

الف) $t_n = 2n^2 - 1$ $2, 11, 24, 47, 82, \dots$

ب) $t_n = \frac{n+1}{n+2}$ $\frac{2}{3}, \frac{3}{4}, \frac{4}{5}, \frac{5}{6}, \frac{6}{7}, \dots$

الف) $t_n = \frac{(-1)^n}{\sqrt{n+3}}$ $t_{12} = \frac{-1}{\sqrt{15}} = \frac{-1}{\sqrt{15}}$

ب) $t_n = 2n - \left\lfloor \frac{n}{2} \right\rfloor$ $t_{12} = 2 \times 12 - \left\lfloor \frac{12}{2} \right\rfloor = 22$

الف) $t_n = n - 10$ $n - 10 < 0 \Rightarrow n < 10 \Rightarrow n < 8 \rightarrow$ جمله ۸

ب) $t_n = n^2 - 12n + 10$ $n^2 - 12n + 10 < 0$
 $(n-10)(n-2) < 0$ $\begin{matrix} 10 & 2 \\ + & - & - & + \end{matrix} \rightarrow$ جمله ۸
 $n = 2, 3, 4, 5, 6, 7, 8, 9$

الف) $t_n = 2n - 14$ $2n - 14 < 0 \Rightarrow 2n < 14 \Rightarrow n < 7 \rightarrow$ جمله ۷

ب) $t_n = n^2 - 12n + 27$ $n^2 - 12n + 27 < 0$
 $(n-9)(n-3) < 0$ $\begin{matrix} 9 & 3 \\ + & - & - & + \end{matrix} \rightarrow$ جمله ۷
 $n = 3, 4, 5, 6, 7, 8, 9$

$\delta d \left(\begin{matrix} t_4 = 7 \\ t_9 = 22 \\ t_{12} = 22 \end{matrix} \right) 18$
 $-9d \left(\begin{matrix} t_4 = 7 \\ t_9 = 22 \\ t_{12} = 22 \end{matrix} \right) -11$

الف) $t_n = n^2 - 4n + 2$ $\text{Min} \left| \frac{-b}{2a} = \frac{4}{2} = 2 \right.$
 $9 - 11 + 2 = -1 \rightarrow \text{القيمة} = -1$

6

ب) $t_n = n^2 + 4n + 1$ $\text{Min} \left| \frac{-b}{2a} = -2 \right. \times$
 $1 - 1 + 1 = 1 \rightarrow \text{القيمة} = t_1 = 1 + 4 + 1 = 6$

$t_n = -1, -4, -9, -16, -25, \dots$
 $a = -1$ $t_n = an^2 + bn + c$
 $a = -1$ $t_n = n^2 - 4n + 1$
 $a + b + c = -1$
 $1 - 4 + 1 = -2$
 $t_{10} = 10^2 - 4 \times 10 + 1 = 51$

7

$t_n = -4, -1, 1, 4, \dots$
 $a = 1$ $t_n = an^2 + bn + c$
 $a = 1$ $t_n = n^2 - n - 4$
 $a + b + c = -4$
 $1 - 1 - 4 = -4$

8

$(-\infty, a+1] \cap [a+1, \infty) = \{a+1\}$

$a+1 > a+1$
 $a > 1$

9

الف) $1 < 3n < 100$ $\frac{1}{3} < n < \frac{100}{3}$ $1 < n < 33 \rightarrow 33$

ب) $1 < 8n < 100$ $\frac{1}{8} < n < \frac{100}{8}$ $1 < n < 12.5 \rightarrow 12$

ج) $1 < 18n < 100$ $\frac{1}{18} < n < \frac{100}{18}$ $1 < n < 5.5 \rightarrow 5$

د) $n(A \cup B) = n(A) + n(B) - n(A \cap B)$
 $33 + 12 - 5 = 40 \rightarrow 40$

10