

الف) $y = \log_{a-r} \frac{a-x}{x-r}$ $a-x > 0$ $a > x$ $x-r \neq 0$ $x \neq r$ $\frac{1}{r} < \frac{1}{x} < \frac{1}{a}$ $DF = (r, a) - \{r\}$
 $a-x < 0$ $x > a$ $x \neq r$ $\frac{1}{r} > \frac{1}{x} > \frac{1}{a}$ $DF = (r, a) \cup (a, +\infty)$

ب) $y = \log_{x+r} \frac{x^r-1}{x+r}$ $x^r-1 > 0$ $x^r > 1$ $x > 1$ $x < -1$ $\frac{1}{x+r} < \frac{1}{x}$ $DF = (-r, -1) \cup (1, +\infty) - \{-r\}$
 $x^r-1 < 0$ $x < -1$ $x \neq -r$ $\frac{1}{x+r} > \frac{1}{x}$

الف) $y = \log \frac{x^r-rx+r}{x-r}$ $\frac{x^r-rx+r}{x-r} > 0$ $\frac{x^r-rx+r}{x-r} = \frac{(x-1)(x-r)^{r-1}}{(x-r)}$ $\frac{1}{0} + \frac{r}{0} +$ $DF = (1, r) \cup (r, +\infty)$

ب) $y = \log \frac{x+r}{x-r}$ $x+a > 0$ $x+a \neq 0$ $x \neq -a$ $\frac{x+r}{x-r} > 0$ $\frac{-r}{0} - \frac{r}{0} +$ $DF = (-a, -r) \cup (r, +\infty) - \{-r, r\}$
 $x+a < 0$ $x < -a$ $x \neq -r$

الف) $y = \sqrt{r - \log_r(x-r)}$ $r - \log_r(x-r) \geq 0$ $-\log_r(x-r) \geq -r$ $\log_r(x-r) \leq r$ $(x-r) \leq 1$ $x \leq 1+a$
 $a = b^c$ $x-r > 0$ $x > r$ $DF = (r, 1+a]$

ب) $y = \log(r \log_r x - 1)$ $x > 0 \rightarrow r \log_r x - 1 > 0 \rightarrow r \log_r x > 1 \rightarrow \log_r x > \frac{1}{r} \rightarrow x > r^{\frac{1}{r}} \rightarrow x > \sqrt[r]{r}$
 $DF = (\sqrt[r]{r}, +\infty)$

الف) $y = \frac{r}{f^x+1}$ $f^x+1 \neq 0$ $f^x \neq -1$ $\rightarrow DF = \mathbb{R}$

ب) $y = \frac{r}{f^x-1}$ $f^x-1 \neq 0$ $f^x \neq 1$ $x \neq 0 \rightarrow DF = \mathbb{R} - \{0\}$

ج) $y = \frac{r}{f^x-r}$ $f^x-r \neq 0$ $f^x \neq r$ $\rightarrow DF = \mathbb{R} - \{\log_f r\}$

د) $y = \frac{r}{f^x-r}$ $f^x-r \neq 0$ $f^x \neq r$ $\rightarrow DF = \mathbb{R} - \{\log_f r\}$

الف) $y = (f(x+1))!$ $f(x+1) \in \mathbb{N}$ $f(x) \in \mathbb{N}-1$ $x \in \frac{\mathbb{N}-1}{f} \rightarrow DF = \{x/x = \frac{k-1}{f}, k \in \mathbb{N}\}$

ب) $y = (\frac{r(x-r)}{r^x-a})!$ $\frac{r(x-r)}{r^x-a} \in \mathbb{N}$ $r(x-r) \in r^x \mathbb{N} - a \mathbb{N}$ $x \in \frac{r-a \mathbb{N}}{r-r^x}$
 $r(x-r) \mathbb{N} \in r-a \mathbb{N}$ $x(r-r^x) \in r-a \mathbb{N}$ $DF = \{x/x = \frac{r-a \mathbb{N}}{r-r^x}, k \in \mathbb{N}\}$

الف) $\frac{\sin x - y}{y \cos x + 1}$

$$r(\cos \alpha + i) \neq 0 \quad \cos \alpha \neq \frac{\alpha \pi}{\pi}, \frac{\sqrt{\pi}}{\pi}$$

$$\cos \alpha \neq -\frac{1}{\sqrt{2}}$$


$$D_F = R - \left\{ rkn + \frac{\gamma n}{r}, \gamma kn + \frac{\gamma n}{r} \right\}$$

ج) $\frac{\sin x + 1}{\cos x - 1} \Rightarrow \cos x - 1 \neq 0$
 $\cos x \neq 1$

$$D_F = R - \{ \pi K \pi + 0 \} = \sqrt{D_F = R - \{ \pi K \pi \}}$$

الف) $\frac{2\sin x + 1}{\tan x + 1}$

$$\tan \lambda + 1 \neq 0$$

$$\tan x = \frac{\sin x}{\cos x}$$

$$\cos \alpha \neq 0 \quad \cos \alpha \neq \frac{q_0}{\sqrt{q_0^2 + v_{v0}^2}}$$

$$\tan \alpha \neq \frac{r_1}{\epsilon}, \frac{r_2}{\epsilon}$$

$$D_F = \mathbb{R} - \left\{ k\pi + \frac{\pi}{4}, k\pi - \frac{\pi}{4} \right\}$$

$$c) \frac{\cos x + 1}{\cot x - 1}$$

$$\cot x - 1 \neq 0$$

$$\cot \alpha = \frac{\cos \alpha}{\sin \alpha} = 4 \sin \alpha \neq 0 \quad \sin \alpha \neq 0, 1, 0$$

$$\cot x - 1$$

$\cot \alpha \neq 1$ 7

$$\cot x \neq \tan^{-1} x, \text{ and } \tan^{-1} x \neq \cot x$$

$$DF = R_i - \left\{ K\pi, K\pi + \frac{\pi}{K} \right\}$$

الف) $\sin y = x^2 - 2$

$$-1 \leq x-2 \leq 1 \rightarrow +1 \leq x \leq 3 \Rightarrow 1 \leq x \leq 3$$

$$-1 \geq x \geq -3$$

$$Df = \begin{bmatrix} +1 & +\sqrt{x} \end{bmatrix} \vee \begin{bmatrix} -\sqrt{x} & -1 \end{bmatrix}$$

c) $y = \arccos(\sqrt{x} - 4)$

$$-1 \leq \sqrt{x-3} \leq 1 \Rightarrow -1 \leq \sqrt{x-3} \leq 1 \Rightarrow -1 \leq x-3 \leq 1 \Rightarrow -2 \leq x \leq 4$$

$$DF = [f(14)]$$

الف) $\cos y = |x| - 3$

$$-1 \leq |x| - 3 \leq 1$$

$$\begin{array}{l} \gamma \leq 1 \leq \gamma \leq \gamma \\ \swarrow \searrow \\ \gamma \leq \gamma \leq \gamma \quad -\gamma \leq \gamma \leq -\gamma \end{array}$$

$$D_f = [-r_c - r] \cup [r, t]$$

c) $y = \arcsin(x^2 + 3x + 1)$

$$-1 \leq x^2 + 3x + 1 \leq 1 \Leftrightarrow 0 \leq x^2 + 3x + 2 \leq 2 \Leftrightarrow 0 \leq (x+1)(x+2) \leq 2$$

$$\begin{array}{c} \text{O} \quad \text{O} \\ | \quad | \\ \text{---} \\ + \quad - \quad - \quad - \quad + \end{array}$$

$= 4$

$x < 4$

$$\Rightarrow \boxed{Df = [-36 - 2] \cup [-160]}$$

الف) $y = \log_3 x^{2-4}$

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$x < -2$

$$P_F = (-\infty, -r) \cup (r, +\infty)$$

$$b) y = \log \frac{r-121}{r}$$

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$x < y$

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$$Y - |X| \geq 0$$

$|x| < r$

$$\begin{array}{ccc} & & 0 \\ & | & | \\ -\gamma & & \gamma \\ 0 & & \end{array}$$

$$Df = (-r, r)$$