

1

1

۲ ۳ ۴

$$b = \frac{a+c}{r} = \frac{1^r + 1 + f}{r} = \frac{1+r}{r} = 1 + \frac{1}{r}$$

$\underbrace{1, 1, \dots, f}_{\text{دسته ۱۹}}$

1, 2, 3

2

4 5 6 7 8 9 10 11 12

13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 135, 136, 137, 138, 139, 140, 141, 142, 143, 144, 145, 146, 147, 148, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185, 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 199, 200, 201, 202, 203, 204, 205, 206, 207, 208, 209, 210, 211, 212, 213, 214, 215, 216, 217, 218, 219, 220, 221, 222, 223, 224, 225, 226, 227, 228, 229, 230, 231, 232, 233, 234, 235, 236, 237, 238, 239, 240, 241, 242, 243, 244, 245, 246, 247, 248, 249, 250, 251, 252, 253, 254, 255, 256, 257, 258, 259, 260, 261, 262, 263, 264, 265, 266, 267, 268, 269, 270, 271, 272, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 283, 284, 285, 286, 287, 288, 289, 290, 291, 292, 293, 294, 295, 296, 297, 298, 299, 300, 301, 302, 303, 304, 305, 306, 307, 308, 309, 310, 311, 312, 313, 314, 315, 316, 317, 318, 319, 320, 321, 322, 323, 324, 325, 326, 327, 328, 329, 330, 331, 332, 333, 334, 335, 336, 337, 338, 339, 340, 341, 342, 343, 344, 345, 346, 347, 348, 349, 350, 351, 352, 353, 354, 355, 356, 357, 358, 359, 360, 361, 362, 363, 364, 365, 366, 367, 368, 369, 370, 371, 372, 373, 374, 375, 376, 377, 378, 379, 380, 381, 382, 383, 384, 385, 386, 387, 388, 389, 390, 391, 392, 393, 394, 395, 396, 397, 398, 399, 400, 401, 402, 403, 404, 405, 406, 407, 408, 409, 410, 411, 412, 413, 414, 415, 416, 417, 418, 419, 420, 421, 422, 423, 424, 425, 426, 427, 428, 429, 430, 431, 432, 433, 434, 435, 436, 437, 438, 439, 440, 441, 442, 443, 444, 445, 446, 447, 448, 449, 450, 451, 452, 453, 454, 455, 456, 457, 458, 459, 460, 461, 462, 463, 464, 465, 466, 467, 468, 469, 470, 471, 472, 473, 474, 475, 476, 477, 478, 479, 480, 481, 482, 483, 484, 485, 486, 487, 488, 489, 490, 491, 492, 493, 494, 495, 496, 497, 498, 499, 500, 501, 502, 503, 504, 505, 506, 507, 508, 509, 510, 511, 512, 513, 514, 515, 516, 517, 518, 519, 520, 521, 522, 523, 524, 525, 526, 527, 528, 529, 530, 531, 532, 533, 534, 535, 536, 537, 538, 539, 540, 541, 542, 543, 544, 545, 546, 547, 548, 549, 550, 551, 552, 553, 554, 555, 556, 557, 558, 559, 560, 561, 562, 563, 564, 565, 566, 567, 568, 569, 570, 571, 572, 573, 574, 575, 576, 577, 578, 579, 580, 581, 582, 583, 584, 585, 586, 587, 588, 589, 590, 591, 592, 593, 594, 595, 596, 597, 598, 599, 600, 601, 602, 603, 604, 605, 606, 607, 608, 609, 610, 611, 612, 613, 614, 615, 616, 617, 618, 619, 620, 621, 622, 623, 624, 625, 626, 627, 628, 629, 630, 631, 632, 633, 634, 635, 636, 637, 638, 639, 640, 641, 642, 643, 644, 645, 646, 647, 648, 649, 650, 651, 652, 653, 654, 655, 656, 657, 658, 659, 660, 661, 662, 663, 664, 665, 666, 667, 668, 669, 670, 671, 672, 673, 674, 675, 676, 677, 678, 679, 680, 681, 682, 683, 684, 685, 686, 687, 688, 689, 690, 691, 692, 693, 694, 695, 696, 697, 698, 699, 700, 701, 702, 703, 704, 705, 706, 707, 708, 709, 710, 711, 712, 713, 714, 715, 716, 717, 718, 719, 720, 721, 722, 723, 724, 725, 726, 727, 728, 729, 730, 731, 732, 733, 734, 735, 736, 737, 738, 739, 740, 741, 742, 743, 744, 745, 746, 747, 748, 749, 750, 751, 752, 753, 754, 755, 756, 757, 758, 759, 760, 761, 762, 763, 764, 765, 766, 767, 768, 769, 770, 771, 772, 773, 774, 775, 776, 777, 778, 779, 780, 781, 782, 783, 784, 785, 786, 787, 788, 789, 790, 791, 792, 793, 794, 795, 796, 797, 798, 799, 800, 801, 802, 803, 804, 805, 806, 807, 808, 809, 810, 811, 812, 813, 814, 815, 816, 817, 818, 819, 820, 821, 822, 823, 824, 825, 826, 827, 828, 829, 830, 831, 832, 833, 834, 835, 836, 837, 838, 839, 840, 841, 842, 843, 844, 845, 846, 847, 848, 849, 850, 851, 852, 853, 854, 855, 856, 857, 858, 859, 860, 861, 862, 863, 864, 865, 866, 867, 868, 869, 870, 871, 872, 873, 874, 875, 876, 877, 878, 879, 880, 881, 882, 883, 884, 885, 886, 887, 888, 889, 890, 891, 892, 893, 894, 895, 896, 897, 898, 899, 900, 901, 902, 903, 904, 905, 906, 907, 908, 909, 910, 911, 912, 913, 914, 915, 916, 917, 918, 919, 920, 921, 922, 923, 924, 925, 926, 927, 928, 929, 930, 931, 932, 933, 934, 935, 936, 937, 938, 939, 940, 941, 942, 943, 944, 945, 946, 947, 948, 949, 950, 951, 952, 953, 954, 955, 956, 957, 958, 959, 960, 961, 962, 963, 964, 965, 966, 967, 968, 969, 970, 971, 972, 973, 974, 975, 976, 977, 978, 979, 980, 981, 982, 983, 984, 985, 986, 987, 988, 989, 990, 991, 992, 993, 994, 995, 996, 997, 998, 999, 1000

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$$121, 122, \dots, 343 \quad \sum_{i=1}^n \frac{1}{i^2} = \frac{6}{5} \quad \sum_{i=1}^n \frac{1}{i^3} = \frac{35}{6}$$

$\frac{1}{x}, n=3K, n=0, 1, 2, 3, 4 \rightarrow \frac{1}{x}, \frac{1}{x^2}, \frac{1}{x^3}, \frac{1}{x^4} \rightarrow 1, x, x^2, x^3$

3

$-2K+f, n=3K+1 \rightarrow n=2, 3, 4 \rightarrow (-2)(1)+f, (-2)(2)+f, (-2)(3)+f \rightarrow f, 2f, 3f$

$$\left[\frac{n}{k+r} \right] + a, n=3K+2 \rightarrow n=3, 4, 5 \rightarrow \left[\frac{3}{1+r} \right] + a, \left[\frac{4}{1+r} \right] + a, \left[\frac{5}{1+r} \right] + a \rightarrow 1+a, 1+a, 1+a$$

$$\sum_{i=1}^n \frac{1}{i^2} = 1 + \frac{1}{4} + \frac{1}{9} + \frac{1}{16} + \frac{1}{25} + \frac{1}{36} + \frac{1}{49} + \frac{1}{64} + \frac{1}{81} + \frac{1}{100} + \frac{1}{121} + \frac{1}{144} + \frac{1}{169} + \frac{1}{196} + \frac{1}{225} + \frac{1}{256} + \frac{1}{289} + \frac{1}{324} + \frac{1}{361} + \frac{1}{400} + \frac{1}{441} + \frac{1}{484} + \frac{1}{529} + \frac{1}{576} + \frac{1}{625} + \frac{1}{676} + \frac{1}{729} + \frac{1}{784} + \frac{1}{841} + \frac{1}{900} + \frac{1}{961} + \frac{1}{1024} + \frac{1}{1089} + \frac{1}{1156} + \frac{1}{1225} + \frac{1}{1296} + \frac{1}{1369} + \frac{1}{1444} + \frac{1}{1521} + \frac{1}{1600} + \frac{1}{1681} + \frac{1}{1764} + \frac{1}{1849} + \frac{1}{1936} + \frac{1}{2025} + \frac{1}{2116} + \frac{1}{2209} + \frac{1}{2304} + \frac{1}{2401} + \frac{1}{2500} + \frac{1}{2601} + \frac{1}{2704} + \frac{1}{2809} + \frac{1}{2916} + \frac{1}{3025} + \frac{1}{3136} + \frac{1}{3249} + \frac{1}{3364} + \frac{1}{3481} + \frac{1}{3600} + \frac{1}{3721} + \frac{1}{3844} + \frac{1}{3969} + \frac{1}{4096} + \frac{1}{4225} + \frac{1}{4356} + \frac{1}{4489} + \frac{1}{4624} + \frac{1}{4761} + \frac{1}{4900} + \frac{1}{5041} + \frac{1}{5184} + \frac{1}{5329} + \frac{1}{5476} + \frac{1}{5625} + \frac{1}{5776} + \frac{1}{5929} + \frac{1}{6084} + \frac{1}{6241} + \frac{1}{6400} + \frac{1}{6561} + \frac{1}{6724} + \frac{1}{6889} + \frac{1}{7056} + \frac{1}{7225} + \frac{1}{7396} + \frac{1}{7569} + \frac{1}{7744} + \frac{1}{7921} + \frac{1}{8100} + \frac{1}{8281} + \frac{1}{8464} + \frac{1}{8649} + \frac{1}{8836} + \frac{1}{9025} + \frac{1}{9216} + \frac{1}{9409} + \frac{1}{9604} + \frac{1}{9801} + \frac{1}{10000}$$

$$a_r + a_{r+1} + \dots + a_{r+19} \xrightarrow{n=3K+2} \left[\frac{r}{1+r} \right] + a, \left[\frac{r+1}{1+r} \right] + a, \dots, \left[\frac{r+19}{1+r} \right] + a$$

مجموعه $a+r$ در 16

$$1-x+1-x+\dots-x+x(1-x)=1-x^2$$

4

$$ax^2+bx+c \rightarrow a = \frac{1}{\sqrt{0}}(-1f) = -\frac{1}{a}, a = 1f, a_v = 1v/r \rightarrow -\frac{1}{a}(a^2)+2b+c = 1f$$

$$-\frac{1}{a}(v^2)+vb+c = 1v/r$$

$$-a+a(f)+c = 1f \rightarrow \boxed{c=1} \quad \frac{vf}{a} - vb = -1v/r$$

$$\boxed{b=1f}$$

$$a_n = \frac{1}{a} n^2 + fn - 1 \quad \frac{a_n}{a_1} = \frac{\frac{1}{a}(1a^2$$

$$q = a + rd = \hat{a}_r, \quad q_x = a + rd = \hat{a}_r, \quad \hat{a}_1, \dots, \hat{a} + qd \rightarrow \hat{a} + qd \quad \cdot a$$

$$q_x - q = fd = \hat{a}_r - \hat{a}_r = ad \rightarrow d = \frac{ad}{f}$$

$$\frac{\hat{a}_1}{d}, \frac{\hat{a}_1 + fd}{d}, \frac{-qd + fd}{d} = \textcircled{f}$$

in b d = a d / f

$$q(a+rd) = a(a+rd) + r(a+rd)a \rightarrow qa^r + qd^r + radz da^r + bad + ra^r + rad \cdot q$$

$$a = ra^r - qd^r + ad \quad (ra - rd)(a + rd) = 0 \quad a = \frac{rd}{r} \quad \frac{q}{d} = \frac{a + rd}{d}$$

$$a = -rd \quad \frac{rd + rd}{d} = \textcircled{\frac{q}{r}} \quad \frac{-rd + rd}{d} = \textcircled{1}$$

$$a, b, c \xrightarrow{\text{V. line}} b, \frac{a}{r}, \frac{c}{f} \quad a + d, \frac{a}{r}, \frac{a + rd}{f}$$

$a = ad \quad a = rd$

$$\frac{\frac{a}{r}}{\frac{a + d}{f}} = \frac{\frac{a + rd}{f}}{\frac{a}{r}} \rightarrow \frac{a}{ra + rd} = \frac{ra + fd}{fa} \quad fa^r = ra^r + rd^r + rad$$

d = x d / x d

$$f(rd^r) = f(-rd) \rightarrow d(rd + ra) = 0 \quad rd + ra = 0 \rightarrow a = -\frac{rd}{r}$$

$$q = \frac{\frac{a}{r}}{\frac{a + d}{f}} = \frac{\frac{d}{r}}{\frac{d}{r}} = 1 \rightarrow rq = r(-1) = \textcircled{-r}$$

$$a, b, c \xrightarrow{\text{V. line}} r b, r a, c \rightarrow r a q, r a, c q \rightarrow a q^r - r a = r a - r a q$$

$a, a q, a q^r$

$$a q^r - fa + ra q = 0 \quad a(q - 1)(q + f) = 0 \quad q = 1 \quad \boxed{q = -f}$$

$$\frac{a q}{a q} = \frac{a q^{\hat{1}}}{a q^{\hat{d}}} = q^r = (-f)^r = -q f$$

11

$$\frac{a_r}{(a_r)^r} + \frac{a_r}{(a)^r} = r \quad \frac{a \hat{q}}{q^r q^r} + \frac{a q^r}{a^r} = \frac{a^r + a q}{a} = r \quad -9$$

$$r a^r - q^r - a q = 0 \quad (r a + q)(a - q) = 0 \rightarrow q = -r a$$

$$\frac{a^r}{q} \rightarrow \frac{a^r}{a q} = \frac{a^r}{a} = 1 \quad (1)$$

$$\frac{a^r}{a q} = \frac{a^r}{-r a^r} = \left(\frac{-1}{r} \right)$$

$$q = \sqrt{a^r} \quad (a q^r)^r = a q^r \rightarrow a^r q^r = a q^r \quad a q = 1 \quad -6$$

$$a = a q^r = r v = a q^r \times q^r = r^r \rightarrow q = r \rightarrow a(r^r) = r v \rightarrow a = \frac{1}{r}$$

$$\frac{1}{r} = \frac{1}{r} = \left(\frac{1}{q} \right)$$