

$y = \sqrt{n f(n)} / y = f(n)$
 $\hookrightarrow n f(n) \geq 0$

	-7	-5	0	2	5
x	-	-	0	+	+
$f(x)$	+	0	-	-	0
$x f(x)$	-	0	+	-	+

$D_f = [-5, 0] \cup [2, 5]$

1

$y = \sqrt{\frac{-x}{f(x)}} \geq 0 \rightarrow \frac{-x}{f(x)} \geq 0$

	-3	0	2	5
x	-	+	+	-
$f(x)$	+	-	-	+

$D_f = [(-3, 0) \cup (0, 2)]$

2

$f(x) = 2f(2) = x^2 - 2x + 2 / f(-2) = ?$

$x = 2 \rightarrow f(2) - 2f(2) = 2 - 4 + 2 \rightarrow -f(2) = 2 \rightarrow f(2) = -2$

$x = -2 \rightarrow f(-2) - 2f(-2) = 4 + 4 + 2 \rightarrow f(-2) + 2 = 12 \rightarrow f(-2) = 10$

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$f(x) = \begin{cases} x - \sqrt{x+2} \rightarrow x > 2 \\ 2x+2 \rightarrow x \leq 2 \end{cases}$

$f(4) + f(2) = ? \rightarrow \sqrt{9} = 3$

$f(4) \rightarrow 4 - \sqrt{4+2} = 4 - \sqrt{6} = 2$

$f(2) \rightarrow 2 \times 2 + 2 = 6$

$f(4) + f(2) = 2 + 6 = 8$

4

$f(x) = ax^2 - bx + 2$

$f(x-1) - f(x) = 4x+2 \rightarrow a-b = ?$

$x=1 \rightarrow f(1) = a - b + 2$

$f(1) - f(1) = 4 + 2 \rightarrow 2 - f(1) = 1 \rightarrow 2 - 1 = f(1) \rightarrow f(1) = 1$

$x=0 \rightarrow f(0) = 2$

$-4 = a - b + 2 \rightarrow a - b = -6$

5

$f(n) = \frac{n^2 + \epsilon n + \alpha}{n^2 + \epsilon n + \gamma}$ | $f(\sqrt{3}-2) = ?$

$\frac{n^2 + \epsilon n + \alpha}{n^2 + \epsilon n + \gamma} + \frac{n^2 + \epsilon n + \alpha}{n^2 + \epsilon n + \gamma} \rightarrow 1 + \frac{n^2 + \epsilon n + \alpha}{n^2 + \epsilon n + \gamma}$

$1 + \frac{(\sqrt{3}-2)^2 + \epsilon(\sqrt{3}-2) + \alpha}{(\sqrt{3}-2)^2 + \epsilon(\sqrt{3}-2) + \gamma}$

$1 + \frac{3 + \epsilon\sqrt{3} - 4 + \epsilon\sqrt{3} - 1 + \alpha}{3 + \epsilon\sqrt{3} + \epsilon\sqrt{3} - 1 + \gamma}$

$\rightarrow 1 + \frac{\epsilon}{1}$

+α

6

$f(n - \frac{1}{n}) = \frac{n^2 + 1}{n^2}$ | $f(-2) = ? \rightarrow x - \frac{1}{n} = -2 \rightarrow n + \frac{1}{n} = -2 \rightarrow n^2 + 1 = -2n \rightarrow n^2 + 2n + 1 = 0$

$\Delta = b^2 - 4ac = 4 - 4 = 0$
 $n = \frac{-b \pm \sqrt{\Delta}}{2a} = \frac{-2 \pm 0}{2} = -1$

$f(-2) \Rightarrow \frac{n^2 + 1}{n^2} \rightarrow \frac{(-2)^2 + 1}{(-2)^2} = \frac{5}{4}$

$\frac{(-2n+1) \times (-2n+1) + 1}{(-2n+1)^2} \rightarrow \frac{4n^2 - 4n + 1 + 1}{4n^2 - 4n + 1} \rightarrow \frac{4n^2 - 4n + 2}{4n^2 - 4n + 1}$

$\frac{4n^2 - 4n + 2}{4n^2 - 4n + 1} \rightarrow \frac{4n^2 - 4n + 1 + 1}{4n^2 - 4n + 1} \rightarrow 1 + \frac{1}{4n^2 - 4n + 1}$

$\frac{1}{4(-2)^2 - 4(-2) + 1} = \frac{1}{16 + 8 + 1} = \frac{1}{25}$

5

1

7

$f(n) = \{(2, 0), (1, -2), (0, 2), (7, 1)\}$

$g(n) = \sqrt{9 - n^2} \rightarrow 9 - n^2 \geq 0 \rightarrow 9 \geq n^2 \rightarrow -3 \leq n \leq 3$

الف) $\frac{f}{g} \rightarrow \{(2, \frac{0}{\sqrt{5}}), (1, \frac{-2}{\sqrt{8}}), (0, \frac{2}{\sqrt{9}})\}$

ب) $\frac{g}{f} \rightarrow \{(2, \frac{\sqrt{5}}{0}), (1, \frac{\sqrt{8}}{-2}), (0, \frac{\sqrt{9}}{2})\}$

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$f(n) = \{(2, 1), (3, 2), (-5, 2), (1, -2)\}$

ا) $2f(n) \rightarrow \{(2, 2), (3, 4), (-5, 4), (1, -4)\}$

ب) $f(n) + 1 \rightarrow \{(2, 2), (3, 3), (-5, 3), (1, -1)\}$

ج) $3f(n) + 1 \rightarrow \{(2, 4), (3, 6), (-5, 6), (1, 3)\}$

د) $f(2n) \rightarrow \{(1, 1), (\frac{3}{2}, 2), (-\frac{5}{2}, 2), (\frac{1}{2}, -2)\}$

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$f(n) = \{(2, 2), (7, 2), (1, 2), (3, 1), (5, 2)\}$

$g(n) = \{(0, 0), (0, 1), (-1, 2), (-2, -2), (0, -1)\}$

ا) $f - g \rightarrow \{(2, 2), (1, 2), (3, 2)\}$

ب) $2 \frac{f}{g} \rightarrow \{(2, \frac{2}{0}), (1, \frac{2}{1}), (3, \frac{2}{-1})\}$

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