

$$(1) \quad y = x^2 - 5 \quad \rightarrow \quad \sqrt{x^2} = \sqrt{y+5}$$

$$x = \pm \sqrt{y+5} \quad \rightarrow \quad y+5 \geq 0$$

$$y \geq -5$$

$$R_f = [-5, +\infty)$$

$$(ب) \quad y = x^2 + 1 \quad R_f = [1, +\infty)$$

$$(2) \quad (الف) \quad y = x^2 - 2x + 4 \quad \rightarrow \quad y = x^2 - 2x + 1 + 3$$

$$y = (x-1)^2 + 3$$

$$\sqrt{y-3} = \sqrt{(x-1)^2} \quad \rightarrow \quad x-1 = \pm \sqrt{y-3}$$

$$x = 1 \pm \sqrt{y-3}$$

$$y-3 \geq 0$$

$$y \geq 3 \Rightarrow R_f = [3, +\infty)$$

$$(ب) \quad y = x^2 - 2x + 1 + \frac{y+1}{2} - \frac{y+1}{2}$$

$$y = x^2 - 2x + \frac{y+1}{2} - \frac{y+1}{2} \quad \rightarrow \quad y = (x - \frac{1}{2})^2 - \frac{y+1}{2}$$

$$R_f = [-\frac{y+1}{2}, +\infty)$$

$$\sqrt{y + \frac{y+1}{2}} = \sqrt{(x - \frac{1}{2})^2}$$

$$x = \frac{1}{2} \pm \sqrt{y + \frac{y+1}{2}} \quad \rightarrow \quad y + \frac{y+1}{2} \geq 0$$

$$\Rightarrow y \geq -\frac{y+1}{2}$$

$$(3) \quad (الف) \quad y = \frac{x^2 + 3}{x^2 - 1} \quad \rightarrow \quad yx^2 - y = x^2 + 3$$

$$yx^2 - x^2 = y + 3$$

$$x^2(y-1) = y+3$$

$$\sqrt{x^2} = \sqrt{\frac{y+3}{y-1}} \quad \rightarrow \quad x = \pm \sqrt{\frac{y+3}{y-1}}$$

$$\frac{y+3}{y-1} \geq 0$$

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$$y+3 \geq 0 \Rightarrow y \geq -3$$

$$y-1 > 0 \Rightarrow y > 1$$

$$\frac{-\frac{3}{2}}{+\frac{1}{2} - \frac{1}{2} +} \Rightarrow R_f = (-\infty, -\frac{1}{2}] \cup (1, +\infty)$$

$$y = \frac{y|n|+1}{|n|-\varepsilon} \rightsquigarrow y|n| - \varepsilon y = y|n|+1$$

$$y|n| - y|n| = \varepsilon y + 1$$

$$|n|(y-\varepsilon) = \varepsilon y + 1$$

$$|n| = \frac{\varepsilon y + 1}{y - \varepsilon} \rightsquigarrow \frac{\varepsilon y + 1}{y - \varepsilon} > 0 \text{ چون مخرج و صورت مثبت است}$$

$$R_f = (-\infty, -\frac{1}{\varepsilon}] \cup (\frac{1}{\varepsilon}, +\infty) \leftarrow \frac{-\frac{1}{\varepsilon}}{+\infty - \frac{1}{\varepsilon}} \leftarrow \begin{cases} \varepsilon y + 1 > 0 \rightarrow y > -\frac{1}{\varepsilon} \\ y - \varepsilon > 0 \rightarrow y > \varepsilon \end{cases}$$

$$y = \frac{1}{n^2 - \varepsilon n} \rightsquigarrow y n^2 - \varepsilon n y = 1$$

$$y n^2 - \varepsilon n y - 1 = 0 \rightsquigarrow \Delta = b^2 - 4ac$$

$$\Delta = 14y^2 + 4y$$

$$n = \frac{-b \pm \sqrt{\Delta}}{2a} \rightsquigarrow n = \frac{\varepsilon y \pm \sqrt{14y^2 + 4y}}{\varepsilon y}$$

$$14y^2 + 4y > 0 \rightsquigarrow \varepsilon y(\varepsilon y + 1) > 0 \rightsquigarrow \varepsilon y > 0 \quad \varepsilon y > 0 \rightarrow y > 0$$

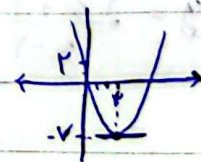
$$\frac{-\frac{1}{\varepsilon}}{+\infty - \frac{1}{\varepsilon}} \rightarrow (-\infty, -\frac{1}{\varepsilon}] \cup (\frac{1}{\varepsilon}, +\infty)$$

$$\varepsilon y + 1 > 0 \rightsquigarrow \varepsilon y > -1 \rightsquigarrow y > -\frac{1}{\varepsilon}$$

$$\text{الف) } n^2 - 4n + 2 \rightsquigarrow \text{Min} \left| \frac{-b}{2a} = \frac{4}{2} = 2 \right.$$

$$R_f = [-2, +\infty)$$

$$4 - 16 + 2 = -10$$

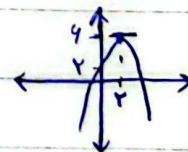


(د)

$$\text{ب) } -n^2 + \varepsilon n + 2$$

$$\text{Max} \left| \frac{-b}{2a} = \frac{-\varepsilon}{-2} = \frac{\varepsilon}{2} = 2 \right.$$

$$-4 + 16 + 2 = 14$$



$$R_f = (-\infty, 2]$$

الف) $y = \sqrt{x^2 - 4x + 2}$ Min $\frac{-b}{2a} = \frac{4}{2} = 2$ (4)

$R_f = \sqrt{[-7, +\infty)} = [0, +\infty)$ $9 - 4x + 2 = -7$

ب) $y = \sqrt{-x^2 + 4x + 10}$ Max $\frac{-b}{2a} = \frac{-4}{-2} = 2$

$R_f = \sqrt{(-\infty, 14]} = [0, \sqrt{14}]$ $-x^2 + 4x + 10 = 14$

الف) $y = x^3 + 3x^2 + 2x + 1$ $R_f = \mathbb{R}$ بزرگترین توان فرد $\Leftarrow$ (7)

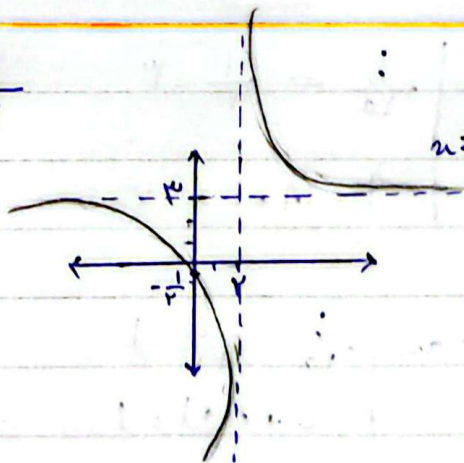
ب) $y = \sqrt{x^5 + 4x^2 + 4x + 1}$ بزرگترین توان فرد است پس بر همان $\mathbb{R}$ است ولی چون زیر رادیکال است اعداد منفی را نمی توان در نظر گرفت $\Leftarrow R_f = [0, +\infty)$

الف) $y = \frac{3x+1}{x-2}$ $c \neq 0$ $bc \neq ad \Rightarrow R_f = \mathbb{R} - \{3\}$ (1)

ب) $y = \sqrt{\frac{4x+1}{x+3}}$ $\Rightarrow \frac{a}{c} = \frac{4}{1} = 4 \Rightarrow R_f = \sqrt{\mathbb{R} - \{4\}}$
 $R_f = [0, +\infty) - \{2\} = [0, 2) \cup (2, +\infty)$

الف) $y = \frac{3x+1}{x-2}$ جانب افقی $\frac{a}{c} = 3$ (9)

جانب عمودی $\frac{b}{d} = 2$ $x=2$



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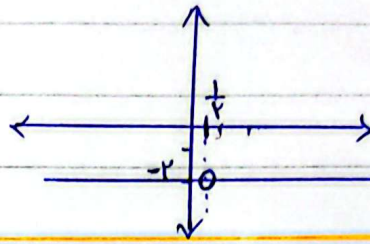
$$b) \frac{f_m - r}{1 - r_m}$$

$$1 - r_m \neq 0$$

$$m \neq \frac{1}{r}$$

شرط $ad \neq bc$ در قرار نیست

$$y = \frac{f}{-r} = -r$$



$$a) y = \cos^r m + \frac{1}{\cos^r m} \rightsquigarrow a + \frac{1}{a} \xrightarrow{\text{if}} a > 0 \rightarrow [r, +\infty) \quad (10)$$

$$\cos^r m > 0 \Rightarrow R_f = [r, +\infty)$$

$$b) y = \sqrt[r]{\frac{m^r + 1}{m}} \Rightarrow y = \sqrt[r]{m + \frac{1}{m}} \Rightarrow m + \frac{1}{m} \rightarrow (-\infty, -r] \cup [r, +\infty)$$

$$R_f = \sqrt[r]{(-\infty, -r] \cup [r, +\infty)}$$

$$R_f = (-\infty, \sqrt[r]{-r}] \cup [\sqrt[r]{r}, +\infty)$$