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الف) $y = \frac{x+1}{x^2-2x+1}$ $\frac{x^2-2x+1}{x^2-2x+1} \cdot \frac{x-1}{x-1}$

$(x-1)(x-1)(x-1) \neq 0$ $\frac{-1x^2+2x-1}{-1x^2+2x-1}$ $D_f = \mathbb{R} - \{1, \frac{2}{x}, \frac{1}{x}\}$

$x-1 \neq 0 \Rightarrow x \neq 1$

$x^2-2 \neq 0 \Rightarrow x^2 \neq 2 \Rightarrow x \neq \pm\sqrt{2}$

$x^2-1 \neq 0 \Rightarrow x^2 \neq 1 \Rightarrow x \neq \pm 1$

ب) $y = \frac{x+1}{x^2-1x-1}$ $\frac{x^2-1x-1}{x^2-1x-1} \cdot \frac{x+1}{x+1}$

$(x+1)(x^2-1x-1) \neq 0$ $\frac{-x^2+x-1}{-x^2+x-1}$ $D_f = \mathbb{R} - \{-1, -\frac{1}{x}, 1\}$

$x+1 \neq 0 \Rightarrow x \neq -1$

$x^2-1x-1 \neq 0 \Rightarrow x^2-1x-1 \neq 0$

$(x+2)(x-4)$

$x = \frac{-2 \pm \sqrt{4+4}}{2} = \frac{-2 \pm 2}{2} = 0, -1$

ج) $y = \frac{x+1}{x-\sqrt{x^2-1}}$ $\frac{x^2-1}{x-\sqrt{x^2-1}} \cdot \frac{x+\sqrt{x^2-1}}{x+\sqrt{x^2-1}}$ $D_f = (-\infty, +\frac{1}{x}] - \{-1, 1\}$

$x^2-1 \geq 0 \Rightarrow x^2 \geq 1 \Rightarrow x \leq -1 \text{ or } x \geq 1$

ب) $y = \frac{x+1}{x-\sqrt{x^2-1}}$ $\frac{x^2-1}{x-\sqrt{x^2-1}} \cdot \frac{x+\sqrt{x^2-1}}{x+\sqrt{x^2-1}}$ $D_f = [\frac{1}{x}, +\infty) - \{1, -1\}$

$x^2-1 \geq 0 \Rightarrow x^2 \geq 1 \Rightarrow x \leq -1 \text{ or } x \geq 1$

الف) $y = \frac{\sin x}{\cos x - 1}$ $\cos x - 1 \neq 0 \Rightarrow \cos x \neq 1 \Rightarrow x \neq 2k\pi$ $D_f = \mathbb{R} - \{2k\pi, \frac{\pi}{2}, \frac{3\pi}{2}\}$

ب) $y = \frac{\cos x + 1}{\sin x + 1}$ $\sin x + 1 \neq 0 \Rightarrow \sin x \neq -1 \Rightarrow x \neq \frac{3\pi}{2} + 2k\pi$ $D_f = \mathbb{R} - \{\frac{3\pi}{2} + 2k\pi\}$

ج) $y = \frac{\tan x + 1}{\cot x - 1}$ $\cot x - 1 \neq 0 \Rightarrow \cot x \neq 1 \Rightarrow x \neq \frac{\pi}{4} + k\pi$ $D_f = \mathbb{R} - \{\frac{\pi}{4} + k\pi\}$

د) $y = \frac{\sin x + 1}{\sin^2 x - 1}$ $\sin^2 x - 1 \neq 0 \Rightarrow \sin^2 x \neq 1 \Rightarrow \sin x \neq \pm 1 \Rightarrow x \neq \frac{\pi}{2} + k\pi, \frac{3\pi}{2} + k\pi$ $D_f = \mathbb{R} - \{\frac{\pi}{2} + k\pi, \frac{3\pi}{2} + k\pi\}$

الف) $x^2 - 4x + 4 > 0$ $(x-2)(x-2)$ $\frac{2}{+} \frac{2}{-} \frac{2}{+}$ $x \in (-\infty, 2) \cup (2, +\infty)$

ب) $x^2 - 4x + 4 < 0$ $(x-1)(x-3)$ $\frac{1}{+} \frac{3}{-} \frac{3}{+}$ $x \in (1, 3)$

ج) $x^2 + 4x + 4 \geq 0$ $(x+2)(x+2)$ $\frac{-2}{+} \frac{-2}{-} \frac{-2}{+}$ $x \in (-\infty, -2] \cup [-2, +\infty)$

د) $x^2 - 4x + 4 \leq 0$ $(x-1)(x-4)$ $\frac{1}{+} \frac{4}{-} \frac{4}{+}$ $x \in [1, 4]$

الف) $x^2 - 3x + 2 < 0$ $(x-2)(x-1)$ $\frac{1}{-} \frac{2}{+} \frac{2}{-}$ $x \in (1, 2)$

ب) $\frac{x^2 - 1}{x^2 - 4x + 4} \geq 0$ $(x-1)(x+1)$ $\frac{-1}{+} \frac{1}{-} \frac{2}{-}$ $x \in (-\infty, -1] \cup (2, +\infty)$

ج) $y = \sqrt{\frac{x^2 - 3x + 2}{x^2 - 1}}$ $\frac{(x-2)(x-1)}{(x-1)(x+1)} \geq 0$ $\frac{1}{-} \frac{2}{-} \frac{2}{+}$ $D_f = [2, +\infty)$

د) $(x-1)(x^2 + x + 1) \neq 0$

ب) $y = \sqrt{\frac{x^2 - 3x + 2}{x^2 - 1}}$ $(x-1)(x+1) \neq 0$ $D_f = \mathbb{R} - \{\pm 1\}$

الف) $y = \log(x^2 - 3x)$ $x^2 - 3x > 0$ $x(x-3) > 0$ $\frac{0}{+} \frac{3}{-} \frac{3}{+}$ $D_f = (-\infty, 0) \cup (3, +\infty)$

ب) $y = \log_{|x|-2}^{14-x^2}$ $14 - x^2 > 0 \rightarrow 14 > x^2 \rightarrow -\sqrt{14} < x < \sqrt{14}$ $D_f = (-\sqrt{14}, -2) \cup (2, \sqrt{14}) - \{\pm 3\}$
 $|x| - 2 > 0 \rightarrow |x| > 2$ $|x| - 2 \neq 1 \rightarrow |x| \neq 3$

$x > 2$ $x < -2$ $x \neq \pm 3$

ج) $y = \log_{10-x} \frac{x^2 - 4x + 4}{x-3}$ $\frac{(x-2)(x-2)}{x-3} > 0$ $\frac{2}{-} \frac{2}{-} \frac{3}{+}$ $D_f = (3, 10) - \{9\}$

د) $y = \sqrt{x^2 - 11x + 11} + \log_x \sqrt{14 - x^2}$ $\sqrt{14 - x^2} > 0$ $14 > x^2 \rightarrow -\sqrt{14} < x < \sqrt{14}$
 $(x-1)(x-11) > 0$ $x > 0$ $x \neq 1$ $D_f = (-\sqrt{14}, 1) \cup (1, \sqrt{14}) - \{1\}$

$\frac{1}{+} \frac{11}{-} \frac{11}{+} \rightarrow (-\infty, 1) \cup [11, +\infty)$

$y = \frac{x^2 - x}{x^2 + x} \rightarrow \frac{x(x-1)}{x(x+1)} \neq 0$ $\frac{-1}{+} \frac{1}{-} \frac{1}{+}$ $D_f = (-\infty, -1) \cup (0, +\infty) \cup (1, +\infty)$

	-1	0	1
$x(x-1)$	+	+	-
$x(x+1)$	+	-	+
y	+	-	+

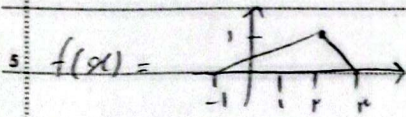
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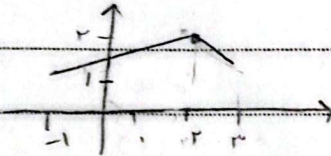
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$$y = \sqrt{\frac{x - f(x)}{f(x)}} \quad f(x) \neq 0 \rightarrow x \neq \pm 2$$

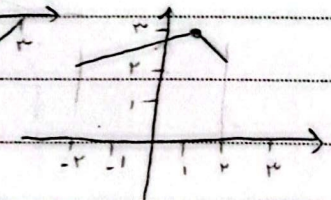
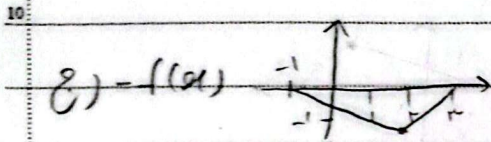
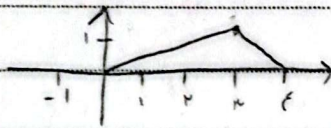
$$\frac{x - f(x)}{f(x)} \geq 0 \quad \begin{array}{c} -2+1 \quad 2 \quad 2 \\ +\frac{1}{2} - \frac{1}{2} + \frac{1}{2} - \frac{1}{2} + \end{array} \quad Df = (-\infty, -2) \cup [-1, 2) \cup [2, +\infty)$$



الف) $f(x) + 1$



ب) $f(x-1)$



د) $f(x+1) + 2$

