

الف) $y_1'' = 2x^2 - x$ $y_2'' = 2x^2 - x$ $y_1' = y_2'$ $y_1 = y_2$ تابع هستند ✓
 ج) $\sqrt{x-4} + |y-2| = 0$ $y-2=0$ $x-4=0$ $x=4$ $y=2$ $\Rightarrow$ تابع نیست $\Rightarrow$ رازان $(4,2)$

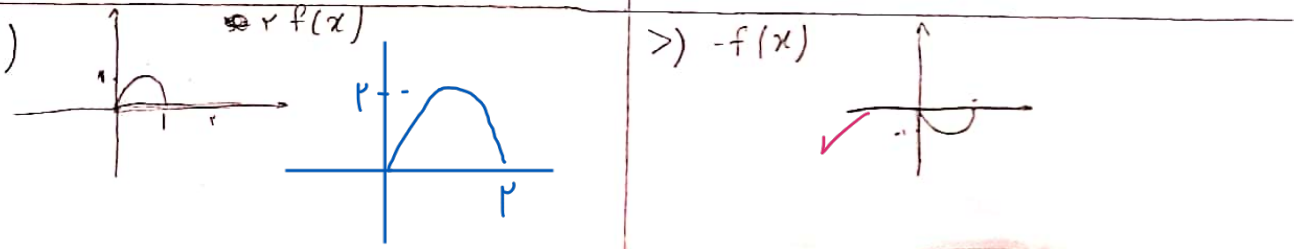
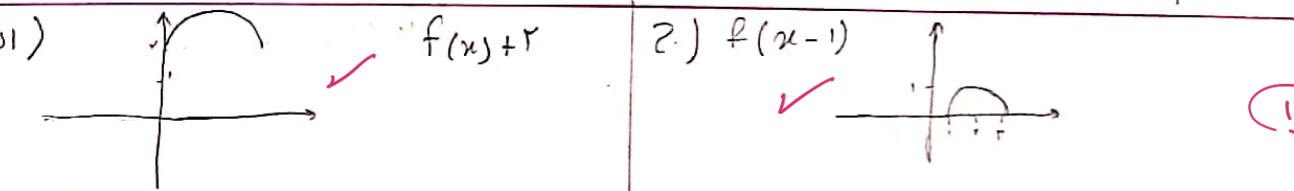
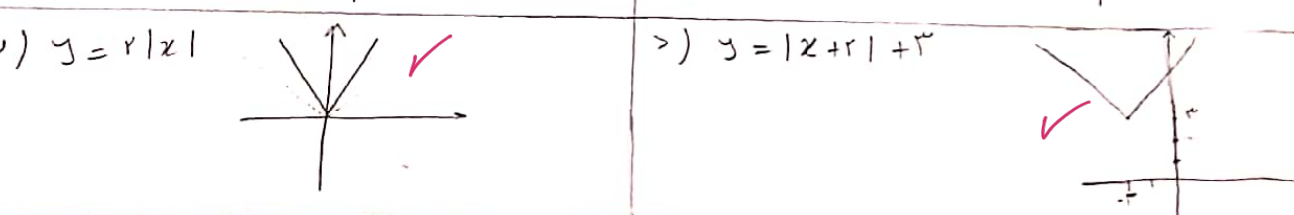
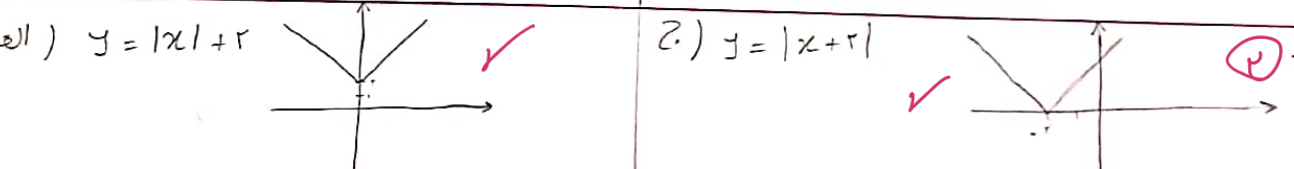
ب) $|y| + x^2 = x + 2 \xrightarrow{x=0} |y| = 2 \Rightarrow y = \pm 2$ تابع نیست ✓
 ج) $x = \cos y \xrightarrow{x=0} \cos y = 0 \Rightarrow y = \{\frac{\pi}{2}, \frac{3\pi}{2}, \dots\}$ ✓

الف) $y = \frac{x+4}{x^2-4x}$ $x^2-4x \neq 0$ $x(x-4) \neq 0$ $x \neq 0, 4$ $Df = R - \{0, 4\}$ ✓
 ج) $y = \frac{x+4}{x^2+x+4}$ $x^2+x+4 \neq 0$ $\Delta = 1-16 < 0$ $\Rightarrow$ خارج می‌شود صفر نمی‌شود $Df = R$ ✓

ب) $y = \frac{x+4}{x^2-7x+14}$ $x^2-7x+14 \neq 0$ $\Delta = 49-56 < 0$ $\Rightarrow$ خارج می‌شود صفر نمی‌شود $Df = R$ ✓
 ج) $y = \frac{x+4}{x^2-4x}$ $x^2-4x \neq 0$ $x^2(x-4) \neq 0$ $x \neq 0, 4$ $Df = R - \{0, 4\}$ ✓

الف) $\sqrt{4-x} + \sqrt{x-2}$ $\begin{cases} 4-x \geq 0 \\ x-2 \geq 0 \end{cases} \Rightarrow \begin{cases} x \leq 4 \\ x \geq 2 \end{cases} \Rightarrow x \in [2, 4]$ ✓
 ج) $\frac{\sqrt{x-2}}{x-4}$ $\begin{cases} x-2 \geq 0 \\ x-4 \neq 0 \end{cases} \Rightarrow \begin{cases} x \geq 2 \\ x \neq 4 \end{cases} \Rightarrow Df = [2, \infty) - \{4\}$ ✓

ب) $y = \frac{x+1}{x^2+1}$ $x^2+1 \neq 0$ $Df = R$ ✓
 ج) $y = \frac{x+3}{|x|+x^2}$ $|x|+x^2 \neq 0$ $Df = R - \{0\}$ ✓



الف) $(x-2)(x-3)(x-4)$

Sign chart: $- \quad + \quad - \quad +$ with roots at 2, 3, 4.

ب) $(x-2)(x-3)^2(x-4)$

Sign chart: $+ \quad - \quad - \quad +$ with roots at 2, 3, 4.

الف) $\frac{(x-2)(x-4)}{x-3}$

Sign chart: $- \quad + \quad - \quad +$ with roots at 2, 3, 4.

ب) $\frac{(x-2)(x-4)}{(x-3)^2}$

Sign chart: $+ \quad - \quad - \quad +$ with roots at 2, 3, 4.

الف) $\frac{x^3 - 3x^2 + 2x}{x-3} = \frac{(x-1)(x^2 + x - 2)}{x-3}$

$= \frac{(x-1)(x+2)(x-1)}{x-3}$

Sign chart: $+ \quad - \quad - \quad +$ with roots at 1, 2, 3.

ب) $\frac{x^3 - 3x^2 + 2x}{x^2 - 2x + 3}$

Sign chart: $+ \quad + \quad - \quad +$ with roots at 1, 2.

الف) $\frac{x^3 - x^2}{x^2 + x + 2} = \frac{x^2(x+1)(x-1)}{x^2 + x + 2}$

Sign chart: $+ \quad - \quad - \quad +$ with roots at 1, -1.

ب) $\frac{x^2 + 3x + 2}{x^2 + 2x + 3}$

Sign chart: $+ \quad + \quad + \quad +$ with no real roots.

صورت و مخرج هیچگاه صفر نمی شوند
و عبارت همواره مثبت است

الف) $\sqrt{\frac{x^3-1}{x^2-x}} \geq 0 \Rightarrow \frac{(x-1)(x^2+x+1)}{x(x^2-1)} \geq 0$

Sign chart: $+ \quad - \quad + \quad +$ with roots at 1, 0.

$D_f = (-\infty, -1) \cup (0, 1) \cup (1, +\infty)$

ب) $\sqrt{\frac{x^2-1}{x^2-2x+3}} \geq 0 \Rightarrow \frac{(x-1)(x+1)}{(x-1)(x-3)}$

Sign chart: $+ \quad - \quad + \quad +$ with roots at 1, 3.

$D_f = [-\infty, -1] \cup (1, 3) \cup (3, +\infty)$