

$$y = \arccos(\sqrt{x} - 2) = x \geq 0$$

$$-1 \leq \sqrt{x} - 2 \leq 1 \quad \sqrt{x} - 2 \geq -1 \rightarrow \sqrt{x} \geq 1 \quad x \geq 1$$

$$\sqrt{x} - 2 \leq 1 \quad \sqrt{x} \leq 3 \quad x \leq 9 \quad 1 \leq x \leq 9$$

$$D_f = [1, 9]$$

$$\cos y = \sqrt{x} - 2 \quad \cos y \in [-1, 1] \quad (1)$$

$$-1 \leq \sqrt{x} - 2 \leq 1 \quad \sqrt{x} - 2 \geq -1 \quad \sqrt{x} \geq 1$$

$$\sqrt{x} - 2 \leq 1 \quad \sqrt{x} \leq 3 \quad x \leq 9$$

$$[-1, -2] \cup [2, 1]$$

$$D_f =$$

$$y = \arcsin(x^2 + 2x + 1) \quad -1 \leq x^2 + 2x + 1 \leq 1$$

$$x^2 + 2x + 1 \geq -1 \quad x^2 + 2x + 1 \geq 0 \quad (x+1)(x+1) \geq 0$$

$$x \geq -1 \quad x \geq -1 \quad \underline{x^2 + 2x + 1 \leq 1} \quad x^2 + 2x \leq 0$$

$$x(x+2) \leq 0 \quad -2 \leq x \leq 0 \quad D_f = [-2, 0] \cup [-1, 0]$$

$$y = \log_r \frac{r^r - r}{r} \quad r^r - r > 0 \quad r^r > r \quad (a)$$

$$r > r$$

$$Df = (-\infty, -r) \cup (r, \infty) \quad r < -r$$

$$y = \log_r \frac{r - |r|}{r} \quad r - |r| > 0 \quad |r| < r$$

$$Df = r \in (-r, r)$$

$$y = \log_{r-r} \frac{a-r}{r-r} \quad a-r > 0 \rightarrow r < a \quad (c)$$

$$r-r > 0 \rightarrow r > r$$

$$Df = (r, r) \cup (r, a) \quad r-r \neq 1 \rightarrow r \neq r$$

$$y = \log_{r+r} \frac{r^r - 1}{r+r} \quad r^r - 1 > 0 \rightarrow (r-1)(r+1) > 0$$

$$r > 1, r < -1$$

$$r+r > 0 \rightarrow r > -r \quad r+r \neq 1 \rightarrow r \neq -r$$

$$Df = (-r, -r) \cup (-r-1, -1) \cup (1, \infty)$$

$$y = \log \frac{r^r - r + r}{r-r} \quad \frac{r^r - r + r}{r-r} > 0 \quad (v)$$

$$\frac{(r-1)(r-r)}{r-r} = r-1, r \neq r \quad r \in (1, r) \cup (r, \infty)$$

$$y = \log \frac{n+r}{n-r}$$

$$\frac{n+r}{n-r} > 0$$

$$n > -r$$

$$n+r > 0$$

$$n+r \neq 1$$

$$n < -r$$

$$n \neq -r$$

$$n > r$$

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$$D_f = (-\infty, -r) \cup (-r, -r) \cup (r, \infty)$$

$$y = \sqrt{r - \log \frac{n-r}{r}}$$

$$n-r > 0 \rightarrow n > r$$

$$(1$$

$$r - \log \frac{n-r}{r} > 0 \rightarrow \log \frac{n-r}{r} < r$$

10

$$n-r \leq r=1 \rightarrow n \leq 1 \quad D_f = (r, 10]$$

$$y = \log(r \log \frac{n}{r} - 1)$$

$$r \log \frac{n}{r} - 1 > 0$$

$$r \log \frac{n}{r} > 1$$

$$\log \frac{n}{r} > \frac{1}{r}$$

$$\log \frac{n}{r} > \frac{1}{r} \rightarrow n > \sqrt{r}$$

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$$n \in (\sqrt{r}, \infty)$$

$$y = \frac{r}{r^n + 1}$$

$$r^n + 1 > 0 \rightarrow n \in \mathbb{R}$$

$$(9$$

$$D_f = \mathbb{R}$$

20

$$y = \frac{r}{r^n - 1}$$

$$r^n - 1 \neq 0 \rightarrow r \neq 1 \quad n \neq 0$$

$$D_f = \mathbb{R} - \{0\}$$

$$y = \frac{r}{e^m - r} \quad e^m - r \neq 0 \rightarrow e^m \neq r \rightarrow m \neq \frac{1}{r}$$

$$D_f = \mathbb{R} - \left\{ \frac{1}{r} \right\}$$

$$y = \frac{r}{e^m - r} \rightarrow e^m - r \neq 0 \quad e^m \neq r \rightarrow m \neq \log_e r$$

$$D_f = \mathbb{R} - \left\{ \log_e r \right\}$$

$$10 \quad y = (e^m + 1) \mid \quad e^m + 1 \in \mathbb{W} \quad (10)$$

$$e^m + 1 = n$$

$$m \in \left\{ -\frac{1}{e}, 0, \frac{1}{e}, \frac{1}{r}, \frac{r}{e}, \frac{1}{r} \right\} \dots \quad m = \frac{n-1}{e} \rightarrow n = 0, 1, 2$$

$$n \in \mathbb{Z} \geq 0 \rightarrow \frac{n-1}{e} \quad D_f = \left\{ m = \frac{n-1}{e}, n = 0, 1, 2, \dots \right\}$$

$$15 \quad \left(\frac{r^m - r}{r^m - \omega} \right) \mid = \quad r^m - \omega \neq 0 \rightarrow m \neq \frac{\omega}{r}$$

$$\frac{r^m - r}{r^m - \omega} = n, n \in \{0, 1, 2, \dots\}$$

$$r^m - r = n(r^m - \omega)$$

$$20 \quad r^m - r = r^n m - \omega n$$

$$r^m - r^n m = -\omega n + r \rightarrow m(r - r^n) = r - \omega n$$

$$\therefore m = \frac{r - \omega n}{r - r^n} \rightarrow m \neq \frac{r}{r} \Rightarrow n = 0, 1, 2$$