ax + a)$ \Rightarrow $\Delta = b^2 - 4ac = 4 - 4a^2 < 0$

$(x-2)(x^2 - ax + a) = (x-2)^2 = (x^2 - 4x + 4) \Rightarrow a = 4$

$\Delta = 4 - 4a^2 < 0 \Rightarrow a(a-2) < 0 \Rightarrow a \in (0, 2]$

⑤ $3ax^2 - 12x - a = 0 \Rightarrow \alpha, \beta \Rightarrow$ $\frac{-b}{a} = \frac{12}{3a} = \frac{4}{a}$ \Rightarrow $\frac{-a}{3a} = -\frac{1}{3}$

$3ax^2 + \beta^2 - 4a = 0$

$3ax^2 - 12x - a = 0 \Rightarrow \alpha^2 - 4a = \frac{a}{3}$
 $\alpha^2 + \beta^2 = 5^2 - 2p = 14 - 2(-\frac{a}{3}) = 14 + \frac{2a}{3}$

$(\alpha^2 - 4a) + (\alpha^2 + \beta^2) = 14 + \frac{2a}{3} \Rightarrow \frac{2a}{3} + 14 = 14 + \frac{2a}{3} \Rightarrow a = -9$

$3ax^2 - 12x + 9 = 0$

$\alpha = 1 \Rightarrow \beta = \frac{9}{3} = 3 \Rightarrow$ $\frac{-9}{3} = -3$

$\textcircled{9} \quad x, y \in \mathbb{N}$
 $A(r\alpha + r^2, a-r) \rightsquigarrow r\alpha + r^2 > 0 \rightarrow r\alpha > -r^2 \rightarrow a > -\frac{r^2}{r} \rightarrow a > -r$
 $B(v-r\alpha, a-r) \rightsquigarrow v-r\alpha > 0 \rightarrow -r\alpha > -v \rightarrow a < \frac{r^2}{v}$
 $\left. \begin{matrix} a > -r \\ a > r \end{matrix} \right\} \Rightarrow a = r$

$A = (a, 1) \quad B = (1, 1) \quad S(b, b-r)$
 $y = a(n-a)^r + r^2$
 $\alpha_s = \frac{a+1}{r} = \frac{1}{r} = a = b \Rightarrow S = (a, r)$
 $\hookrightarrow a(-\varepsilon)^r + r^2 = 1$
 $(1, 1) \quad 1 \cdot a = -r \rightarrow a = -\frac{1}{r}$
 $\text{المجموع} = C = -\frac{r^2}{r} + r^2 = (-1/r^2) = -\frac{1}{r}$

$\textcircled{10} \quad \text{معاملات}$
 $ax^r - ax - b = 0 \rightsquigarrow \alpha, \beta$
 $B = 1 - \alpha \quad (r_0 \beta^r + r_0 \alpha^r - r_0 \beta) = 1V$
 $\hookrightarrow r_0(1-\alpha)^r + r_0(\alpha^r) - r_0(1-\alpha) = 1V$
 $r_0 + r_0 \alpha^r - 1 - \alpha + r_0 \alpha^r - r_0 + r_0 \alpha = 1V$
 $2r_0 \alpha^r - 2\alpha = 1V$
 $r_0 \alpha^r - \alpha = \frac{1}{2}V$
 $r_0 \alpha^r - \alpha + r^2 = - \rightsquigarrow r_0 \alpha^r - r_0 \alpha + 1 = -$
 $\Delta = B^2 - 4AC = r^2 - 4 \cdot 1 \cdot 1 = r^2 - 4$
 $\alpha = \frac{-r \pm \sqrt{r^2 - 4}}{2r} = \frac{r_0 \pm \sqrt{r^2 - 4}}{r} = \frac{r_0 \pm \sqrt{r^2 - 4}}{r} = \frac{r_0 \pm \sqrt{r^2 - 4}}{r}$

$\textcircled{11} \quad (a, 2B) \quad (1, 2B)$
 $x_s = \frac{-2+1}{r} = -\frac{1}{r}$
 $y_s = -\frac{1}{r}$
 $y = \frac{1}{r}n^r + r^2n + \frac{r^2}{r}$
 $\hookrightarrow n=1 \quad \frac{1}{r} + r + \frac{r^2}{r} = r + r = r \rightsquigarrow \beta = r$

$S = -4 \quad p = a \quad \Delta = r^2 - 4a$
 $\textcircled{12} \quad \alpha^r + 4\alpha + a = 0 \quad \alpha < \beta < 0 \quad a = ?$
 $\alpha = \frac{-4 + \sqrt{r^2 - 4a}}{r} \quad \beta = \frac{-4 - \sqrt{r^2 - 4a}}{r}$
 $\alpha = -r - \sqrt{r^2 - 4a} \quad \beta = -r + \sqrt{r^2 - 4a}$
 $\alpha^r + (\alpha + \beta)^r = 1V\sqrt{r} + 1\omega$
 $\alpha^r + (-r)^r = r^r(r^2 - 4a) + (-r + \sqrt{r^2 - 4a})^r = r^r - r^r + 4a + r + 4a - a + 4\sqrt{r^2 - 4a} = 1V\sqrt{r} + 1\omega$
 $4a - a = 1 \rightarrow a = 1$

$\textcircled{13} \quad r^2 \alpha^r - (m + 1r) \alpha + 1 = 0$
 $\frac{1}{\sqrt{a}} + \frac{1}{\sqrt{b}} = \frac{\sqrt{b} + \sqrt{a}}{\sqrt{a}\sqrt{b}} = \frac{\sqrt{b} + \sqrt{a}}{\sqrt{m+r}}$
 $(\sqrt{a} + \sqrt{b})^r = \alpha + \beta + r \frac{\sqrt{a}\sqrt{b}}{1} = \frac{1}{r} + \frac{m+1r}{r} = \frac{m+r}{r}$
 $\rightsquigarrow \sqrt{a} + \sqrt{b} = \frac{\sqrt{m+r}}{r}$
 $y = m\alpha^r + r^2\alpha + r \quad m = -1 \rightsquigarrow y = -\alpha^r + r^2\alpha + r$
 $P = \frac{C}{a} = \frac{r}{-1} = -r$