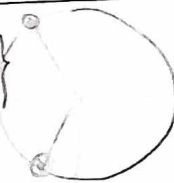


$$y = \frac{\sin x - 2}{2 \cos x + 1} \Rightarrow \begin{cases} 2 \cos x + 1 \neq 0 \\ 2 \cos x \neq -1 \\ \cos x \neq -\frac{1}{2} \end{cases} D_f = \mathbb{R} - \left\{ 2k\pi + \frac{2\pi}{3}, 2k\pi + \frac{4\pi}{3} \right\}$$

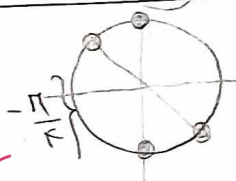


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$$y = \frac{\sin x + 2}{\cos x - 1} \Rightarrow \begin{cases} \cos x - 1 \neq 0 \\ \cos x \neq 1 \end{cases} D_f = \mathbb{R} - \{ 2k\pi \}$$

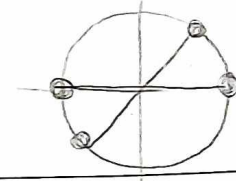


$$y = \frac{2 \sin x + 1}{\tan x + 1} \Rightarrow \begin{cases} \tan x + 1 \neq 0 \Rightarrow \tan x \neq -1 \\ \cos x \neq 0 \end{cases} D_f = \mathbb{R} - \left\{ k\pi + \frac{\pi}{4}, k\pi - \frac{\pi}{4} \right\}$$



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$$y = \frac{\cos x + 1}{\cot x - 1} \Rightarrow \begin{cases} \cot x - 1 \neq 0 \Rightarrow \cot x \neq 1 \\ \sin x \neq 0 \end{cases} D_f = \mathbb{R} - \left\{ k\pi, k\pi + \frac{\pi}{2} \right\}$$



$$\sin y = x^2 - 2 \Rightarrow \begin{cases} -1 \leq x^2 - 2 \leq 1 \Rightarrow \sqrt{1} \leq x \leq \sqrt{3} \text{ or } -\sqrt{3} \leq x \leq -1 \\ -1 \leq x^2 \leq 3 \Rightarrow -\sqrt{3} \leq x \leq \sqrt{3} \end{cases} D_f = [1, \sqrt{3}] \cup [-\sqrt{3}, -1]$$

$$y = \arccos(\sqrt{x} - 3) \Rightarrow \begin{cases} -1 \leq \sqrt{x} - 3 \leq 1 \\ 0 \leq \sqrt{x} \leq 4 \\ 9 \leq x \leq 16 \end{cases} D_f = [9, 16]$$

$$\cos y = |x| - 3 \Rightarrow \begin{cases} -1 \leq |x| - 3 \leq 1 \Rightarrow 2 \leq |x| \leq 4 \\ 2 \leq x \leq 4 \text{ or } -4 \leq x \leq -2 \end{cases} D_f = [2, 4] \cup [-4, -2]$$

$$y = \arcsin(x^2 + 3x + 1) \Rightarrow \begin{cases} -1 \leq x^2 + 3x + 1 \leq 1 \\ x^2 + 3x + 1 \geq -1 \Rightarrow x^2 + 3x + 2 \geq 0 \Rightarrow (x+1)(x+2) \geq 0 \\ |x^2 + 3x + 1| \leq 1 \Rightarrow x^2 - 3x \leq 0 \Rightarrow x(x-3) \leq 0 \end{cases} D_f = [-2, -1] \cup [0, 3]$$

$$y = \log_{x^2-2} x \Rightarrow \begin{cases} x^2 - 2 > 0 \Rightarrow x^2 > 2 \Rightarrow x > \sqrt{2} \text{ or } x < -\sqrt{2} \\ x^2 - 2 \neq 1 \Rightarrow x^2 \neq 3 \Rightarrow x \neq \sqrt{3} \text{ or } x \neq -\sqrt{3} \end{cases} D_f = (\sqrt{2}, +\infty) \cup (-\infty, -\sqrt{2})$$

$$y = \log_{x^2-2} (x-1) \Rightarrow \begin{cases} x^2 - 2 > 0 \Rightarrow x > \sqrt{2} \text{ or } x < -\sqrt{2} \\ x^2 - 2 \neq 1 \Rightarrow x^2 \neq 3 \Rightarrow x \neq \sqrt{3} \text{ or } x \neq -\sqrt{3} \\ x-1 > 0 \Rightarrow x > 1 \end{cases} D_f = (\sqrt{2}, 1) \cup (\sqrt{3}, +\infty)$$

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$$y = \log_{x-r} \omega - x$$

$$x-r+1$$

$$x+r$$

$$\omega - x > 0$$

$$\omega > x$$

$$x-r > 0$$

$$x > r$$

$$D_f = (r, \omega) - \{r\}$$

$$y = \log_{x+r} x^r - 1$$

$$x^r - 1 > 0 \quad (x-1)(x+1) > 0$$

$$x+r > 0 \quad x+r \neq 1 \quad D_f = (-r, -1] \cup [1, +\infty) - \{-r\}$$

$$y = \log_{x-r} \frac{x^r - r x + r^2}{x-r}$$

$$\frac{(x-1)(x-r)}{r x - r^2} > 0$$

$$D_f = [1, r), (r, +\infty)$$

$$y = \log_{x-r} \frac{x+r}{x-r}$$

$$x+\omega$$

$$x+\omega > 0$$

$$x > -\omega$$

$$x+\omega \neq 1$$

$$x \neq -r$$

$$D_f = (-\omega, -r] \cup (r, +\infty) - \{-r\}$$

$$y = \sqrt{r - \log_r (x-r)}$$

$$r - \log_r x - r \geq 0$$

$$x-r > 0$$

$$x > r$$

$$\log_r x - r \leq r$$

$$D_f = (r, 1]$$

$$x-r \leq 1 \quad x \leq 1$$

$$y = \log(r \log_r x - 1)$$

$$r \log_r x - 1 > 0$$

$$r \log_r x > 1$$

$$\log_r x > \frac{1}{r}$$

$$D_f = (r^{\frac{1}{r}}, +\infty)$$

$$x > r^{\frac{1}{r}}$$

$$y = \frac{r}{r^x + 1}$$

$$r^x \neq -1$$

$$D_f = \mathbb{R}$$

$$y = \frac{r}{r^x - r}$$

$$r^x - r \neq 0$$

$$r^x \neq r \rightarrow x \neq \log_r r$$

$$D_f = \mathbb{R} - \{\log_r r\}$$

$$y = \frac{r}{r^x - 1}$$

$$r^x \neq 1$$

$$x \neq 0$$

$$D_f = \mathbb{R} - \{0\}$$

$$y = \frac{r}{r^x - r}$$

$$r^x \neq r$$

$$x \neq \log_r r$$

$$D_f = \mathbb{R} - \{\log_r r\}$$

$$y = (r x + 1)!$$

$$r x + 1 \in \mathbb{W}$$

$$r x \in \mathbb{W} - 1$$

$$x \in \frac{\mathbb{W} - 1}{r}$$

$$D_f = \{x \mid x = \frac{k-1}{r}, k \in \mathbb{W}\}$$

$$y = \left( \frac{r x - r}{r x - \omega} \right)!$$

$$\frac{r x - r}{r x - \omega} \in \mathbb{W}$$

$$r W x - \omega W = r x - r$$

$$r W x - r x = \omega W - r$$

$$x(r W - r) = \omega W - r$$

$$x = \frac{\omega W - r}{r W - r}$$

$$D_f = \left\{ x \mid x = \frac{\omega k - r}{r k - r}, k \in \mathbb{W} \right\}$$