

الف) $t_n = 3n^2 - 1$ $2, 11, 22, 47, 74, \dots$ (۱)

ب) $t_n = \frac{n+1}{n+5}$ $\frac{10}{5}, \frac{9}{6}, \frac{8}{7}, \frac{7}{8}, \frac{6}{9}, \frac{5}{10}, \dots$ (۲)

الف) $t_n = \frac{(-1)^n}{\sqrt{n+4}}$ $= \frac{(-1)^{13}}{\sqrt{13+4}} = \frac{-1}{\sqrt{17}}$ (۲)

ب) $t_n = 2n - [\frac{n}{5}]$ $2 \times 13 - [\frac{13}{5}] = 24 - 2 = 22$ (۲)

الف) $t_n = 2n - 10$ $2n - 10 < 0 \Rightarrow n < 5$ $(5-1)+1 = 4$ (۲)

ب) $t_n = n^2 - 14n + 40$ $(n-10)(n-4) < 0$ $4 < n < 10$ $(9-4)+1 = 5$ (۲)

الف) $t_n = 2n - 14$ $2n - 14 < 0 \Rightarrow n < 7$ $(7-1)+1 = 7$ (۲)

ب) $t_n = n^2 - 12n + 27$ $(n-3)(n-9) < 0$ $3 < n < 9$ $(9-3)+1 = 7$ (۲)

$\begin{cases} a(4) + b = 7 \\ a(1) + b = 2 \end{cases} \Rightarrow \begin{cases} 4a + b = 7 \\ a + b = 2 \end{cases} \Rightarrow \begin{cases} 3a = 5 \\ a = \frac{5}{3} \end{cases}$ $b = -\frac{1}{3}$ (۲)

الف) $t_n = n^2 - 9n + 2$ $\frac{-b}{2a} = \frac{9}{2} = 4.5$ $9 - 1 \times 4.5 = 4.5$ (۲)

ب) $t_n = n^2 + 8n + 1$ $\frac{-b}{2a} = -4$ $1 - 1 \times (-4) = 5$ $t_1 = 4, t_2 = 13 \rightarrow t_{min} = t_1 = 4$ (۲)

$t_n = -1, -4, -9, -16, -25, \dots$ $a = -1, a = 1$ $t_1 = 1 + b + c = -1 \Rightarrow b + c = -2$ $t_2 = 4 + 2b + c = -4 \Rightarrow 2b + c = -8$ $b = -6, c = 4$ (۲)

$$t_n = -4, -1, 1, 11, \dots$$

Diagram showing a sequence of points on a number line with arrows indicating differences: $-4 \xrightarrow{5} -1 \xrightarrow{2} 1 \xrightarrow{10} 11$. The differences are labeled 5, 2, and 10.

$$t_a = f$$

$$a = 2$$

$$t_1 = 2 + b + c = -4 \Rightarrow -b - c = 6 \quad (1)$$

$$t_2 = 1 + 2b + c = -1 \Rightarrow 2b + c = -2$$

$$b = -1$$

$$2 + (-1) + c = -4$$

$$c = -5$$

$$G_{n+1} = 2n - n \quad \checkmark$$

$$(-\infty, a+f] \cup [a+1, +\infty)$$

$$a+1 \geq a+f$$

$$a \geq f$$

$$[f, +\infty)$$

(2)

$$1 < n < 100$$

$$(100-1) + 1 = 100$$

$$\frac{1}{n} < n < \frac{100}{n}$$

$$1 < n < 100$$

$$1 < n < 100$$

$$(100-1) + 1 = 100$$

$$1 < n < 100$$

$$1 < n < 100$$

$$(100-1) + 1 = 100$$

$$1 < n < 100$$

$$(100+100) - 100 = 200$$

(b) الف

(2)

(c)

(d)

(e)